# PREDICTION OF SAILING BOAT PERFORMANCE

Edmund Colby Munger

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# PREDICTION OF SAILING BOAT PERFORMANCE

by

EDMUND COLBY MUNGER

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Submitted to the Department of Ocean Engineering on May 7, 1976 in partial fulfillment of the requirements for the degrees of Master of Science in Naval Architecture and Marine Engineering and Naval Architect.

## ABSTRACT

Mathematical models are developed for the hydrodynamic and aerodynamic forces which act on a sailing boat. The solution of the force and moment equilibrium provides the sailing boat's speed and attitude for performance prediction. Each force model is evaluated for its capability to make adequate engineering predictions. Further, expressions are given for the dimensions and coefficients to provide a feasible baseline design to which parametric variations may be made.

The system of force equations constitute a parameterized system model in four degrees of freedom for steady state sailing conditions. The mathematical model provides a design tool for the naval architect conducting geometric parameter trade-off analysis against hydrodynamic performance.

The principal result is a computerized model which is capable of predicting boat speed, heel angle, leeway angle and rudder angle for a geometrically defined sailing boat in a given wind condition. Example boats are evaluated and the results recorded in order to demonstrate the use and versatility of the model.

Thesis Supervisor: Jerome H. Milgram
Title: Professor of Ocean Engineering

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## NOMENCLATURE

$A_k$ = keel cross-sectional area.

$A_l$ = projected lateral area of the hull above the LWL.

$A_m$ = cross-sectional area of the maximum hull station, or cross-sectional area of mast depending on context.

$A_r$ = platform area of the rudder.

$A_s$ = total area of the sails.

$A_t$ = projected transverse area of the hull above the LWL.

BWL = maximum waterline beam.

$C_{dc}$ = rudder cross flow drag coefficient.

$C_{do}$ = rudder section form drag coefficient.

$C_{dis}$ = sail induced drag coefficient.

$C_f$ = friction drag coefficient.

$C_{ffb}$ = fairbody friction drag coefficient.

$C_{fk}$ = keel friction drag coefficient.

$C_{fm}$ = hull form drag coefficient.

$C_{fr}$ = rudder friction drag coefficient.

$C_{lr}$ = rudder lift coefficient.

$C_{ls}$ = sail lift coefficient.

$C_{\bar{mc}/4}$ = rudder moment coefficient about the mean quarter chord.

$C_n$ = rudder normal force coefficient.

$C_p$ = prismatic coefficient.

$C_{po}$ = parent prismatic coefficient.

$C_{popt}$ = optimum prismatic coefficient.

$C_{xr}$ = rudder drag coefficient.

$C_y$ = keel side force coefficient

$C_{ysb}$ = slender-body side force coefficient.

$C_{yr}$ = rudder side force coefficient.

$D_s$ = sail drag

$D_{so}$ = offwind sail drag.

$F_h$ = aerodynamic hull force.

$F_n$ = Froude Number.

H = maximum canoe body draft.

K = heeling moment.

$K_h$ = hydrostatic righting moment

$K_k$ = keel heeling moment.

$K_r$ = rudder heeling moment.

$K_s$ = sail heeling moment.

L = load waterline length.

$L_s$ = sail lift.

$L_{so}$ = offwind sail lift.

LCB = position of center of buoyancy (%LWL).

$LCB_o$ = parent position of center of buoyancy.

$LCB_{opt}$ = optimum location of center of buoyancy.

LWL = load waterline length.

M = pitching moment

N = yawing moment

$N_k$ = keel yawing moment.

$N_r$ = rudder yawing moment.

$N_{sb}$ = slender-body yawing moment.

$N_{sx}$ = yawing moment due to sail driving force.

$N_{sy}$ = yawing moment due to sail side force.

$\bar{P}$ = vector of assumed variable values.

$P_{1,2,3, \text{ or } 4}$ = assumed value of individual variable.

$R_f$ = total frictional resistance.

$R_{fm}$ = total form resistance.

$R_n$ = Reynold's Number.

$R_u$ = upright resistance.

$R_w$ = wave resistance.

$R_{wp}$ = parent wave resistance.

$\bar{R}$ = vector of force equilibrium errors.

$R_{1,2,3, \text{ or } 4}$ = individual force equilibrium errors.

$S_{fb}$ = fairbody wetted surface.

$S_k$ = keel wetted surface.

$S_r$ = rudder wetted surface.

$T_c$ = canoe body maximum draft.

$U_b$ = boat velocity in the $X_o$ direction.

$V_a$ = apparent wind velocity.

$V_b$ = boat velocity parellel to the y axis.

$V_t$ = true wind velocity.

$X$ = force in the $X_o$ direction.

$X_h$ = hull resistance.

$X_k$ = keel and hull induced drag.

$X_o$ = axis on the plane of the free surface in the direction of boat velocity.

$X_r$ = rudder induced drag.

$X_s$ = sail driving force.

$Y$ = force in the $Y_o$ direction, side force.

$Y_k$ = keel side force.

$Y_o$ = an axis on the plane of the free surface at right angles to boat velocity.

$Y_r$ = rudder side force.

$Y_s$ = sail side force.

$Z$ = force in the $Z_o$ direction, heave force.

$Z_o$ = an axis perpendicular to the free surface downward.

$a_f$ = fortriangle aspect ratio.

$a_m$ = mainsail aspect ratio.

$a_r$ = rudder aspect ratio.

$a_s$ = total sail area aspect ratio.

$b_b$ = draft at forward perpendicular.

$b_o$ = maximum draft.

$b_r$ = rudder span.

$b_{1,2,3}$ = intermediate draft measurements.

$c_{rr}$ = rudder root chord.

$c_{rt}$ = rudder tip chord.

$c_{r/4}$ = rudder quarter chord.

$\bar{c}_k$ = keel mean chord.

$\bar{c}_r$ = rudder mean chord.

$d_1$ = metacentric height/LWL.

$d_2$ = non-linear hydrostatic righting moment coefficient.

$d_3$ = Froude Number dependent righting moment coefficient.

$f_i(\ )$ = spline cubic function.

$g$ = acceleration due to gravity.

$r_o$ = canoe body draft at maximum draft measurement.

$s$ = sinkage.

$s_{ij}$ = $\partial R_i / \partial P_j$.

$t_r$ = taper ratio.

$x$ = axis in the load waterline plane along the centerline of the boat.

$x_b$ = horizontal distance to the maximum draft measurement.

$x_{cph}$ = horizontal distance to the aerodynamic center of effort on the hull.

$x_{cpk}$ = horizontal distance to center of effort on the keel.

$x_{cpr}$ = horizontal distance to the center of effort on the rudder.

$x_{cps}$ = horizontal distance to center of effort on the sail.

$x_e$ = main boom length.

$x_j$ = base of the fortriangle.

$x_m$ = horizontal distance to the mast.

$x_o$ = 0.0, location of maximum draft.

$x_{\bar{pc}/4}$ = horizontal distance from the rudder mean chord quarter point to the rudder center of effort.

$x_{rs}$ = horizontal distance to the rudder stock.

$x_{1,2,3}$ = horizontal distance from maximum draft to intermediate draft measurements.

$y$ = axis orthaginal to the x axis to starboard in the waterline plane.

$z$ = axis orthaginal to the waterline plane, downward.

$z_{cpk}$ = vertical distance to the center of effort on the keel.

$z_{cpr}$ = vertical distance to the center of effort on the rudder.

$z_{cpxs}$ = vertical distance to the sail driving force.

$z_{cpys}$ = vertical distance to the sail side force.

$z_{fb}$ = freeboard.

$z_g$ = vertical distance to the center of gravity.

$z_i$ = mast height.

$z_p$ = main hoist.

$z_{ro}$ = vertical distance from the rudder root chord to the center of effort on the rudder.

$z_{rrc}$ = vertical distance to the rudder root chord.

$\nabla_c$ = volumetric displacement of the fairbody.

$\nabla_k$ = volumetric displacement of the keel.

$\Delta$ = weight of the boat in tons.

$\alpha_r$ = rudder angle.

$\beta$ = apparent wind angle.

$\beta_u$ = upright apparent wind angle.

$\gamma$ = true wind angle.

$\delta$ = variable increment.

$\theta$ = pitch angle.

$\lambda$ = angle between boat centerline and aerodynamic hull force.

$\gamma_{H_2O}$ = kinematic viscosity of water.

$\pi$ = 3.14159

$\rho_{air}$ = density of air.

$\rho_{H_2O}$ = density of water.

$\phi$ = heel angle.

$\psi$ = leeway angle.

$\Omega$ = rudder sweep angle.

# I. INTRODUCTION

## 1.1 General

All designers of engineering systems desire a procedure for predicting the performance of their designs prior to final construction. Until lately, prediction of a sailing yacht's performance has been limited to evaluation of scale models and intuition. The development of the high speed computer and numerical techniques for rapid solution of non-linear equations has made the use of mathematical models a reasonable alternative for performance prediction. It is the purpose of this paper to present mathematical models for the forces and moments acting on a sailing boat. The solution of the force and moment equilibrium will provide the boat's speed and attitude for performance prediction.

Each force is parameterized in dimensions and coefficients, generally utilized by designers, to make the model a useful design tool for the naval architect. Further, expressions are given for the required dimensions and coefficients to provide a feasible baseline design from which parametric variations may be made. Each force model is evaluated for its capability to make adequate engineering predictions, including inherent limitations.

## 1.2 Historical Development

From the earliest days, yacht design has been called an "art". Though the use of wind propulsion for ships is ancient, the action of the forces and moments on the sailing ship is

complex and multidimensional. Historically there has been no technique for simple evaluation of the effect a change in one parameter has on the forces acting on the boat.

Until fifty years ago design evolved slowly through obervation of existing ships. Due to the inability to evaluate a change prior to incorporation into a newly constructed yacht, new designs tended to consist of only conservative changes to a previously successful design. This was understandable for failure of an innovation in the final yacht could be professionally catastrophic for the designer.

In the early 1900's, techniques were developed for predicting yacht performance from model tests. A designer could now build a relatively inexpensive model and evaluate it against other model results prior to incorporating a modification into a new design. Adequate prediction of full scale results have been limited by adverse scale effects, but the usefulness of these tests is unquestioned. Unfortunately, the cost of model testing still precludes extensive parametric trade-offs. Each parametric change requires construction and testing of individual models. Usually, the limited design budget for one yacht precludes any systematic variation of parameters, and testing is limited to one or two candidate models. The appeal of a parameterized mathematical model which is inexpensive to utilize is apparent.

The idea of using mathematical expressions for describing yacht performance is by no means a new concept. The rating rules used to handicap yachts are an attempt to apply mathematical models to boat performance. Because rating rules attempt to measure a boat's speed potential for a large range of conditions and reduce the results to a single number, it is easily understood why they have little application to predicting performance for a given wind direction and speed.

It was not until the second half of this century that towing tank test results were combined with sail force coefficients in a computer to solve force and moment equilibriums. These programs could provide prediction of performance for a given condition within the limitations of the data. These solutions were for the specific boat tested and a scaled family of geometrically similar boats.

In the early 1970's attempts for steady state solution from mathematical models began to be published. One pioneer in the field has been John S. Letcher, publishing parts of his model in references (1), (2), and (3). Further work has been done by Myers (4) and Kerwin (5). The computational technique for solution of the force equilibrium condition has been described by Hazen (6).

By parameterizing forces in four degrees of freedom, the model developed in this paper grows from these previous works.

## 1.3 Overview

In order to resolve the aerodynamic, hydrodynamic and hydrostatic forces acting on a sailing boat a coordinate system and origin are established. Achieving an equilibrium of forces and moments requires that the summation of all forces and moments acting either through the origin and about the origin are equal to zero. To facilitate modeling, component forces which act independently or nearly so are identified and examined. Once the forces acting on the system and the location and direction through which they act are identified, each may be modeled and superimposed to give the required equilibrium solution.

### 1.3.1 Coordinate System

Figure 1 presents a coordinate system which describes the sailing boats velocity and attitude. The coordinate system designated by the capital letters $X_o$, $Y_o$, and $Z_o$ are located on the free surface with $X_o$ and $Y_o$ axis in the horizontal plane. The $X_o$ axis lies in the direction of the boat's motion and the $Y_o$ axis is to starboard at right angles to this velocity. The $Z_o$ axis is vertically downward.

A second coordinate system is fixed in the boat at the forward end of the waterline as presented in Figure 2. This coordinate system is designated by the small letters x, y, and z. The x axis is oriented along the fore and aft centerline on the boat's waterline with the y axis in the transverse

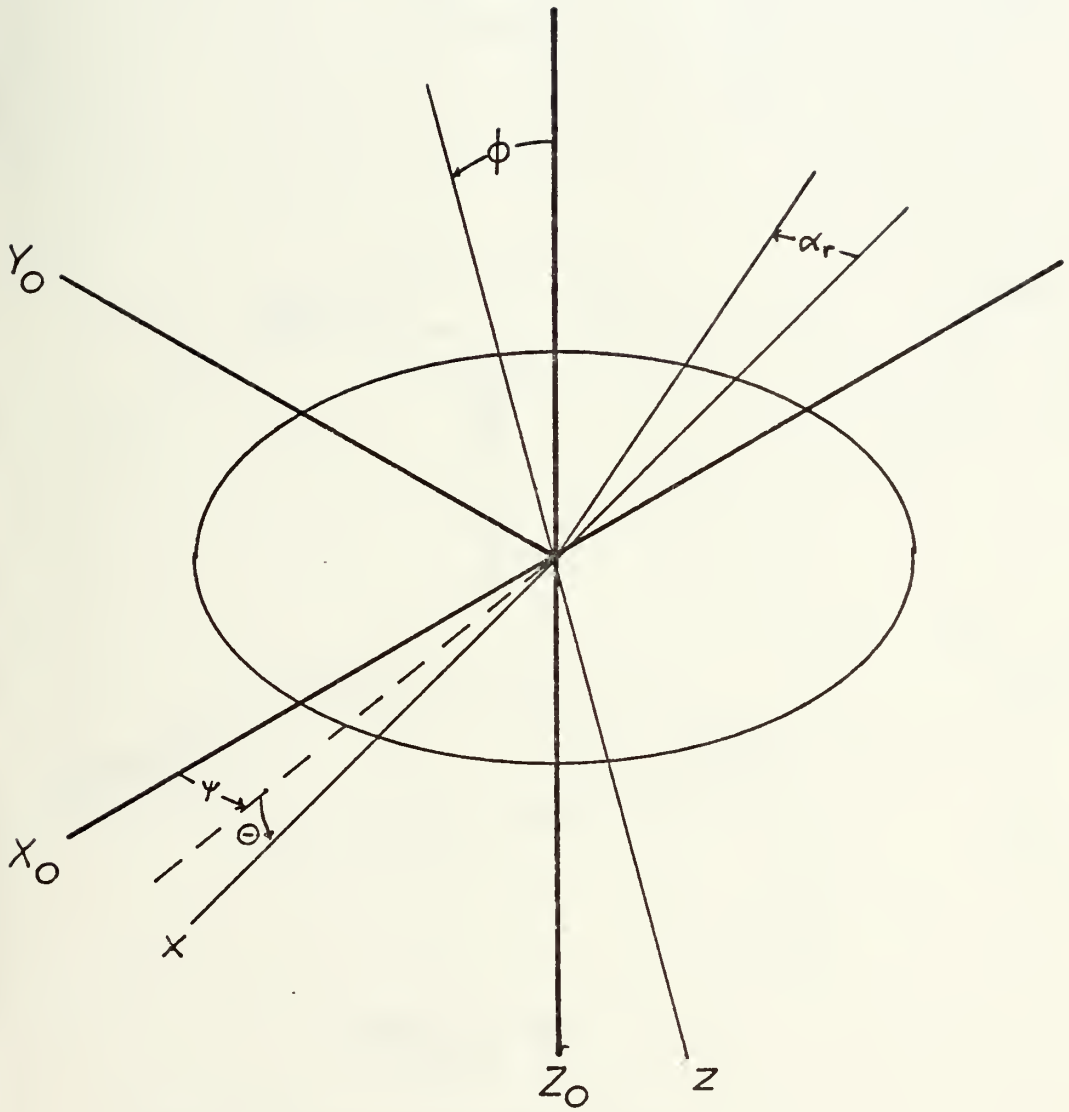



Figure 1 - Coordinate Systems

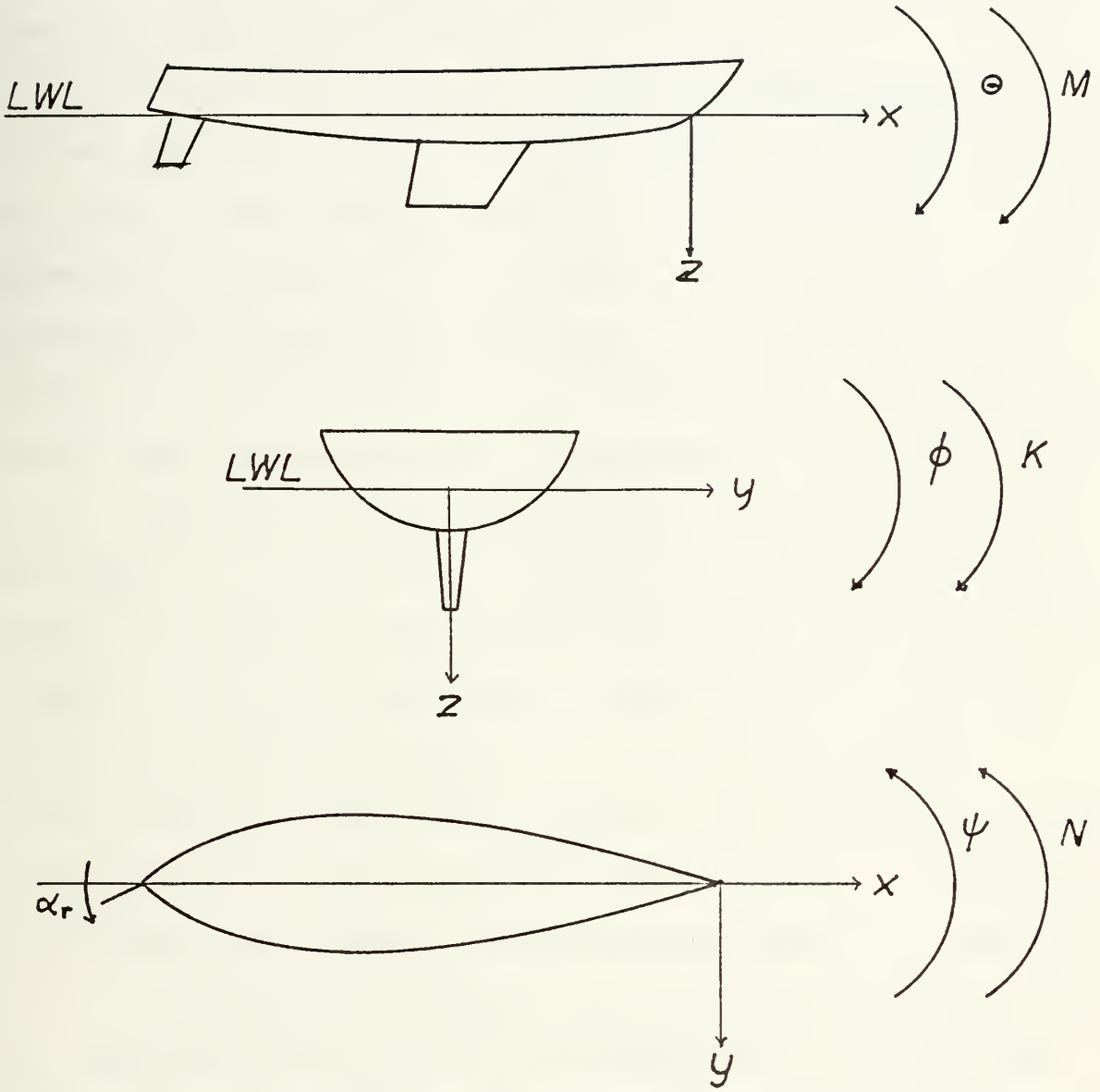



Figure 2

Boat Coordinate System

direction to starboard. The z axis desends orthogonally to the x-y plane in the direction of the keel.

The angular differences between the two coordinate systems describe the attitude of the boat as it moves through the water. The positive direction for these angles are also presented in Figure 2. Their direction was selected to provide positive values when the boat is in equilibrium under normal sailing conditions with a weather helm. The order in which these angles are taken is important to the final attitude. The boat is first rotated about the $Z_o$ axis through the angle $\psi$. The angle $\psi$ is identical to the boat's leeway angle. The boat is then rotated about the X axis, an angle $\phi$, which is the boat's heel angle. The boat is then rotated about the $Y_o$ axis, an angle $\theta$. $\theta$ is the angle by which the boat pitches down at the bow and is also the angle of the axis about which the boat heels. Finally the angle $\alpha_R$ is the angle the rudder is deflected from the boat's centerline.

A sailing boat responding to the forces acting upon it and conforming hydrostatically to deformations in the free surface would heave in the positive $Z_o$ direction an amount s.

The selection of these coordinate systems allows the modeling of forces in either coordinate system. When modeling velocity related forces, such as wave drag and lift, the coordinate system fixed in the water is more attractive computationally. On the other hand, hydrostatic forces are more easily computed in the coordinate system fixed in the

boat. In the final solution of force equilibrium, forces and moments are resolved in the $X_o$, $Y_o$, and $Z_o$ system except the heeling moment which is resolved about the x axis.

It is a common practice in naval architecture to describe a vessel's dimensions and coefficients in a positive sense. With few exceptions this is done throughout this paper. The positive direction of forces and moments is defined in Section 1.3.2.

1.3.2 Equilibrium of Forces

The forces and moments acting upon a sailing boat in these coordinate systems may be divided into six components:

X = Forces in the positive $X_o$ direction

Y = Forces in the positive $Y_o$ direction

Z = Forces in the positive $Z_o$ direction

K = Moments about the x axis

M = Moments about the y axis

N = Moments about the $z_o$ axis

The positive direction of the moments K, M, and N are taken in the same sense as the angles $\phi$, $\theta$, $\psi$ respectively as indicated in Figure 2. Under normal conditions sail aerodynamic forces will create positive forces and moments on the boat.

Through out the remainder of this paper the moments K, M, and N may be referred to interchangeably as forces or moments.

The resolution of forces into equilibrium requires that the summation of all the forces acting in the six directions be equal to zero, i.e.;

$$\Sigma X_i = \Sigma Y_i = \Sigma Z_i = \Sigma K_i = \Sigma M_i = \Sigma N_i = 0$$

where "i" designates individual aerodynamic or hydrodynamic forces or moments acting in the prescribed direction. An example of a contributing force is $X_s$, the sail driving force. This is one of a number of forces acting along the $X_o$ axis.

The achievement of an equilibrium of forces in the six directions requires the solution of six non-linear simultaneous equations. To obtain a unique solution, six variables are required. A selection of variables for the six degrees of freedom problem is:

$$(U_b, \psi, s, \phi, \theta, \alpha_r)$$

The only unidentified variable is $U_b$, which is the boat's velocity in the positive $X_o$ direction. Each variable contributes a major effect to a corresponding force. The boat's resistance is strongly dependent on boat speed, $U_b$. As leeway angle, $\psi$, strongly contributes to side force, so does heel angle, $\phi$, to the righting moment and rudder angle, $\alpha_r$, to the yaw balance.

The present model excludes the solution in heave and pitch. This exclusion of two degrees of freedom was not due to their lack of importance, but the lack of an adequate parametric model. In reality the axis about which the boat heels may be pitched as severely as 15°. This pitch makes a measurable change in the boat's angle of incidence when heeled to large angles. Further, due to the drop in dynamic pressure as the water passes around the hull a certain amount of sinkage will occur as a measure of the hydrostatic reaction. Besides the effect on form drag, this dynamic pressure and resulting sinkage also increases the boat's wetted surface and viscous resistance. The magnitude of these effects is small enough that they may be reasonably ignored. In the generation of mathematical models for the remaining forces, emperical data was used that came from experimental tests which included the effects of both pitch and heave.

The present model fixes the pitch angle, $\theta$, and sinkage, s, at zero. The variables are reduced to the following four:

$$( U_b, \psi, \phi, \alpha_r)$$

The remaining major forces acting on a sailing boat are resolved into X, Y, K, and N components and are added together to give the following force equilibriums:

$$\Sigma X_i = X_s + X_h + X_k + X_r = 0 \quad (1)$$

$$\Sigma Y_i = Y_s + Y_k + Y_r = 0 \quad (2)$$

$$\Sigma K_i = K_s + K_h + K_k + K_r = 0 \quad (3)$$

$$\Sigma N_i = N_{sx} + N_{sy} + N_k + N_r = 0 \quad (4)$$

The individual forces are described as follows:

$X_s$ = Sail driving force

$X_h$ = Hull resistance

$X_k$ = Hull and keel induced drag

$X_r$ = Rudder induced drag

$Y_s$ = Sail side force

$Y_k$ = Hull and keel side force

$Y_r$ = Rudder side force

$K_s$ = Sail heeling moment

$K_h$ = Hull righting moment

$K_k$ = Keel heeling moment

$K_r$ = Rudder heeling moment

$N_{sx}$ = Yawing moment from sail driving force

$N_{sy}$ = Yawing moment from sail side force

$N_{k}$ = Yawing moment from keel side force

$N_{r}$ = Yawing moment from rudder side force.

Each individual force is defined in later sections as a function of the boat's geometry, a true wind vector and the four variables $U_b$, $\psi$, $\phi$, and $\alpha_r$. The solution of equations 1 through 4 for a given boat geometry and wind condition provides values for boat speed and attitude. From these values the hydrodynamic performance of the specific sailing boat may then be evaluated.

## II. FORCE AND MOMENT MODELS

### 2.1 Hydrodynamic Forces

The hydrodynamic forces acting on a sailing boat may be conveniently divided into four areas for modeling. The four areas are hull forces, keel forces, rudder forces, and hydrostatic forces. Hull forces consist of resistance from wave making, viscous effects, and form drag. Keel forces are made up of lift on the keel and hull, and drag induced by this lift. Rudder forces in the same way consist of lift and induced drag from the rudder. Finally, hydrostatic forces are caused by the change in position of the center of buoyancy in the hull. Each of these areas is presented individually and models are developed for their contribution to the total force equilibrium.

#### 2.1.1 Hull Resistance

The estimation of hull resistance is a problem faced by naval architects in the design of every ocean going vehicle. The difference, in predicting a sailing boat's resistance, is in the determination of the effects changes in attitude have on these calculations. The approach taken is to determine a model for up-right resistance and modify this resistance as necessary to account for changes in the boat's attitude.

Upright Resistance

The technique commonly used for prediction of resistance from tow tank data is based on Froude's Hypothesis. Basically, the hypothesis states that the total upright resistance may be divided into two components. The first is frictional or viscous resistance. Frictional resistance is dependent on Reynold's Number, a non-dimensional parameter defined as:

$$R_n = U_b L/\gamma_{H_2O}$$

The second component is residual resistance. The residual resistance is the combination of drag due to the generation of waves and the effects of eddy making and form drag. The effect of the hull generating waves is a gravitational effect, largely dependent on Froude Number. This non-dimensional coefficient is defined as:

$$F_n = U_b/\sqrt{gL}$$

Though Froude left the separation of the elements of resistance in these two components, form drag and eddy making resistance have little dependence on either Froude or Reynolds Numbers over the velocity ranges encountered by sailing boats. For this reason it is logical to further separate residual resistance into wave resistance and form resistance.

The separate components of upright resistance are assumed independent of each other so that the total resistance of a boat at a given speed may be estimated by superposition of the forces. Total upright resistance is then:

Upright resistance = frictional resistance
+ wave resistance + form resistance.

Each component of upright resistance is examined in detail and mathematical expressions are developed to quantify their magnitude.

Wave Resistance

The mathematical model for wave resistance is based on a generalized form of Michell's Integral. This expression is evaluated for a base hull form and is corrected for parametric deviation from this parent form. This expression is emperically adjusted to give accurate prediction of the towing tank results of Antiope (3).

Michell (7) postulated that wave resistance for thin ships depends upon the computation of pressure changes, $\delta_p$, due to the wave pattern. His expression for this resistance is

$$R_w = \frac{4\rho g}{\pi U_b^2} \int_1^\infty (I^2+J^2) \frac{\lambda}{\sqrt{\lambda^2-1}} d\lambda \qquad 5$$

where

$$I = \int_{-e}^{+e} \int_{0}^{K(x)} \frac{\partial y}{\partial x} e^{-\lambda^2 gz/U_b^2} \cos\left(\frac{\lambda g x}{U_b^2}\right) dx\, dz \qquad 6$$

$$J = \int_{-e}^{e} \int_{0}^{K(x)} \frac{\partial y}{\partial x} e^{-\lambda^2 gz/U_b^2} \sin\left(\frac{\lambda g x}{U_b^2}\right) dx\, dz \qquad 7$$

Another form of these equations was derived by Weiblum (8). A general expression of his result is

$$R_w = \rho g \frac{B^2 H^2}{L} F\left(\frac{L}{T_c}, \text{ form coefficients, } F_n\right) \qquad 8$$

By assuming that the block coefficient, $C_b$, varies very little between yacht forms, equation 8 may be written as:

$$R_w = \frac{L^3}{\rho g} \left[\frac{\Delta}{(L/100)^3}\right]^2 f\left(\frac{L}{T_c}, \text{ form coefficients, } F_n\right) \qquad 9$$

The number of experiments conducted to validate Michell's result is small. Wigley (9) compared model results to theory and observed the interference humps in the resistance curve were overpredicted by theory. Further comparison between vessels of constant draft and varying beam done by Wigley (10), Weinblum (11), and Mumford (12) indicate for slender ships wave resistance is approximately proportional to the square of the beam as estimated by Michell's Integral, but as the beam to length increases dependence of resistance on beam appears to be less than quadratic. It is expected that the

high beam to length ratios encountered in sailing boats will strain the slender ship limits of Michell's Integral.

The basic form of the wave resistance is rewritten as:

$$R_w = \frac{L^3}{\rho g} \left[\frac{\Delta}{(L/100)^3}\right]^n f(L/T_c, \text{ form coefficients, } F_n) \qquad 10$$

where n is between one and two. The actual value is determined by emperical data discussed in the following sections.

The identification of the most important parameters affecting wave resistance is required. Todd (13) did a regression analysis of over two hundred destroyers and found the following coefficients had the highest correlation between the speed length ratios of 0.8 and 1.25.

$$(\nabla/(L/100)^3,\ C_p,\ LCB,\ L/T_c,\ F_n)$$

For geometrically similar boats we know directly from Froude's Hypothesis that the wave resistance scales is the cube of the characteristic length. The general form of Michell's Integral, equation 10, is used for the dependence on displacement to length ratio. By assuming base value for prismatic coefficient, $C_{po}$; longitudinal position of the center of buoyancy, $LCB_o$; and length to draft ratio, $L/T_{co}$; an expression for the wave resistance of a parent form may be written:

$$R_{wp} = f_1(U_b/\sqrt{L}) \frac{L^3}{\rho g} \left[\frac{\Delta}{(L/100)^3}\right]^n \qquad 11$$

at $C_{po}$, $LCB_o$, and $L/T_{co}$.

To predict the wave resistance of a sailing boat, the resistance of the parent boat is adjusted by correction factors based on the boat's geometric deviation from the parent. The wave resistance equation is

$$R_w = R_{wp} \text{ (1 + } C_p \text{ correction factor + LCB correction factor + } L/T_c \text{ correction factor)} \qquad 12$$

Each component of this equation is defined and discussed in the following sections.

Characteristic Length - L

The characteristic hydrodynamic length or "effective length" of a sailing boat is difficult to quantify. This has been a difficulty in the maintenance of all offshore rating rules as demonstrated by the extremes to which designers have gone to make rated length look shorter than the boat's actual hydrodynamic length. For the purposes of this model, L is determined to be the load water line, LWL. This creates little difficulty when examining the comparitive performance of similar forms, but subjective adjustment would be required

when comparing plumb bow, transom stern boats to long ended boats with shallow buttocks and entrance profiles. To some extent the latter might increase in length with Froude Number as the boat will be supported more by her overhangs.

Parent Froude Number Dependence - $f_1(U_b/\sqrt{L})$

The speed length ratio, $U_b/\sqrt{L}$, was adopted instead of the dimensionally correct variable $F_n = U_b/\sqrt{gL}$ due to the common usage and the comfortable feel most yacht designers have with speed length ratio. The function, $f_1(U_b/\sqrt{L})$ adjusts the wave resistance equation to accurately predict the resistance of the yacht Antiope. The function was determined by inputting Antiope's geometry into the model and selecting $f_1(U_b/\sqrt{L})$ to insure proper correlation with the full scale towing test results reported in (3) and (14). Values of the function were established at each data point given in (14) and a spline cubic curve was fitted to give the curve in Figure 3 for n = 2.0.

Displacement to Length Factor - $[\Delta/(L/100)^3]^n$

The high beam to length ratios, B/L, encountered in sailing boats requires that the exponent, n, be determined from emperical data. Unfortunately, the data base from tests of actual sailing boats is small. The scale effects pointed out in reference (15) precludes the use of results from towing tests of small scale yacht forms.

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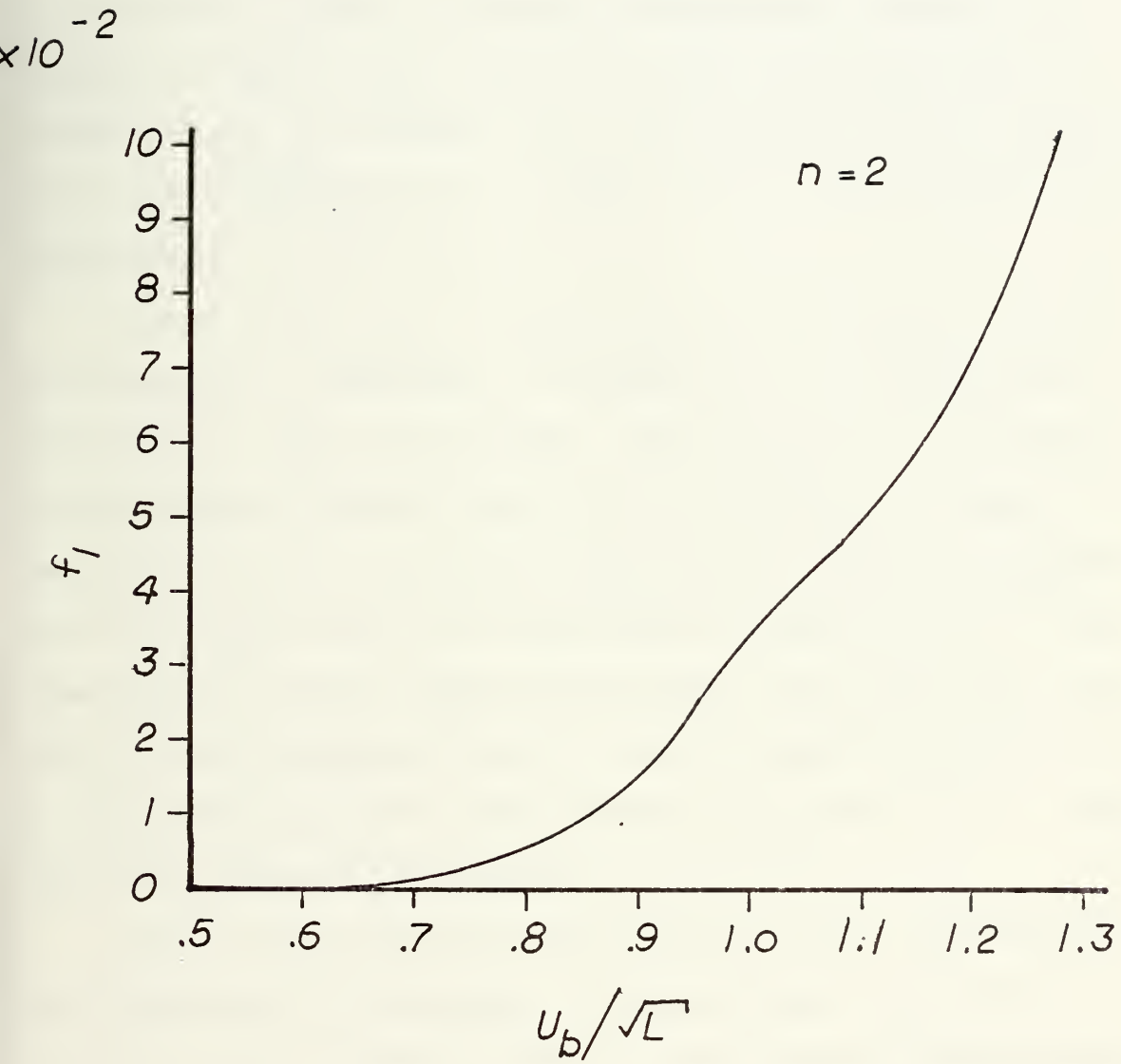



Figure 3

Parent Froude Number Dependence

Examination of Taylor Standard Series (16) at prismatic coefficients typical in yacht design indicate that a value of n between 1.8 and 2.0 appears reasonable. Though the prismatic coefficients, length to draft and displacement to length ratios in reference (16) are typical of sailing boats, the block coefficient, $C_b$, is high and not characteristic of yacht forms.

Figure 4 is a plot of two curves predicting the wave resistance of a Standfast 43 sailboat by the mathematical model with n equal one and two. Also plotted are the data points from the towing tests of a one sixth scale model conducted by M.I.T. and Delft University. Figure 5 compares the full scale test (15) of the one ton yacht Bullet to two theoretical curves. The form drag data from both yachts was taken as the residuary drag at a speed length ratio equal to 0.4 and subtracted from the residuary resistance versus speed curve to obtain the wave drag.

Two is maintained as the value of n in the computerized model appended to this paper. Though comparisons made in Figures 4 and 5 indicate that n = 2 may slightly overestimate the effect displacement to length ratio has on wave making resistance, the limited sample size available for correlation does not justify adjustment from the theoretical value.

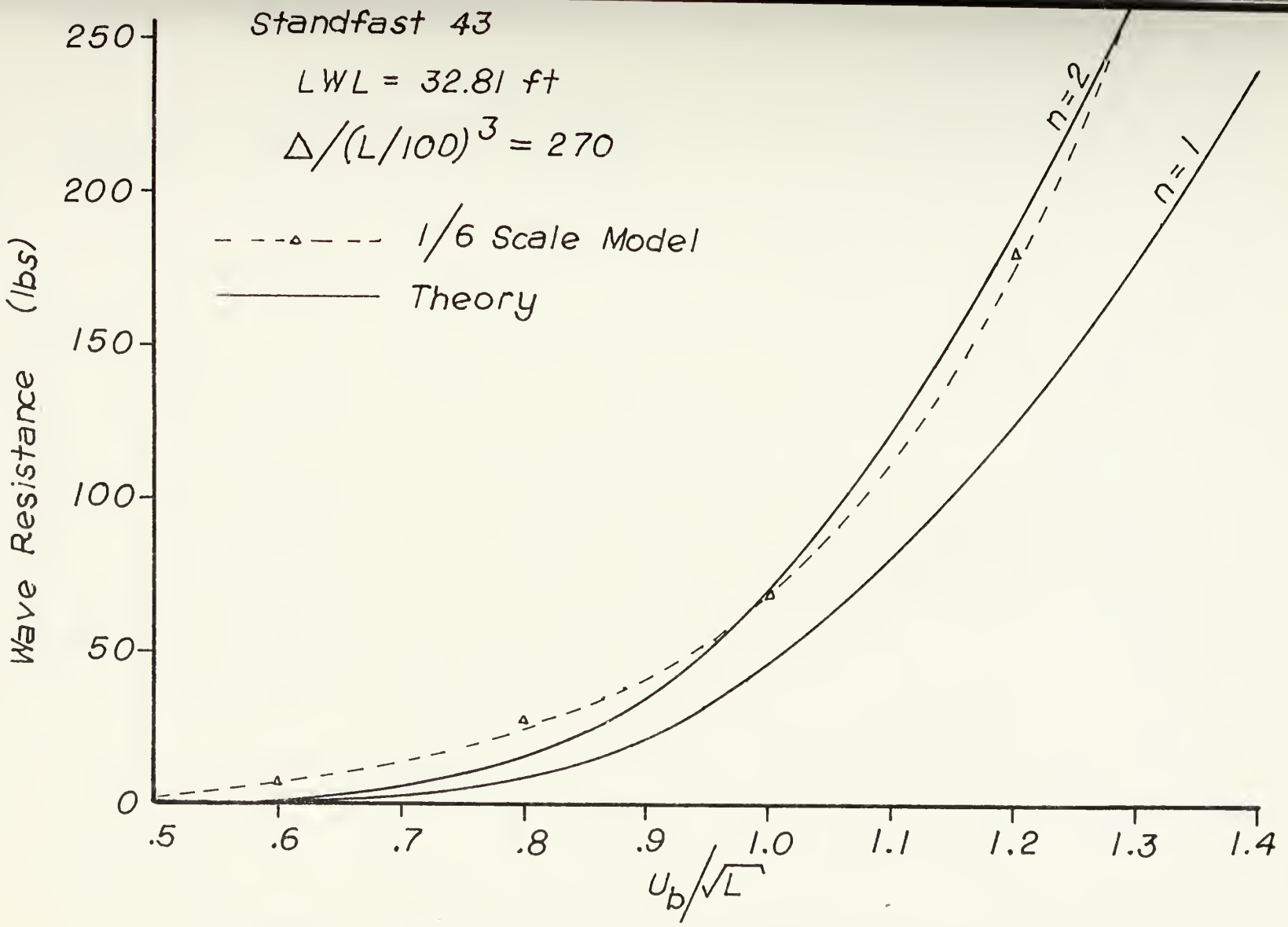



Figure 4 – Standfast 43 Wave Resistance

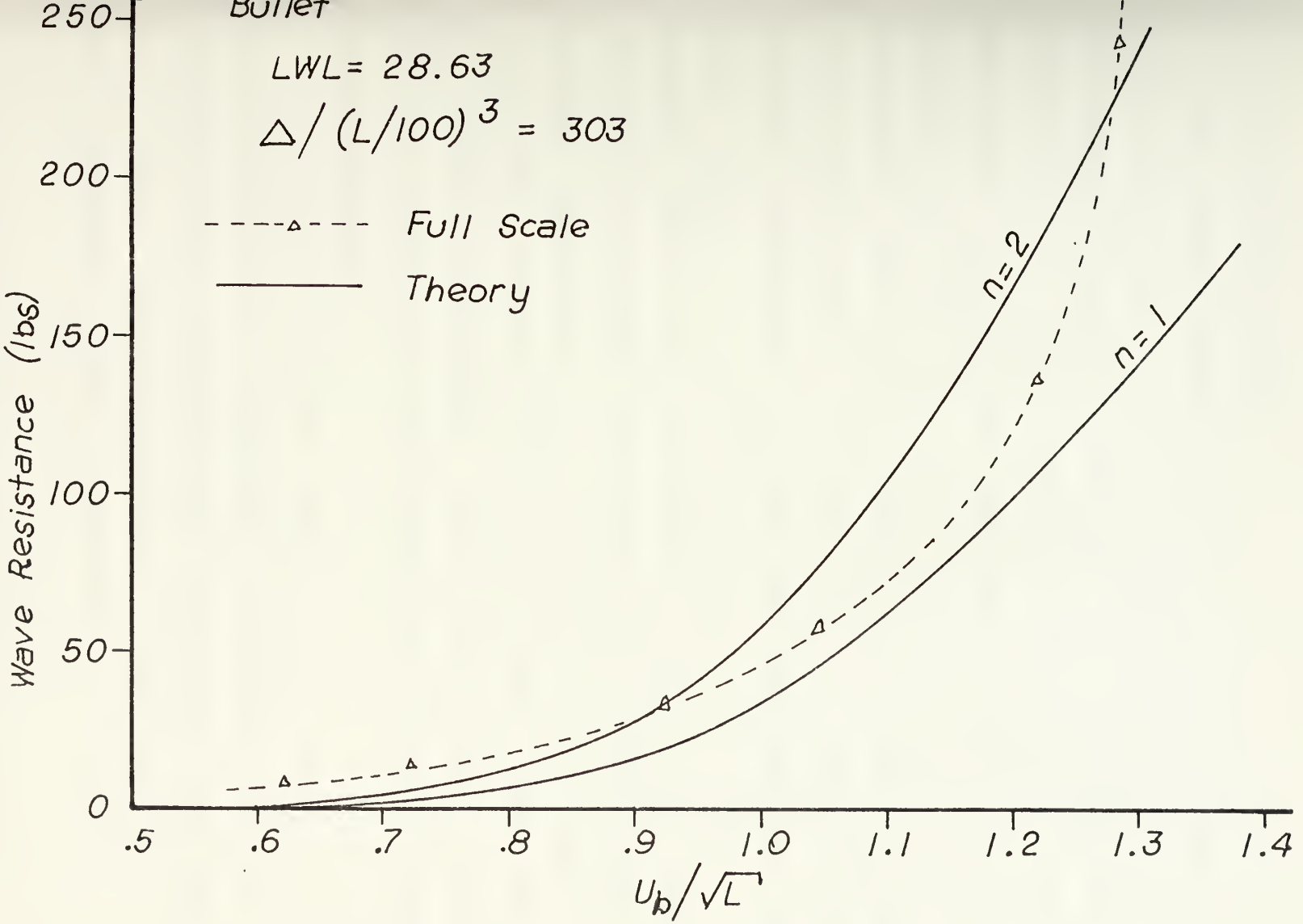



Figure 5 - Bullet Wave Resistance

## $C_p$ Correction Factor

The prismatic correction factor corrects the magnitude of the sailing boat's wave resistance for deviations away from the base prismatic coefficient, $C_{po}$. The base prismatic coefficient, $C_{po}$, was selected to be the optimum prismatic coefficient, $C_{popt}$, for each speed length ratio. Taylor's Standard Series (16) data are the only tests available of large models where prismatic coefficient was systematically varied. Examination of these data reveals a definite optimum prismatic coefficient, $C_{popt}$, for each tabulated speed length ratio. Figure 6 is a spline cubic fit of this optimum prismatic taken at the displacement to length ratio equal to 250 and plotted versus speed length ratio. This optimum prismatic coefficient, $C_{popt}$, as a function of the speed length ratio is selected as the base prismatic coefficient, $C_{po}$, of the parent equation. This is done so that deviations from this optimum will always result in an increase in wave making resistance.

From Taylor's Standard Series, reference (16), the percentage increase in resistance for deviation from the optimum prismatic coefficient was tabulated for each speed length ratio. From this emperical data the expression for the $C_p$ correction factor is generated.

$$C_p \text{ correction factor} = f_2(U_b/\sqrt{L})\,|100(C_{popt}-C_p)|^{1.7} \qquad 13$$

Figure 7 is a plot of the spline cubic fit of the correction factor's dependence on speed length ratio, $f_2(U_b/\sqrt{L})$. A reasonable definition for the sailing boat's prismatic coefficient, $C_p$, must be established to insure quantitative agreement between the Taylor Series, reference (16), forms and the yacht forms. A method for weighting the volume and sectional area of the keel in the calculation of the longitudinal prismatic coefficient is developed. Equations 6 and 7 of Michell's Integral indicate that displacement should be weighted exponentially in the vertical direction by

$$e^{-\lambda^2 gz/U_b^2}.$$

There are two common practices in calculating the $C_p$ of a sailing boat. The first is to include the total volume and sectional area of the keel into the calculation. The inclusion of all the deeply placed sectional area of the keel would overestimate its effect on the wave making resistance when compared to the keel's actual effect on the wave train. On the other hand, the second method is to treat the keel as an appendage and calculate only a fairbody or canoe prismatic. This ignores the keel's displacement effect altogether. Typical values of $C_p$ for the same yacht calculated both ways are 0.52 and 0.58 with and without the keel included respectively. If the Taylor Series, reference (16), optimum is to be used, the corresponding prismatic coefficient would be somewhere in between these two values.

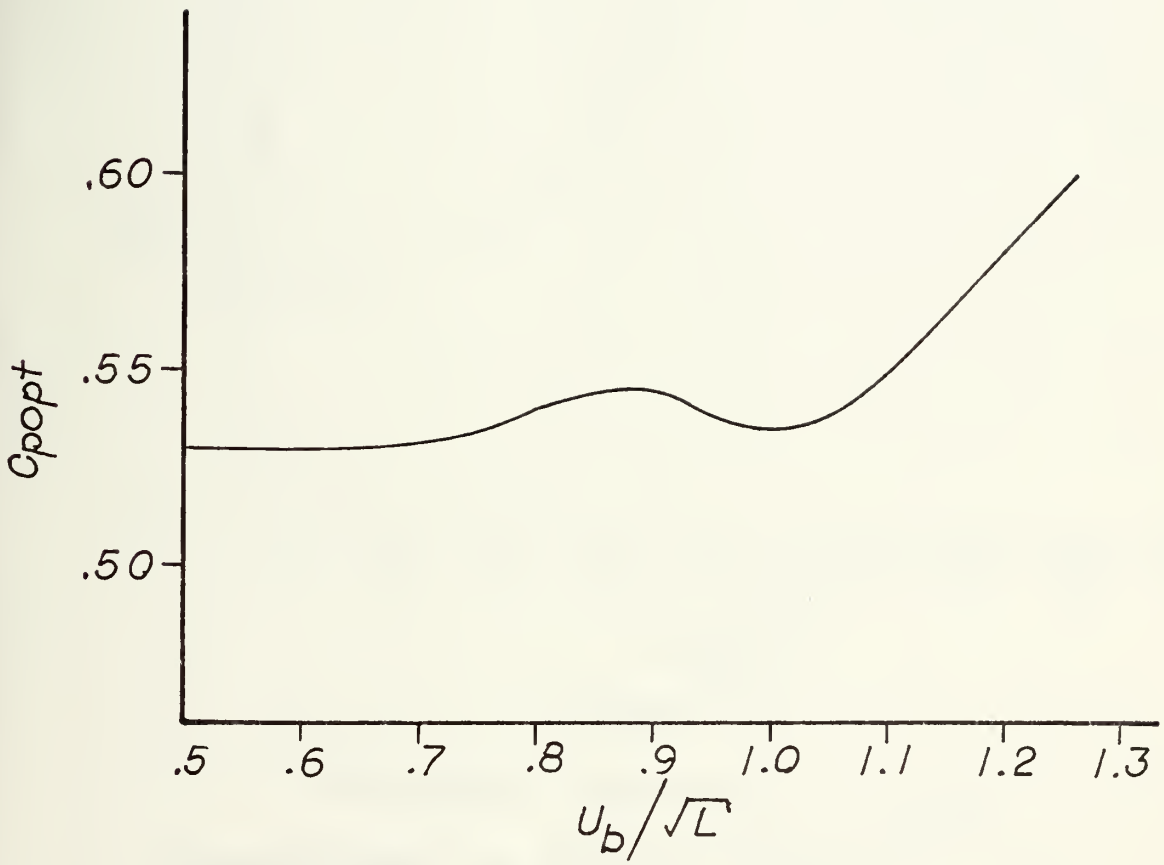



Figure 6 - Optimum Prismatic Coefficient

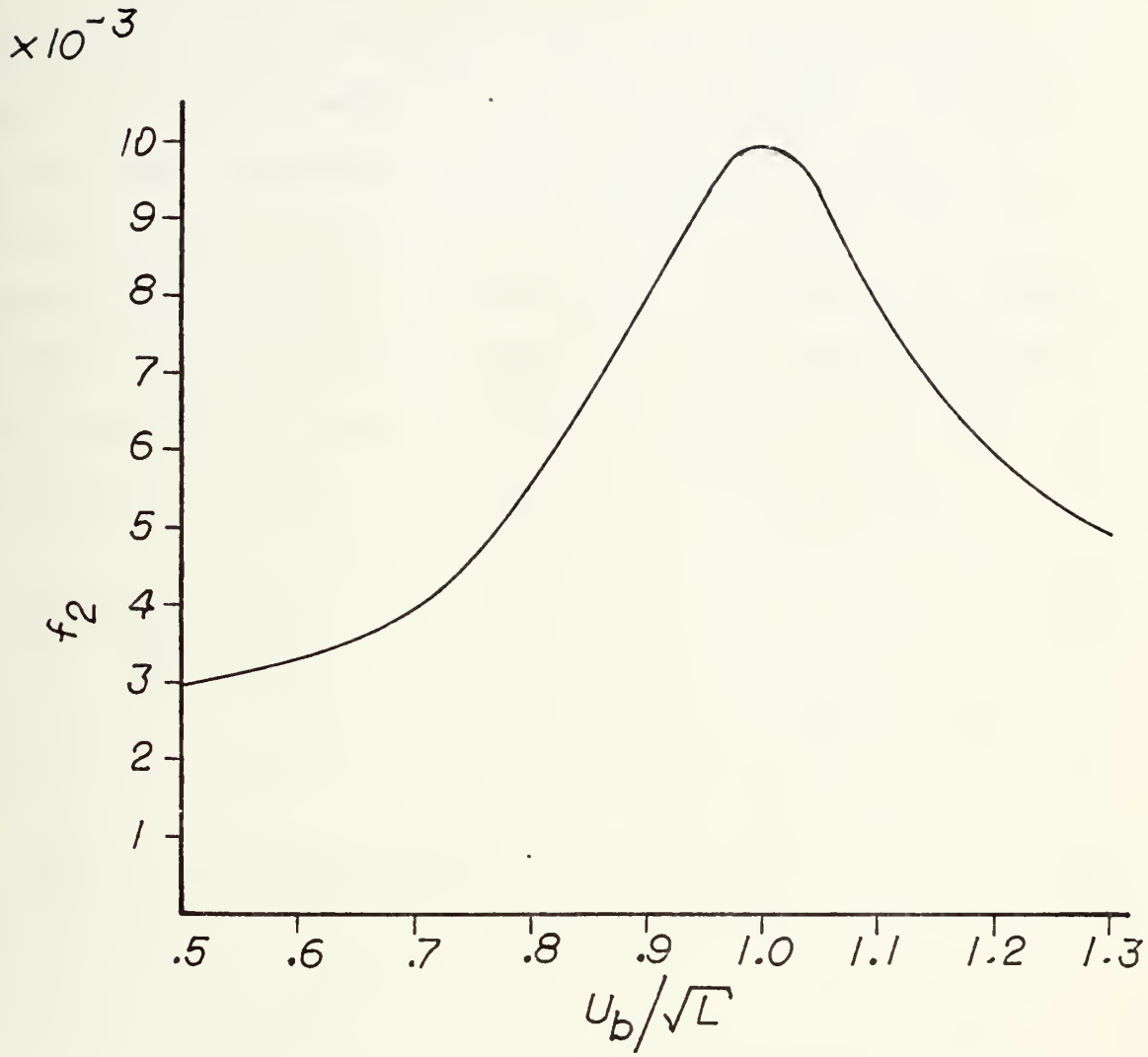



Figure 7

Prismatic Correction Factor

Dependence on Froude Number, $f_2$

One would expect the volume of the keel to have its largest effect when the sailing boat is sitting on a wave of approximately the same length as the waterline. At this point the wave trough would bring the keel the closest to the free surface. An estimation of keel's proper effect on prismatic coefficient, $C_p$, may be made by weighting the keel's area and volume by $e^{-1/F_{nz}^2}$ where $F_{nz}$ is the vertical Froude number evaluated at speed length ratio equal to one. The longitudinal prismatic coefficient, $C_p$, is defined as:

$$C_p = \frac{\nabla_c + \nabla_k^*}{(A_m + A_k^*)\ L} \qquad 14$$

where

$$\nabla_k^* = \nabla_k\ e^{-32.2d/(1.689L)^2} \qquad 15$$

and

$$A_k^* = A_k\ e^{-32.2d/(1.689L)^2} \qquad 16$$

$\nabla_c$ and $\nabla_k$ are the displaced volume of the canoe body and keel respectively. $A_m$ and $A_k$ are the maximum cross sectional area of the canoe body and the cross sectional area of the keel at that station respectively. The depth, d, is measured from the static waterline to the center of the keel's displaced volume.

## $L/T_c$ Correction Factor

Taylor Standard Series (16) tabulates data on ships at length to draft ratios equal to eight and sixteen. Taylor Series (16) asserted that linear interpolation between these ratios was adequate.

The base length to draft ratio, $L/T_{co}$, of 16 is selected from Taylor Series (16) data and the correction factor is

$$L/T_c \text{ correction factor} = -f_3(U_b/\sqrt{L})(16-L/T_c) \qquad 17$$

where $f_3(U_b/\sqrt{L})$ is a spline cubic fit of the speed length effect as shown by Taylor (16). $f_3(U_b/\sqrt{L})$ is plotted in Figure 8.

The major differences between the ships tested for Taylor's Standard Series (16) and yacht forms are in the shape of the sections. The Taylor form typically has a maximum section coefficient, $C_m$, of 0.98 while sailing boats range between 0.60 and 0.70. As a result, the vertical distribution of volume between the two forms differ to a large extent. It is not completely accurate to assume that vertical shifts in the volumetric distribution of the two forms will have a similar effect on wave making resistance. The model utilizes the best data available to date, but the need exists for a large scale yacht series examining just such a systematic parameter variation.

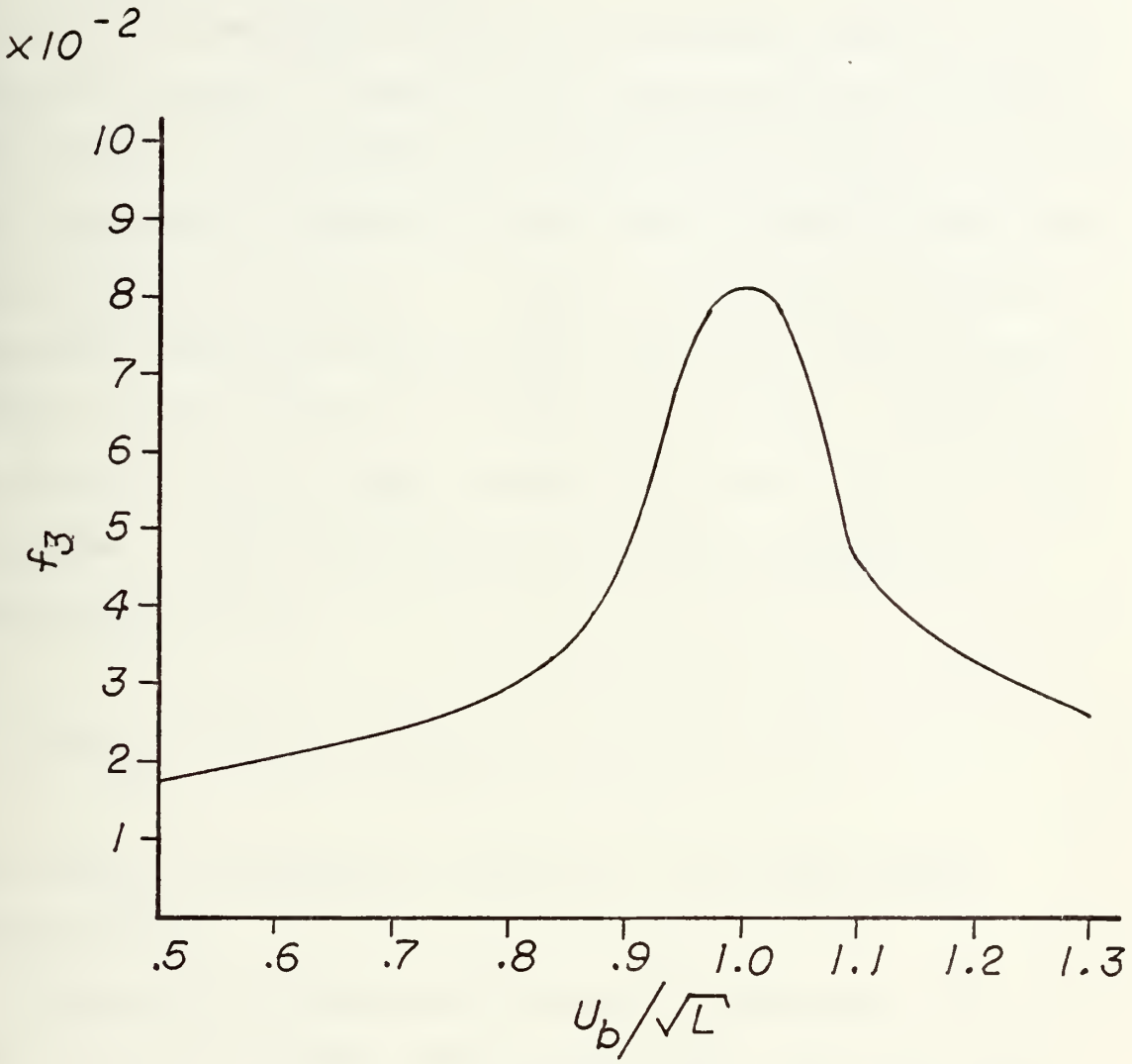



Figure 8

$L/T_c$ Correction Factor

Dependence on Froude Number

LCB Correction Factor

In the same manner as the $C_p$ correction factor, the LCB correction factor is based on the actual LCB and an optimum LCB position. A summation of recommended optimum LCB positions as a function of block coefficient and prismatic coefficient was presented by Todd (17). There is reasonable agreement among the recommended curves with less than 1.5% variation between extreme curves in the area of interest. Comparing the LCB curves with common practice in yacht design a curve attributed to Professor Troost in (17) was adopted. In modified form it is

$$LCB_{opt} = 62.5 - 17.5C_p \qquad 18$$

where $LCB_{opt}$ is measured in percent L from the forward perpendicular.

Examination of the major series in references (17), (19), and (20) which consider LCB as a variable, none adequately cover the region in which sailing boats fall. In all cases, these series cover block coefficients higher than typical yachts. Certain trends may be determined though:

1. As with the previous factors, there is a peak effect at speed length ratio equal to one.
2. As block coefficient decreases, the penalty for non-optimum center of buoyancy position also decreases.

The above series, therefore, place an upper bound on the expected penalty.

Todd (17) indicates for Series 60 that a one percent change from the optimum LCB position will increase wave making resistance by approximately one percent. Beyond a one percent change the penalty increases sharply.

The assumed factor is

$$\text{LCB correction factor} = \sin(90U_b/\sqrt{L})\,|62.5-17.5C_p-\text{LCB}|^3/100 \qquad 19$$

Frictional Resistance

The mathematical model for frictional resistance is derived from procedures adopted by the Eighth International Towing Tank Conference (21), ITTC in 1957. Traditionally frictional or viscous resistance is defined as:

$$R_f = C_f\, 1/2\rho\, S_w\, U_b^2$$

$S_w$ is the wetted surface of the sailing boat and $C_f$ is the coefficient of frictional resistance.

The ITTC defined the coefficient of frictional resistance as:

$$C_f = 0.075/(\log_{10} R_n - 2)^2$$

where Reynold's Number, $R_n$, is the only parameter affecting this coefficient. Again, Reynold's Number is defined as:

$$R_n = U_b L/\gamma_{H_2O}$$

where $\gamma_{H_2O}$ is the kinematic viscosity of water.

A suitable definition of the Reynold's Number characteristic length, L, must be established. The ITTC adopted the use of the load waterline length, LWL, as the characteristic length. This makes sense for ships with rectangular profiles, but sailing boats characteristically have cut away profiles and keel and rudder chords which have little dependence on the length of the waterline. Davidson (22) realized this problem and adopted seventy percent of the waterline length as the characteristic length. The adoption of a constant length lacks sensitivity to the effects differing profiles have on the characteristic length. To make the mathematical model sensitive to these variations, the total wetted surface of the yacht is divided into three areas, each with its own characteristic length.

The three areas are the sailing boat's canoe body, the keel and the rudder. The load waterline length, LWL, is the characteristic length of the canoe body while the mean chord of the keel, $\bar{c}_k$, and rudder, $\bar{c}_r$, are the characteristic lengths of the keel and rudder respectively.

The coefficient of friction for each area is calculated using equation 21. The total frictional resistance is the sum of the resistances of each area and is written as:

$$R_f = 1/2\rho_{H_2O} U_b^2 (C_{ffb}S_{fb}+C_{fk}S_k+C_{fr}S_r)$$

The above coefficients and wetted surfaces are defined as:

$C_{ffb}$ = fairbody coefficient of friction

$S_{fb}$ = fairbody wetted surface

$C_{fk}$ = keel coefficient of friction

$S_k$ = keel wetted surface

$C_{fr}$ = rudder coefficient of friction

$S_r$ = rudder wetted surface

The ITTC equation for the coefficient of friction is an emperical formulation which historically has either slightly overpredicted or underpredicted frictional resistance for certain forms. From previous experience with a given form, a factor may be added to give satisfactory correlation with full scale results. When equation 22 is applied to Antiope (3), the correlation factor is unnecessary. This would indicate that the yacht Antiope has no form resistance or skin roughness. This is unfounded and indicates that the ITTC formulation overpredicts the frictional resistance of the yacht Antiope by the approximate magnitude of its own form resistance. This effect is discussed further in the next section.

Form Resistance

Form resistance is a combination of effects which show little dependence on Froude Number and Reynold's Number in the speed range seen by sailing boats. Form resistance, $R_{fm}$, is defined as:

$$R_{fm} = C_{fm}\ 1/2\rho S_{fb} U_b^2 \qquad 24$$

The form resistance coefficient, $C_{fm}$, is a constant with speed and depends only on the boat's geometry, surface roughness, and appendages. Form resistance is made up of eddy making resistance, roughness effects, and pressure drag due to separation.

The form resistance of a yacht may constitute ten percent of the boat's total resistance at low speed and decreases to less than two percent as the effects of wave making resistance increase. Kirkman and Pedrick (15) discuss the difficulty in modeling form resistance from analytic and emperical sources. The scale effects from small scale model tests have made the measurement of this component difficult. Further, the selection of the ITTC friction coefficient formulation includes an arbitrary amount of form resistance which is not quantifiable. The use of this line in predicting Antiope (3) resistance did not require the use of a form drag coefficient to provide correlation.

The present mathematical model does not parameterize the form resistance coefficient but allows the user to input a value to improve correlation with known results. The inclusion of this coefficient allows future parameterization as techniques for its prediction become available.

Hull Force Formulation

The total upright resistance, $R_u$, is the superposition of wave resistance, frictional resistance, and form resistance as defined by equations 12, 23, and 24.

$$R_u = R_w + R_f + R_{fm} \qquad 25$$

The change in hull resistance with heel and leeway angle must be considered. For small angles of leeway, $\psi$, the change in resistance is considered an effect of lift and is modeled in the section on keel forces, 2.1.2.

In the absence of lift, the change in upright resistance due to heel, $\phi$, is caused by a number of effects. As the sailing boat heels, one would expect not only changes in the boat's symetrical lines, but also her form. Depending on the yacht form, the effective sailing length may also increase or decrease. Further, as the boat heels, the keel moves closer to the free surface and in effect decreases the effective prismatic coefficient and increases resistance.

Examination of a number of towing tank tests conducted at M.I.T. show that the increase in resistance at zero side force varies depending on the design. This variation ranged from an increase in resistance from a minimum of five percent to a maximum of twenty-five percent at twenty-five degrees heel. The majority of the well-designed models show an increase of approximately ten percent at twenty-five degrees heel. Because of the lack of test date available which systematically investigates heel effects, the increase in resistance with heel is limited to an estimate of what good design practice has demonstrated. This effect is emperically modeled by dividing the upright resistance by the cosine of the heel angle.

The expression for the hull forces in the $X_o$ direction is written as:

$$X_h = R_u/\cos \phi \qquad 26$$

where $R_u$ is the upright resistance defined by equation 25.

2.1.2 Keel Forces

The mathematical models for lift forces acting on the hull and keel are derived from slender body theory as applied to fish-like bodies in references 23, 24, and 25. Expressions are defined for the hull and keel side force, $Y_k$; induced drag, $X_k$; yawing moment, $N_k$; and the heeling moment, $K_k$.

Hull and Keel Side Force

Letcher (3) investigated the possibility of utilizing available theories for predicting a sailing boat's side force. He compared lifting line theory, slender body theory and an adoption of slender-body theory for fish-like bodies to the towing tank test results of the yacht Antiope. The theory presented by Newman and Wu (24) for fish-like bodies demonstrated excellent correlation to Letcher's (3) regression analysis of Antiope's test data. An adaptation of this theory is utilized for modeling the hydrodynamic lifting forces acting on the keel and hull.

The side force acting on the keel and hull is defined as:

$$Y_k = -C_{Y\psi}\cos^2\phi(1/2\rho_{H_2O}\ L^2U_b^2\psi) \qquad 27$$

where the $\cos^2\phi$ term was found by Letcher (3) to satisfactorily quantify the effect heel has on the side force coefficient, $C_Y$, for the yacht Antiope. L is the load waterline length.

A mathematical model for side force coefficient is derived from slender-body theory as applied to fish-like forms. Milgram (23) gives an expression for the local lift, L(x), on a slender-body as:

$$L(x) = \frac{\pi}{2}\rho_{H_2O}\ \frac{d}{dx}\ [b^2(x)]V_bU_b \qquad x_o < x < x_b \qquad 28$$

where b(x) is the local span, $x_o$ is the horizontal position of the maximum span, and $x_b$ is the horizontal distance from the maximum span to the forward perpendicular. Figure 9 shows Antiope's profile with the locations of $x_o$ and $x_b$. $V_b$ is the component of velocity y direction.

The total side force predicted by slender-body theory is

$$Y_{sb} = \int_{x_o}^{x_b} L(x)\, dx \qquad 29$$

For the numerical computation of the slender-body side force, the yacht's profile is tabulated at the five points shown in Figure 9 and the profile, b(x), is approximated by straight lines between these points. Equation 29 is evaluated numerically to give the slender-body lift on the hull and keel.

The velocity $V_b$ may be approximated for small leeway angle by the linear expression:

$$V_b = U_b \psi \qquad 30$$

The coefficient of side force, $C_{y\psi sb}$, based on slender-body theory may be written as:

$$C_{y\psi sb} = Y_{sb} / \tfrac{1}{2} \rho_{H_2O} L^2 U_b^2 \psi \qquad 31$$

where L is taken as the waterline length, LWL.

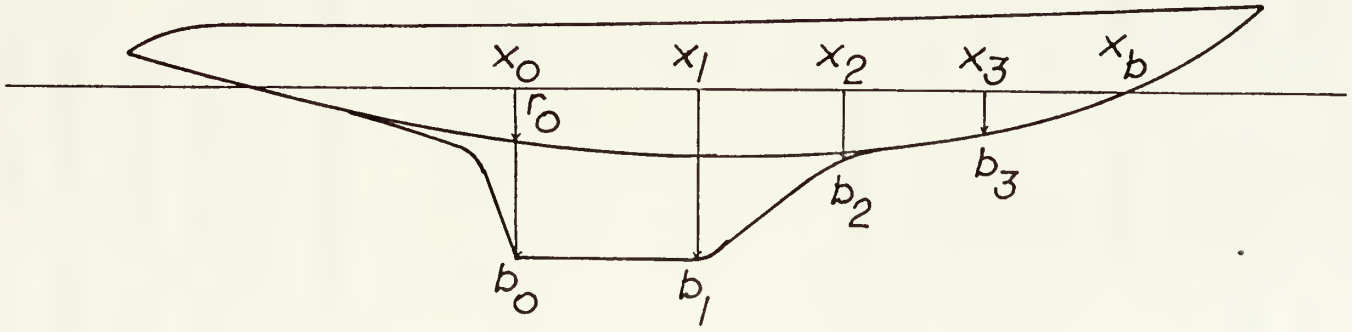



Figure 9 - Antiope Profile

Newman and Wu (24) developed a procedure for determining the effect an axisymetric body of radius $r_o$ has on the slender-body lift. From reference 24, Figure 10 is a plot of $-L/\pi\rho U_b V_b b_o^2$ versus $r_o/b_o$. At $r_o/b_o$ equal to zero, the curve gives the slender-body lift for a given span. As $r_o/b_o$ increases the lift is attenuated by the amount shown in the curve. This curve may be defined as a fair body factor, $f_{fb}$. The curve is entered with the ratio $r_o/b_o$ to obtain the fair body factor. The slender-body coefficient from equation 31 is multiplied by the fair body factor to compute the yacht's side force coefficient. The expression for the side force coefficient is

$$C_{y\psi} = C_{y\psi sb}(f_{fb}) \qquad 32$$

The radius, $r_o$, is measured as the draft of the canoe body at the maximum draft measurement, $b_o$. These two measurements are depicted in Figure 9.

This technique for the solution of side force correlates well with the full scale tests of the yacht Antiope (3). Antiope has a moderately long keel compared to modern sailboats with their fin keels. For a given hydrodynamic span, as the chord of a long keel decreases, the lift remains essentially unchanged, but at a certain point a further decrease in the keel's chord can no longer support the spanwise elliptic

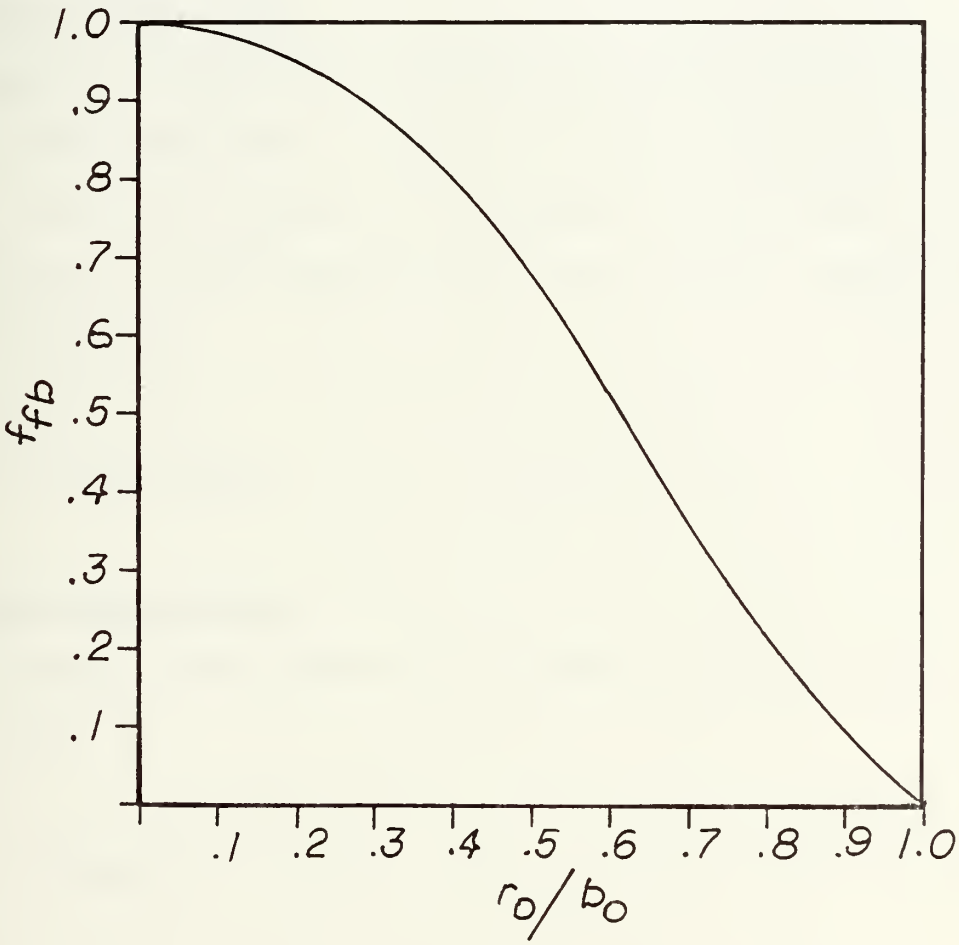



Figure 10 - Lift Attenuation

loading assumed by slender-body theory. The present model is not sensitive to this effect, and though the model is adequate for modeling changes in draft, it should not be utilized to optimize keel area.

Keel Induced Drag

Newman in reference 25 develops the equation for induced drag on fish-like forms. Figure 11 is from reference 25 and gives a curve for $(\psi Y_k/D_i)$ as a function of the ratio $r_o/b_o$. By generating a spline cubic fit to this curve, induced drag, $X_k$, is defined as:

$$X_k = Y_k\psi/(\psi Y_k/D_i) \qquad 33$$

Keel Yawing Moment

The yawing moment due to the side force on the keel is defined as:

$$N_k = x_{cpk}Y_k \qquad 34$$

The center of effort of the hydrodynamic side force, $x_{cpk}$, is determined from slender-body theory. Milgram (23) gives the yawing moment about $x_o$ in Figure 9 as:

$$N_{sb} = \int_{x_o}^{x_b} xL(x)dx \qquad 35$$

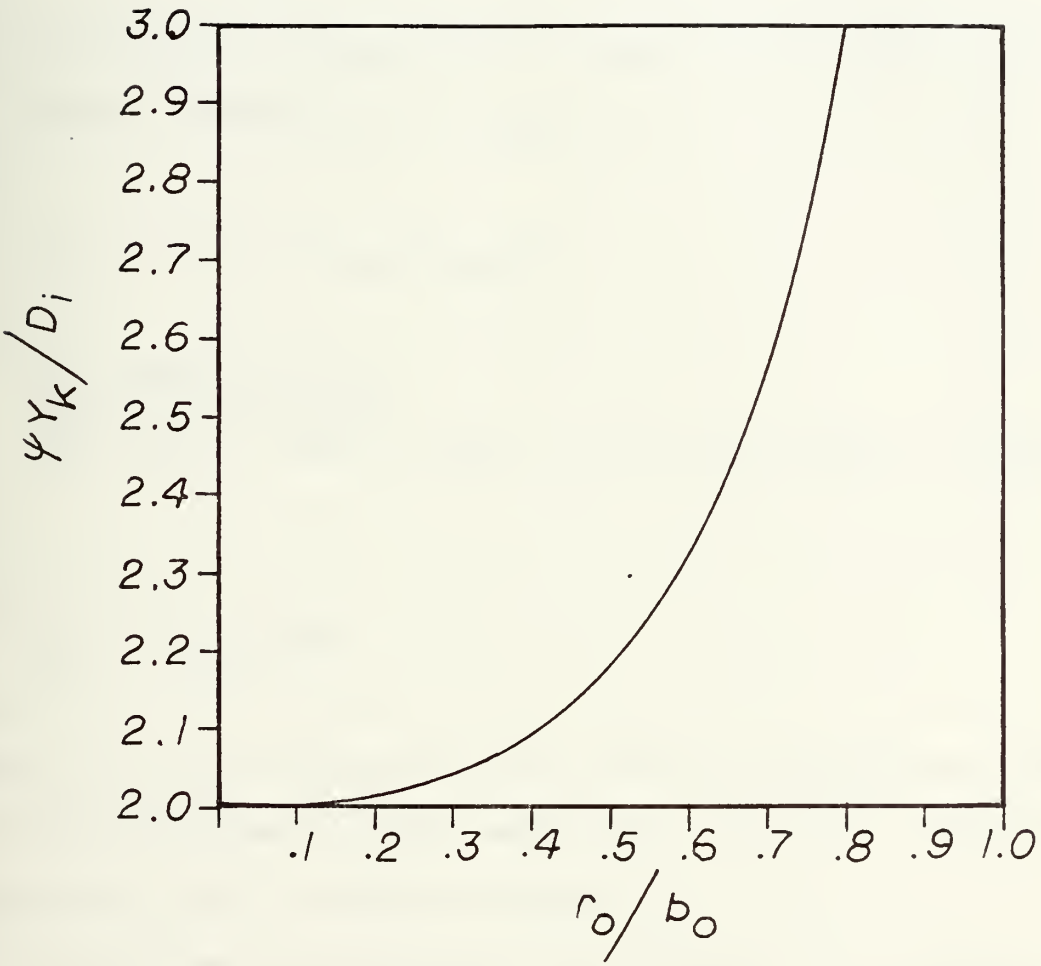



Figure 11 - Induced Drag

where L(x) is defined by equation 28. Hence, the non-dimensional coefficient for yawing moment can be written as:

$$C_{n\psi sb} = N_{sb}/\tfrac{1}{2}\rho H_2O\ L^3\ U_b^2\psi \qquad 36$$

and the distance to the center of hydrodynamic effort from the forward perpendicular, $x_{cpk}$, as:

$$x_{cpk} = (1.0 - C_{n\psi sb}/C_{y\psi sb})L \qquad 37$$

Keel Heeling Moment

The heeling moment caused by the side force on the keel is

$$K_k = -Y_k z_{cpk} \cos\psi \qquad 38$$

where $z_{cpk}$ is the distance to the vertical hydrodynamic center of effort measured from the waterline. Since the leeway angle, $\psi$, is small, $\cos\psi$ is taken as unity.

Slender-body theory tends to overpredict the location of the vertical center of effort when compared to towing tank data. Letcher (3) reduced Antiope data for the location of the center of effort and deduced that the vertical center of effort was approximately 1.5 feet below the waterline. From this a reasonable estimate for the vertical center of effort, $z_{cpk}$, is made.

$$z_{cpk} = 0.33b_o \qquad 39$$

where $b_o$ is the maximum draft as defined in Figure 9.

2.1.3 Rudder Forces

Mathematical models for the forces acting on the rudder are derived from the emperical equation for spade rudders presented in reference (26). Expressions are defined for the rudder side force, $Y_r$; rudder drag, $X_r$; rudder yawing moment, $N_r$; and rudder heeling moment, $K_r$.

Rudder Side Force

Whicker and Fehlmer (26) conducted a series of wind tunnel tests on low and medium aspect ratio spade rudders and provided emperical equations which accurately model the forces and moments acting on a large family of spade rudders. The equations are sensitive to aspect ratio, $a_r$, sweep angle, $\Omega$, and taper ratio, $t_r$.

The modeling of rudder forces in relation to a sailing boat are complicated by the effect of the downwash from the keel. By treating the keel as a low aspect ratio lifting surface, the downwash can be assumed to deflect the flow along the centerline of the boat. Although the keel will actually deflect the flow slightly less than this, the approximation is considered reasonable. The model therefore assumes that the angle of attack on the rudder and the rudder's deflection from the boat's centerline, $\alpha_r$, are identical. The effect of heel on rudder performance is considered negligable.

Figure 12 is a drawing of a spade rudder including the measurements and nomenclature used in determining the rudder's performance. The geometrical ratios required by the theory are derived from these measurements. The hydrodynamic aspect ratio, $a_r$, is defined as:

$$a_r = 2b_r/\bar{c}_r \tag{40}$$

where $b_r$ is the geometric span and $\bar{c}_r$ is the mean chord as defined in Figure 12. Taper ratio, $t_r$, is defined as:

$$t_r = c_{rt}/c_{rr} \tag{41}$$

where $c_{rt}$ is the rudder tip chord, and $c_{rr}$ is the rudder root chord as defined in Figure 12.

Whicker (26) defines the coefficient of lift as:

$$C_{lr} = \left(\frac{\partial C_L}{\partial \alpha_r}\right)\alpha_r + \frac{C_{dc}}{a_r}\left(\frac{\alpha_r}{51.3}\right)^2 \tag{42}$$

where $C_{dc}$ is the cross flow drag coefficient, and the rudder angle, $\alpha_r$ is measured in degrees.

An emperical expression from reference (27) for the cross flow drag coefficient, $C_{dc}$, for rudders with faired tips is

$$C_{dc} = 0.08 + 0.72t_r \tag{43}$$

direction to starboard. The z axis desends orthogonally to the x-y plane in the direction of the keel.

The angular differences between the two coordinate systems describe the attitude of the boat as it moves through the water. The positive direction for these angles are also presented in Figure 2. Their direction was selected to provide positive values when the boat is in equilibrium under normal sailing conditions with a weather helm. The order in which these angles are taken is important to the final attitude. The boat is first rotated about the $Z_o$ axis through the angle $\psi$. The angle $\psi$ is identical to the boat's leeway angle. The boat is then rotated about the X axis, an angle $\phi$, which is the boat's heel angle. The boat is then rotated about the $Y_o$ axis, an angle $\theta$. $\theta$ is the angle by which the boat pitches down at the bow and is also the angle of the axis about which the boat heels. Finally the angle $\alpha_R$ is the angle the rudder is deflected from the boat's centerline.

A sailing boat responding to the forces acting upon it and conforming hydrostatically to deformations in the free surface would heave in the positive $Z_o$ direction an amount s.

The selection of these coordinate systems allows the modeling of forces in either coordinate system. When modeling velocity related forces, such as wave drag and lift, the coordinate system fixed in the water is more attractive computationally. On the other hand, hydrostatic forces are more easily computed in the coordinate system fixed in the

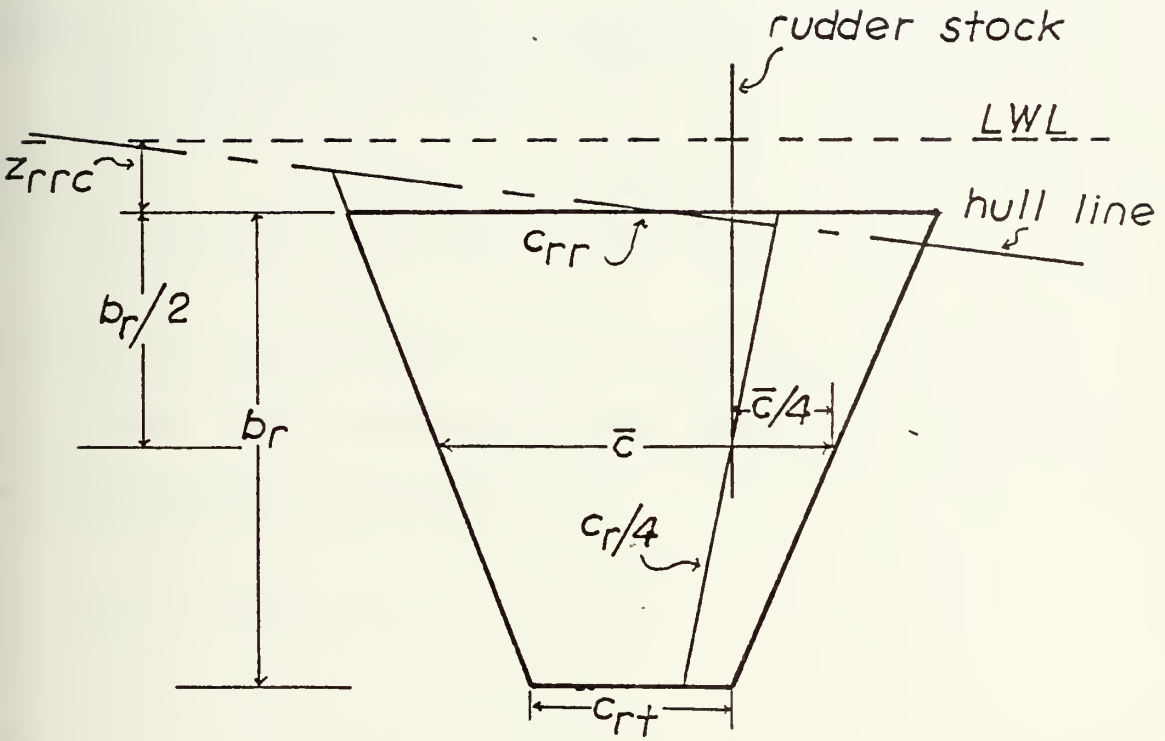



Figure 12 - Rudder Geometry

$\partial C_L/\partial \alpha_r$ is defined (26) as:

$$\frac{\partial C_L}{\partial \alpha_r} = \frac{(0.9)(2\pi)\ a_r}{(57.3)\left[\cos\Omega\sqrt{\frac{a_r^2}{\cos^4\Omega} + 4} + 1.8\right]} \qquad 44$$

where $\Omega$ is the sweep angle as defined in Figure 12.

The rudder's drag coefficient, $C_{dr}$, is defined as:

$$C_{dr} = C_{do} + C_{lr}^2/\pi a_r e + 0.0166\ C_{lr}^2 \qquad 45$$

where e is an efficiency factor established at 0.9 (26). $C_{do}$ is the rudder section form drag coefficient and if not specified $C_{do}$ is assumed to be

$$C_{do} = 0.0065 \qquad 46$$

The $0.0166\ C_{lr}^2$ term is an emperical increase in functional resistance due to lift recommended by Kerwin (28). This form drag coefficient is from the NACA 0015 section (26). The interference drag caused by the interaction between the fair-body boundary layer and the rudder root chord is not accounted for in the present model and should be examined in future studies.

By transforming the rudder's lift and drag coefficients from the boat's coordinate system into the system located on the horizontal surface of the water, the rudder side force

coefficient is written as:

$$C_{yr} = (C_{lr}\cos\psi - C_{dr}\sin\psi)\cos\phi \qquad 47$$

Hence, the rudder side force is

$$Y_r = -C_{yr}(\tfrac{1}{2}\rho_{H_2O} A_r U_b^2) \qquad 48$$

where $A_r$ is the rudder's plan form area. The plan form area is defined as:

$$A_r = b_r \bar{c}_r \qquad 49$$

Rudder Drag

The rudder drag coefficient is

$$C_{xr} = C_{lr}\sin\psi + C_{dr}\cos\psi \qquad 50$$

where $C_{lr}$ and $C_{dr}$ are defined by equations 42 and 45 respectively.

The equation for rudder drag, $X_r$, is

$$X_r = -C_{xr}(\tfrac{1}{2}\rho_{H_2O} A_r U_b^2) \qquad 51$$

Rudder Yawing Moment

To determine the yawing moment caused by rudder forces, the location of the center of effort on the rudder, with respect to the rudder stock, is calculated. The rudder stock is assumed to pass through the quarter point on the mean chord as shown in Figure 12.

The moment coefficient about the quarter chord (26) is:

$$C_{m\bar{c}/4} = [0.25 - (\frac{\partial C_m}{\partial C_L})_{C_L=0}] \ (\frac{\partial C_L}{\partial \alpha_r})_{\alpha_r=0} - \frac{1}{2} \frac{C_{dc}}{a_r} (\frac{\alpha_r}{57.3})^2 \qquad 52$$

where

$$(\frac{\partial C_m}{\partial C_L})_{C_l=0} = \frac{1}{2} - \frac{1.11\sqrt{a_r^2+4} + 2}{4(a_r+2)} \qquad 53$$

The normal force coefficient, $C_n$, is

$$C_n = C_{lr}\cos\alpha_r + C_{dr}\cos\alpha_r \qquad 54$$

The location of the center of effort with respect to the quarter point on the mean chord is

$$x_{p\bar{c}/4} = - \frac{C_{m\bar{c}/4} \ \bar{c}}{C_n} \qquad 56$$

The distance from the forward perpendicular to the center of effort of the rudder, $x_{cpr}$, is

$$x_{cpr} = x_{\bar{pc}/4} + x_{rs} \tag{57}$$

where $x_{rs}$ is the distance from the forward perpendicular to the rudder stock.

The yawing moment due to rudder forces is

$$N_r = x_{cpr} Y_r \tag{58}$$

Rudder Heeling Moment

From reference 26, the distance to the spanwise center of effort from the root chord, $z_{ro}$, is

$$z_{ro} = \frac{(C_{lr}(4/3\pi) \cos\alpha_r + C_{dr} \sin\alpha_r) b_r}{C_n} \tag{59}$$

The distance from the waterline to the center of effort is

$$z_{cpr} = z_{ro} + z_{rrc} \tag{60}$$

where $z_{rrc}$ is the distance from the waterline to the root chord as shown in Figure 12.

The rudder heeling moment, $K_r$, is

$$K_r = z_{cpr} C_{lr} (\tfrac{1}{2}\rho_{H_2O} A_r U_b^2) \tag{61}$$

2.1.4 Hydrostatic Forces

A satisfactory model for the hydrostatic righting moment is presented by Kerwin in reference (5). In modified form, Kerwin's (5) model for the hydrostatic righting moment, $N_r$, is adopted.

$$N_r = -0.00224[\Delta/(L/100)^3]\ L^4\phi(d_1+d_2\phi+d_3F_n) + z_g \sin\phi \qquad 62$$

where L is the waterline length, LWL, and $d_1$, $d_2$, and $d_3$ are non-dimensional stability coefficients which depend on hull form. The term, $z_g \sin\phi$ accounts for the distance from the waterline to the center of gravity.

Each coefficient has physical significance and may be input by the model user or generated from the expressions given below. A systematically varied yacht series based on the yacht, Standfast 43, is presently being tested jointly by M.I.T. and Delft University. The hydrostatic data from this series was utilized to generate parameterized expressions for each of the coefficients.

The coefficient, $d_1$, is the height of the metacenter above the waterline divided by the load waterline length, LWL. An expression for $d_1$ which accurately predicts the Standfast 43 series is:

$$d_1 = \frac{1119(BWL/L)^3}{[\Delta/(L/100)^3]} - 0.335/(L/T_c) \qquad 63$$

The coefficient, $d_2$, is the non-linear effect on the righting moment. The emperical expression for $d_2$ is

$$d_2 = d_1[0.0822(BLW/L) - 0.02162] \quad 64$$

The coefficient, $d_3$, quantifies the effect the wave train has on the stability at high Froude Numbers. This effect depends on the boat's beam to length ratio, BWL/L, and the fineness of her bow and stern. The expression for $d_3$ is an emperical fit to Standfast 43 data and is only dependent on the beam to length ratio.

$$d_3 = [7.8 - 56{,}350(BWL/L-0.28)^{2.75}\ (10^{-5}) \quad BWL/L > 0.28 \quad 65$$

and

$$d_3 = 7.8 \times 10^{-5} \quad BWL/L \leq 0.28 \quad 66$$

The location of the center of gravity below the water-line, $z_g$, may be specified. If not specified, $z_g$ is assumed to be

$$z_g = 0.025L. \quad 67$$

## V. RESULTS

Figures 17 and 18 are performance polar plots of two yachts. Figure 17 shows the theoretical boat velocity of the yacht Antiope as predicted by the mathematical model. The velocity is plotted as a function of the true wind angle, $\gamma$, and the three wind velocities 5, 7.5, and 10 knots. For this prediction the sail area was assumed to be 400 square feet and the center of gravity is 0.61 feet below the waterline. The sailplan geometry and placement was generated by the model and the keel fixed rudder was modeled by placing the program's spade rudder at the trailing edge of the keel and setting the wetted surface of the rudder equal to zero. Since the correlation of many of the model's forces are derived from data of the full scale testing of Antiope (3), her performance polar is included in the results even though the model is not designed for accurate prediction of rudder forces on keel mounted rudders.

Figure 18 gives the performance polar of the model generated sailing boat for the same three wind velocities. The geometry of each boat is fully described in the computer printout listed in Section 8.3. The two example output listings in Section 8.3 are the source for the plots in Figures 17 and 18.

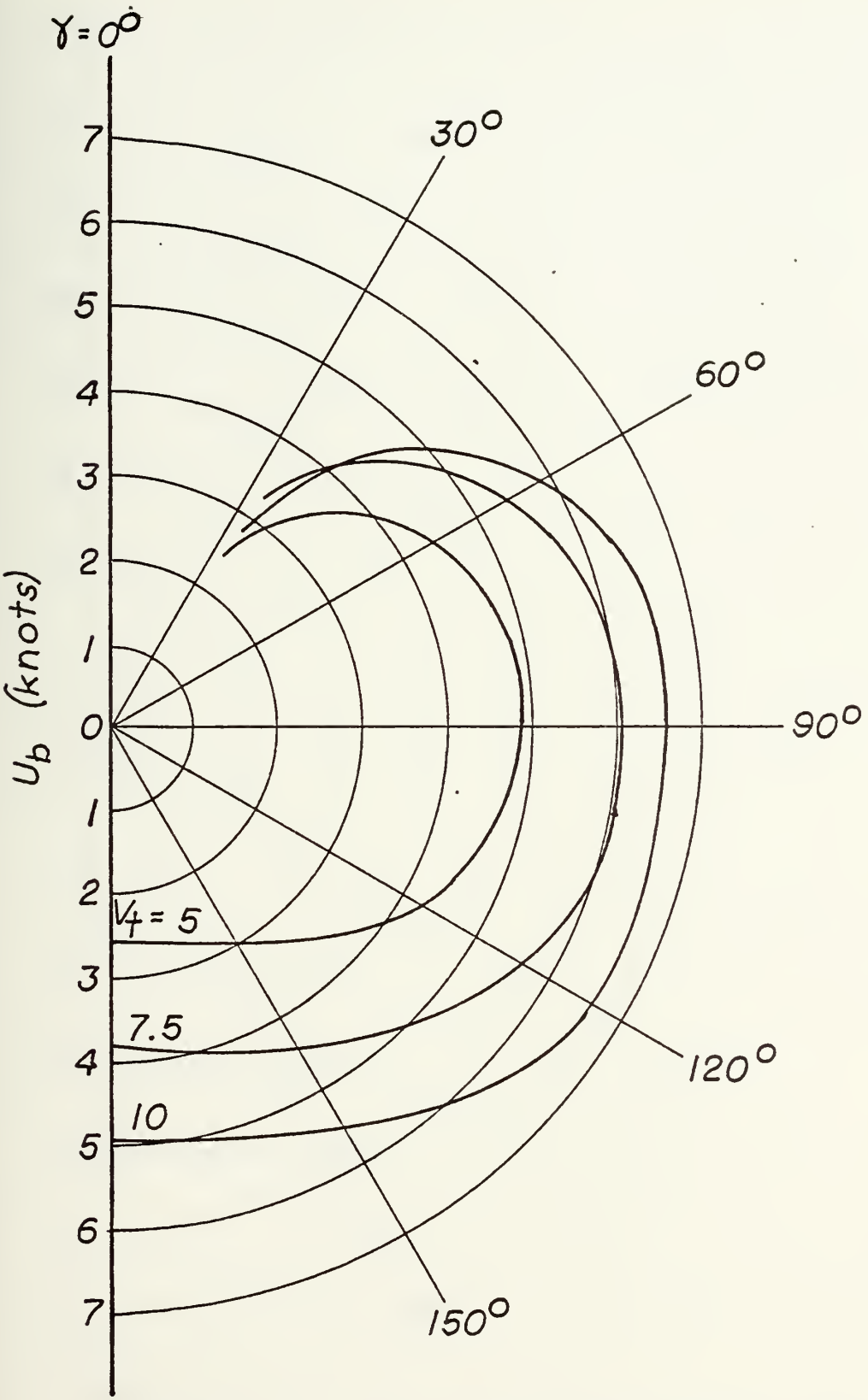



Figure 17 - Antiope Performance Polar

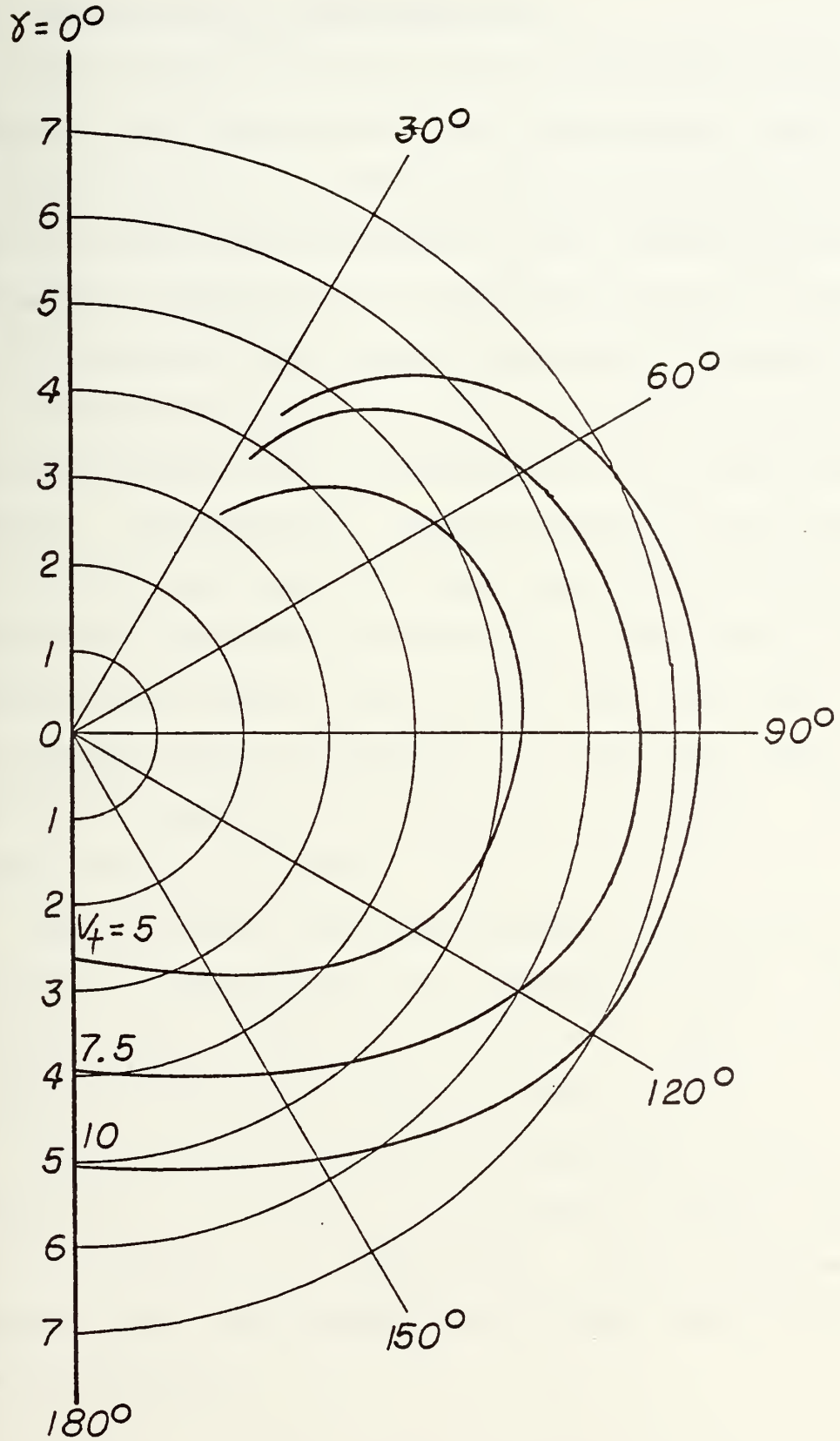



Figure 18 – Default Boat Peformance Polar

## VI. CONCLUSIONS AND RECOMMENDATIONS

Two important criteria should be considered when evaluating the capabilities of a system model. The first is the verification of the accuracy of the predicted performance, and the second is an assessment of the capabilities and limitations a model has for predicting changes in performance due to variation in the controlling geometric parameters.

To determine the accuracy of the model in predicting total performance, the performance data of a known yacht is required. Unfortunately, the measurement of the performance of an actual yacht under sail has never been accomplished. To provide a basis for correlation, the four independent variables, boat speed, leeway angle, heel angle, and rudder angle would have to be measured on a full scale yacht along with true or apparent wind velocity and direction. This data is not available to date.

Other programs exist for resolving tow tank data and assumed sail coefficients into performance polars. These programs might be used in the future as a basis for comparison if large or full scale towing tank data is used.

The use of other performance prediction programs for correlation is not useful unless another standard exists with which to measure their capabilities. If two performance programs agree, the agreement may be that both will give the same wrong answer.

The polar plots in Figures 17 and 18 are considered reasonable only because they correlate subjectively with the author's own sailing experience. Though each component force is correlated against either emperical or theoretical data, a means of examining the capability of the mathematical model for the total system should be developed in the future.

The capability of a mathematical model to respond correctly to changes in boat geometry and therefore enable parametric tradeoffs requires physical accuracy of the individual force models. When the individual force models were presented, the limitation and capabilities of each was discussed. The limitations and capabilities of each model are summerized below.

Hull Resistance

Hull resistance is calculated by superposition of frictional resistance, wave resistance and form resistance.

The frictional resistance coefficient is based on the ITTC line and is applied to the fairbody, the keel and the rudder. This line includes an unspecified amount of form resistance. Future model refinement should include a frictional coefficient which does not include form resistance and a mathematical model that parameterizes form resistance. The form resistance coefficient is not parameterized in the present model.

Wave resistance is estimated by a combination of the results of Michell's theory, Taylor Standard Series tests and full scale tests of the yacht Antiope. The resulting semi-emperical mathematical model for wave resistance needs to be compared to the results of a series of full scale yacht wave resistance tests.

The mathematical model for hull resistance is considered adequate for predicting calm water resistance. To predict a boat's performance in rough water, a mathematical model predicting the added resistance due to waves should be developed.

The change in resistance due to heel angle is also not parameterized and was modeled as an average of what good designs can expect. The investigation and incorporation of heel effects would be worthwhile.

The present resistance model is considered dependable for parametric variation in displacement to length ratio and wetted surface.

Keel Forces

The hydrodynamic side force on the hull and keel are derived from slender-body theory modified for fish-like forms (24). This model provides accurate prediction of forms fixed with moderate keels such as found on the yacht Antiope. A method for determining decrease in lift as the keel chord decreases at a given span should be developed. The present

method adequately models changes in performance due to draft but is insensitive to reduction in keel area due to chord length changes.

The interference effects between the hull boundary layer and the root chord of the keel should be the subject of further investigation.

Rudder Forces

The rudder forces are modeled from the free stream tests of low and medium aspect ratio lifting surfaces (26). The model is adequate for yachts with spade rudders, but many yachts are being designed with skeg rudders. A model should be developed for rudder forces as a function of the percentage flap on the skeg rudder. The fairbody boundary layer interference effects on the rudder have been ignored in the present model.

The mathematical model is expected to satisfactorily model changes in the spade rudder geometry.

Hydrostatic Forces

Hydrostatic forces are modeled using the concept of the metacentric height and are adjusted for Froude Number effects. The model is considered sensitive to geometric changes though further verification of the Froude Number effects is desirable.

To accurately model the righting moment on smaller yachts, a function representing the effect of crew weight on righting moment should be added.

Sail Forces

The sail force mathematical model is based on lifting surface theory presented in reference (29). The model is adequate for close hauled prediction but is not parameterized for reaching and running due to lack of data. Work is needed to determine force coefficients as a function of the apparent wind angle and sail plan geometry for off wind conditions. Further work needs to be accomplished to parameterize the form drag coefficient as a function of rig geometry and apparent wind angle.

The utilization of the model should be limited to light and moderate wind conditions until the optimization variables for reefing and flattening are included.

The effect of the vertical wind gradient on heel has not been included and should be added in the future. When added resistance in waves is investigated, it will also be important to study the effect large pitching motions have on sail forces and their relationship to the added resistance in waves.

The limitations of the sail force model in its present form preclude the accurate prediction in off wind and heavy air conditions.

Aerodynamic Hull Forces

The wind forces acting on the hull are modeled from data on cargo ship hulls (30). Though the model is derived from a different hull form, the prediction of these forces

is considered reasonable. Tests on yacht hulls would help improve the correlation for this mathematical model, but the effect on the final prediction should be minor.

In Conclusion

The present form of the mathematical models is useful for preliminary design in determining the quantitative effect changes in the major geometrical parameters have on a boat's performance. These parameters include displacement to length ratio, wetted surface, beam to length ratio, total draft, rudder geometry, position of the center of gravity, sail plan geometry for on wind conditions, and sail area.

The development of the model has been useful in cataloguing available theoretical and emperical sources for modeling forces acting on a sailing boat and has made clear the necessary improvements required in the science of sailing boats to improve prediction capability. For the naval architect, this first generation system model for sailing boat performance may be used as a file to which improvements may be made as a greater understanding of the science develops.

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## VIII. APPENDICES

### 8.1 Computer Input

The required data cards are divided into two data sets described below:

#### Card Set Number One

Card set number one consists of the input points necessary to generate the spine cubic curves required by the force models. There are twenty-four cards punched in FORMAT (8F10.0). This data set is an integral part of the program and does not change from run to run. Table 1 is a listing of the required data cards.

#### Card Set Number Two

Card set number two is repeated for each boat evaluated by the mathematical model. The cards control the program options and describe the geometry of a given sailing boat. A listing of the card set used to describe the yacht Antiope is given in Table 2. Table 3 is an example of the required data set where all parameters are defaulted.

| | Card Set #2 |
|---|---|
| card #1 | IFAM, NGAM, NVT; FORMAT (8I10); no default. |
| col 10 | If IFAM = 1 forces and moments are printed. |
| | If IFAM = 0 no forces and moments are printed. |
| col 11 - 20 | NGAM = number of true wind angles desired. |
| col 21 - 30 | NVT = number of true wind velocities desired. |

| | |
|---|---|
| card #2 | ITMAX, IPRINT, N; FORMAT (10X, I3, 17X, I1, 19X, I3); no default. |
| col 11 - 13 | ITMAX = maximum number of iterations allowed per solution. |
| col 31 | If IPRINT = 1, the independent variables, apparent wind data, and forces and moments will be printed out each iteration.<br><br>If IPRINT = 0, only the convergent or final iteration will be printed. |
| col 53 | N = 4, the number of degrees of freedom |
| card #3 | EPS1, EPS2; FORMAT (10X, E7.1, 13X, E7.1); no default. |
| col 11 - 17 | EPS1 = required tolerance in force equilibrium. |
| col 31 - 37 | EPS2 = step size taken for computing first differences. |
| card #4 | (XOLD(I), I=1,4); FORMAT (20X, 5F10.3); no default. |
| col 21 - 30 | XOLD(1) = initial assumed value of boat velocity, (feet per second) |
| col 31 - 40 | XOLD(2) = initial assumed heel angle, (degrees) |
| col 41 - 50 | XOLD(3) = initial assumed leeway angle, (degrees) |
| col 51 - 60 | XOLD(4) = initial assumed rudder angle, (degrees) |
| card #5 or more | (KVT(I),I = 1,NVT); FORMAT (8F10.5); no default. |
| col 1 - 80 | KVT(I) = desired true wind velocities (knots) |
| card #6 or more | DGAMMA(I), I = 1,NGMA); FORMAT (8F10.5), no default |
| col 1 - 80 | DGAMMA(I) = desired true wind angles (degrees) |

| | |
|---|---|
| card #7 | C(2), C(7), C(8), C(9), C(10); FORMAT (8F10.5); default = -1.0 |
| col 1 - 10 | C(2) = waterline length (feet |
| col 11 - 20 | C(7) = displacement to length ratio |
| col 21 - 30 | C(8) = prismatic coefficient |
| col 31 - 40 | C(9) = length to draft ratio |
| col 41 - 50 | C(10) = distance from FP to LCB (%LWL) |
| card #8 | C(11), FORMAT (E14.7), default = -1.0 |
| col 1 - 14 | C(11) = kinematic viscosity of water |
| card #9 | (C(I), I = 12,18); FORMAT (8F10.5); default = -1.0 |
| col 1 - 10 | C(12) = density of water |
| col 11 - 20 | C(13) = mean keel chord (feet) |
| col 21 - 30 | C(14) = mean rudder chord (feet) |
| col 31 - 40 | C(15) = form and correlation coefficient |
| col 41 - 50 | C(16) = fairbody wetted surface |
| col 51 - 60 | C(17) = keel wetted surface |
| col 61 - 70 | C(18) = rudder wetted surface |
| card #10 | C(1), C(3), C(4), C(5), C(6); FORMAT (8F10.5); default = -1.0 |
| col 1 - 10 | C(1) = beam to length ratio |
| col 11 - 20 | C(3) = sail area |
| col 21 - 30 | C(4) = heeling moment arm |
| col 31 - 40 | C(5) = pitching moment arm |
| col 41 - 50 | C(6) = distance from FP to rudder stock |

| | |
|---|---|
| card #11 | (C(I),I = 19,26); FORMAT (8F10.5); default = -1.0 |
| col 1 - 10 | C(19) = close hauled lift coefficient |
| col 11 - 20 | C(20) = rig form drag coefficient |
| col 21 - 30 | C(21) = cross sectional area of rig |
| col 31 - 40 | C(22) = sail frictional coefficient |
| col 41 - 50 | C(23) = induced drag coef/lift coef$^2$ |
| col 51 - 60 | C(24) = lateral area of the hull |
| col 61 - 70 | C(25) = transverse area of the hull |
| col 71 - 80 | C(26) = distance from CE sail to FP |
| card #12 | (C(I),I = 27,30); FORMAT (8F10.5); default = -1.0 |
| col 1 - 10 | C(27) = off wind drag coefficient |
| col 11 - 20 | C(28) = off wind lift coefficient |
| col 21 - 30 | C(29) = distance for CE hull to FP |
| col 31 - 40 | C(30) = density of air |
| card #13 | (C(I), I = 31,38); FORMAT (8F10.5); default = -1.0 |
| col 1 - 10 | C(31) = $x_0$ |
| col 11 - 20 | C(32) = $x_1$ |
| col 21 - 30 | C(33) = $x_2$ |
| col 31 - 40 | C(34) = $x_3$ |
| col 41 - 50 | C(35) = $x_b$ |
| col 51 - 60 | C(36) = $b_0$ |
| col 61 - 70 | C(37) = $b_1$ |
| col 71 - 80 | C(38) = $b_2$ |

| | |
|---|---|
| card #14 | C(39), C(40); FORMAT (8F10.5); default=-1.0 |
| col 1 - 10 | C(39) = $b_3$ |
| col 11 - 20 | C(40) = $b_b$ |
| card #15 | (C(I), I = 41,43); FORMAT (8F10.0); default = -1.0 |
| col 1 - 10 | C(41) = draft of the canoe body/total draft |
| col 11 - 20 | C(42) = hydrodynamic lift coefficient |
| col 21 - 30 | C(43) = $\psi$X lift/drag |
| card #16 | (C(I), I = 45,52); FORMAT (8F10.5); default = -1.0 |
| col 1 - 10 | C(45) = distance from LWL to rudder root chord |
| col 11 - 20 | C(46) = rudder root chord |
| col 21 - 30 | C(47) = rudder tip chord |
| col 31 - 40 | C(48) = rudder span |
| col 41 - 50 | C(49) = rudder sweep angle |
| col 51 - 60 | C(50) = rudder aspect ratio |
| col 61 - 70 | C(51) = rudder mean chord |
| col 71 - 80 | C(52) = rudder $\partial C_l/\partial \alpha_r$ |
| card #17 | (C(I), I = 53,56), C(61); FORMAT (8F10.5); default = -1.0 |
| col 1 - 10 | C(53) = rudder cross flow drag coefficient |
| col 11 - 20 | C(54) = rudder $\partial C_m/\partial C_l$ |
| col 21 - 30 | C(55) = rudder form drag coefficient |
| col 31 - 40 | C(56) = rudder area |
| col 41 - 50 | C(61) = distance from CE keel to LWL |

| | |
|---|---|
| card #18 | (C(I), I = 57,60); FORMAT (8F10.5); default = -1.0 |
| col 1 - 10 | C(57) = metacentric height/LWL |
| col 11 - 20 | C(58) = Froude Number righting moment coefficient |
| col 21 - 30 | C(59) = non-linear hydrostatic coefficient |
| col 31 - 40 | C(60) = distance from LWL to CG |
| card #19 | (C(I), I = 62,69); FORMAT (8F10.5); default = -1.0 |
| col 1 - 10 | C(62) = mast height |
| col 11 - 20 | C(63) = base of the fortriangle |
| col 21 - 30 | C(64) = main hoist |
| col 31 - 40 | C(65) = main boom length |
| col 41 - 50 | C(66) = aspect ratio of the fortriangle |
| col 51 - 60 | C(67) = aspect ratio of the main |
| col 61 - 71 | C(68) = aspect ratio of the sail area |
| col 71 - 80 | C(69) = distance from mast aft to sail CE |
| card #20 | C(70), C(71); FORMAT (8F10.5); default=-1.0 |
| col 1 - 10 | C(70) = forward overhang |
| col 11 - 20 | C(71) = freeboard |
| card #21 | KEND, FORMAT (I1), no default |
| col 1 | If KEND = 1, indicates this is final data set<br><br>If KEND = 0, indicates other data sets to follow |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 0.0 | 0.2 | 0.4 | 0.6 | 0.7 | 0.8 | 0.9 | 1.0 |
| 1.1 | 1.2 | 1.25 | | | | | |
| 0.0 | 0.00006 | 0.00011 | 0.000277 | 0.0028 | 0.00703 | 0.01425 | 0.0349 |
| 0.0549 | 0.07196 | 0.0898 | | | | | |
| 0.0 | 0.0011 | 0.0022 | 0.0033 | 0.00385 | 0.006 | 0.008 | 0.01 |
| 0.008 | 0.006 | 0.005 | | | | | |
| 0.0 | 0.007 | 0.012 | 0.02 | 0.025 | 0.03 | 0.046 | 0.0821 |
| 0.0467 | 0.0326 | 0.029 | | | | | |
| 0.53 | 0.53 | 0.53 | 0.53 | 0.53 | 0.54 | 0.545 | 0.535 |
| 0.547 | 0.58 | 0.60 | | | | | |
| 0.0 | 0.08767 | 0.17453 | 0.34907 | 0.5236 | 0.69813 | 0.87266 | 1.0472 |
| 1.2217 | 1.3963 | 1.5708 | 1.7453 | 1.9199 | 2.0944 | 2.2689 | 2.4434 |
| 2.618 | 2.7925 | 2.9671 | 3.0543 | 3.1416 | | | |
| 0.0 | 0.8378 | 1.1345 | 1.4312 | 1.5359 | 1.5533 | 1.5708 | 1.5708 |
| 1.5708 | 1.5708 | 1.5708 | 1.5708 | 1.5708 | 1.5708 | 1.5795 | 1.6057 |
| 1.6406 | 1.6929 | 1.8326 | 2.0595 | 3.1416 | | | |
| 0.0 | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 |
| 0.8 | 0.9 | 1.0 | | | | | |
| 1.0 | 0.98 | 0.95 | 0.885 | 0.8 | 0.68 | 0.535 | 0.385 |
| 0.22 | 0.09 | 0.0 | | | | | |
| 2.0 | 2.002 | 2.012 | 2.042 | 2.095 | 2.184 | 2.33 | 2.555 |
| 3.0 | 5.0 | 10.0 | | | | | |
| 1.64 | 2.06 | 2.4728 | 2.885 | 3.297 | | | |
| 0.1927 | 0.1546 | 0.1303 | 0.1132 | 0.1009 | | | |



TABLE 1

```
          0          9          3
ITMAX  =    10       IPRINT =  0          N       =    4
EPS1   =  1.0E-10    EPS2   =  1.0E-02
XOLD(1)...XOLD(4)    10.0       0.0        0.0        0.0
5.0        7.5       10.0
180.0      160.0     140.0      120.0      100.0      80.0       60.0       45.0
35.0
24.3       180.4     0.53       12.15      53.5
   0.12791E-04
1.99       7.125     0.0        0.0        118.61     41.382     0.0
0.239      400.0     -1.0       -1.0       16.0
1.25       0.4       19.6       0.04       0.1303     100.0      27.0       11.5
0.0        0.0       -1.0       0.00238
0.0        5.75      8.51       14.67      16.91      4.65       4.62       2.12
0.78       0.0
0.35       -1.0      -1.0       -1.0
-1.0       -1.0      -1.0       -1.0       -1.0       -1.0       -1.0       -1.0
-1.0       -1.0      -1.0       -1.0       -1.0
-1.0       -1.0      -1.0       -1.0
-1.0       -1.0      -1.0       -1.0       -1.0       -1.0       -1.0       -1.0
-1.0       2.75      -1.0       -1.0       -1.0       -1.0       -1.0       -1.0
0
```



TABLE 2

```
          0          9          3
ITMAX  =    10       IPRINT =  0        N      =    4
EPS1   =  1.0E-10    EPS2   =  1.0E-02
XOLD(1)...XOLD(4)    10.0       0.0       0.0       0.0
5.0         7.5      10.0
180.0       160.0    140.0      120.0     100.0     80.0      60.0      45.0
35.0
-1.0        -1.0     -1.0       -1.0      -1.0      -1.0      -1.0      -1.0
       -0.1E 01
-1.0        -1.0     -1.0       -1.0      -1.0      -1.0      -1.0      -1.0
-1.0        -1.0     -1.0       -1.0      -1.0      -1.0      -1.0      -1.0
-1.0        -1.0     -1.0       -1.0      -1.0      -1.0      -1.0      -1.0
-1.0        -1.0     -1.0       -1.0      -1.0      -1.0      -1.0      -1.0
-1.0        -1.0     -1.0       -1.0      -1.0      -1.0      -1.0      -1.0
-1.0        -1.0     -1.0       -1.0      -1.0      -1.0      -1.0      -1.0
-1.0        -1.0     -1.0       -1.0      -1.0      -1.0      -1.0      -1.0
-1.0        -1.0     -1.0       -1.0      -1.0      -1.0      -1.0      -1.0
-1.0        -1.0     -1.0       -1.0      -1.0      -1.0      -1.0      -1.0
-1.0        -1.0     -1.0       -1.0      -1.0      -1.0      -1.0      -1.0
-1.0        -1.0     -1.0       -1.0      -1.0      -1.0      -1.0      -1.0
1
```

TABLE 3

## 8.2 Computer Listing

The main program and all necessary subroutines utilized to compute the mathematical model are listed in this section.

```
C      MAIN PROGRAM
C
       REAL KVA,KVT,KXOLD1
       REAL*8 A,XINC,EPS1,SIMUL,DABS
       DIMENSION AY(15,4),AXOLD(4)
       DIMENSION XIN(11),YIN1(11),YIN2(11),YIN3(11),CPIN(11)
       DIMENSION AE1(44),AE2(44),AE3(44),AEP(44)
       DIMENSION CLIN(11),DLIN(11)
       DIMENSION BIN(21),AIN(21),AEA(80),
      1XOLD(21),XINC(21),A(5,5),Y(15),D(15,4),
      2ROB(11),AEL(40),AEDL(40),KVT(20),DGAMMA(40),C(100)
       DIMENSION ARSP(5),DILN(5),ADIL(16)
       DIMENSION VOLD(4)
C
C      DUCK FIT SECTION
C
       READ (5,300)  (XIN(I),I=1,11)
       READ (5,300)  (YIN1(I),I=1,11)
       READ (5,300)  (YIN2(I),I=1,11)
       READ (5,300)  (YIN3(I),I=1,11)
       READ (5,300)  (CPIN(I),I=1,11)
       READ (5,300)  (BIN(I), I=1,21)
       READ (5,300)  (AIN(I), I=1,21)
       READ (5,300)  (ROB(I),I=1,11)
       READ (5,300)  (CLIN(I),I=1,11)
       READ (5,300)  (DLIN(I),I=1,11)
       READ (5,300)  (ARSP(I),I=1,5)
       READ (5,300)  (DILN(I),I=1,5)
   300 FORMAT (8F10.0)
       CALL UGLYDK (11,2,1,XIN,YIN1,0.0,0.0,AE1)
       CALL UGLYDK (11,2,2,XIN,YIN2,0.0,0.0,AE2)
       CALL UGLYDK (11,2,2,XIN,YIN3,0.0,0.0,AE3)
       CALL UGLYDK (11,2,2,XIN,CPIN,0.0,0.0,AEP)
       CALL UGLYDK (21,2,0,BIN,AIN,0.0,0.0,AEA)
       CALL UGLYDK (11,2,0,ROB,CLIN,0.0,0.0,AEL)
       CALL UGLYDK (11,2,0,ROB,DLIN,0.0,0.0,AEDL)
```

```
      CALL UGLYDK (5,2,0,ARSP,DILN,0.0,0.0,ADIL)
C
C     READ AND PRINT DATA
C
    1 CONTINUE
      READ (5,310) IFAM,NGAM,NVT
  310 FORMAT (8I10)
    2 READ (5,100) ITMAX,IPRINT,N,EPS1,EPS2,(VOLD(I),I=1,N)
      WRITE (6,205) ITMAX,IPRINT,N,EPS1,EPS2,N,(VOLD(I),I=1,N)
      READ (5,300) (KVT(I),I=1,NVT)
      READ (5,300) (DGAMMA(I),I=1,NGAM)
      WRITE (6,315) (KVT(I),I=1,NVT)
  315 FORMAT ('0',9X,'SOLUTIONS ARE COMPUTED FOR THE FOLLOWING TRUE',
     1' WIND SPEEDS (KNOTS)'//(10F10.5/))
      WRITE (6,316) (DGAMMA(I),I=1,NGAM)
  316 FORMAT ('0',9X,'SOLUTIONS ARE COMPUTED FOR THE FOLLOWING TRUE',
     1' WIND ANGLES FOR EACH WIND SPEED'//(10F10.5/))
      VOLD(2)=VOLD(2)*.0174533
C
C     CALL GEOM TO EVALUATE REQUIRED GEOMETRIC COEFICENTS AND CONSTANTS
C
      CALL GEOM (C,ROB,AEL,AEDL,ARSP,ADIL)
C
C     ZERO Y AND D ARRAYS
C
      DO 6 I=1,13
      Y(I)=0.0
      DO 6 J=1,4
      AY(I,J)=0.0
    6 D(I,J)=0.0
      DO 80 II=1,NVT
      DO 15 I=1,4
   15 XOLD(I)=VOLD(I)
      VT=KVT(II)*1.689
      DO 70 III=1,NGAM
      GAMMA=DGAMMA(III)*.0174533
```

```
C
C     NEWTON-RAPHSON ITERATICN
C
    7 CONTINUE
      DO 50 ITER=1,ITMAX
C
C     SET UP AUGMENTED VALUES FOR DIRIVATIVES
C
      DO 8 I=1,4
    8 AXOLD(I)=XOLD(I)+EPS2
C
C     CALL SAIL TO EVALUATE AERCDYNAMIC FORCES, MOMENTS AND PARTIALS
C
      CALL SAIL (XOLD,AXOLD,VT,GAMMA,C,Y,AY,KVA,DBETTA,BIN,AEA)
C
C     CALL RTMOM TO EVALUATE THE HYDROSTATIC RIGHTING MOMENT
C
      CALL RTMOM (XOLD,AXOLD,C,Y,AY)
C
C     CALL HULL TO EVALUATE HULL DRAG
C
      CALL HULL (XOID,AXOLD,C,Y,AY,AE1,AE2,AE3,AEP,XIN)
C
C     CALL KEEL TO EVALUATE INDUCED KEEL FORCES
C
      CALL KEEL (XOLD,AXOLD,C,Y,AY)
C
C     CALL RUDDR TO EVALUATE INDUCED RUDDER FCRCES
C
      CALL RUDDR(XOLD,AXOLD,C,Y,AY)
C
C     COMPUTE PARTIAL DIRIVATIVES OF COMPONENT FORCES AND MOMENTS
C
      DO 10 I=1,15
      DO 10 J=1,4
   10 D(I,J)=(AY(I,J)-Y(I))/EPS2
```

```
C
C     CALL ON CALCN TO SET UP THE A MATRIX
C
      CALL CALCN (A,Y,D)
C
C     CALL SIMUL TO COMPUTE JACOBIAN AND CORRECTION IN XINC
C
      DETER=SIMUL (N,A,XINC,EPS1,1,5)
      IF (DETER.NE.0.0) GO TO 20
      WRITE (6,201)
      GO TO 60
C
C     CHECK FOR CONVERGENCE AND UPDATE XOLD VALUES
C
   20 ITCON=1
      DO 25 I=1,N
      IF (DABS(XINC(I)).GT.EPS2) ITCON=0
   25 XOLD(I)=XOLD(I)+XINC(I)
      IF (IPRINT.EQ.1) WRITE (6,202) ITER,DETER,N,(XOLD(I),I=1,N)
      IF (IPRINT.EQ.1) WRITE (6,206) KVA,DBETTA
      IF (IPRINT.EQ.1) WRITE (6,302) (I,Y(I),I=1,15)
      IF (ITCON.EQ.0) GO TO 50
      WRITE (6,208)
  208 FORMAT ('0',9X,'-----------------------------------------------')
      WRITE (6,207) KVT(II),DGAMMA(III)
  207 FORMAT ('0',9X,'KVT=  ',F10.5,'  KNOTS',10X,'DGAMMA=  ',F10.5,
     1'  DEGREES')
      WRITE (6,206) KVA,DBETTA
  206 FORMAT ('0',9X,'KVA=  ',F10.5,'  KNOTS',10X,'DBETTA=  ',F10.5,
     1'  DEGREES')
      IF (IFAM.EQ.1) WRITE (6,302) (I,Y(I),I=1,15)
  302 FORMAT ('0',9X,'FORCES AND MOMENTS'//(10X,I2,4X,E14.5,10X,I2,
     14X,E14.5,10X,I2,4X,E14.5//))
      KXOLD1=XOLD(1)/1.689
      DXOLD2=XOLD(2)*57.3
      WRITE (6,203) ITER,KXOLD1,DXOLD2,XOLD(3),XOLD(4)
```

```
      WRITE (6,208)
       GO TO 60
   50 CONTINUE
C
      WRITE (6,204)
      WRITE (6,207) KVT(II),DGAMMA(III)
      WRITE (6,206) KVA,DBETTA
      KXOLD1=XOLD(1)/1.689
      DXOLD2=XOLD(2)*57.3
      WRITE (6,203) ITER,KXOLD1,DXOLD2,XOLD(3),XOLD(4)
      GO TO 60
C
C     PROGRAM CONTROL SECTION
C
   60 CONTINUE
   70 CONTINUE
   80 CONTINUE
      READ (5,301) KEND
  301 FORMAT (I1)
      IF (KEND.EQ.0) GO TO 1
      IF (KEND.EQ.1) STOP
C
C     FORMATS FOR INPUT AND OUTPUT STATEMENTS
C
  100 FORMAT ( 10X,I3,17X,I1,19X,I3/ 10X,E7.1,13X,E7.1/ (20X, 5F10.3) )
  201 FORMAT ( 38H0MATRIX IS ILL-CONDITIONED OR SINGULAR )
  202 FORMAT ( 10H0ITER   = ,I8/  10H DETER  = , E18.5/
     2   26H           XOLD(1)...XOLD(, I2, 1H) / (1H ,1P4E16.6) )
  203 FORMAT ( 24H0SUCCESSFUL CONVERGENCE / 10H0ITER   = , I3//
     110X,'BOAT SPEED=  ',F10.5,'  KNOTS',10X,'HEEL ANGLE=  ',F10.5,
     2'  DEGREES'//10X,'LEEWAY ANGLE=  ',F10.5,'  DEGREES',
     310X,'RUDDER ANGLE=  ',F10.5,'DEGREES')
  204 FORMAT ( 15H NO CONVERGENCE )
  205 FORMAT ( 10H1ITMAX  = , I8/  10H IPRINT = , I8/  10H N      = ,
     1   I8/  10H EPS1   = ,1PE14.1/ 10H EPS2  = , 1PE14.1/
     2   26H0          XOLD(1)...XOLD(, I2, 1H) / 1H / (1H ,1P4E16.6) )
```

```
      STOP
C
      END
```

```
      SUBROUTINE GEOM (C,ROB,AEL,AEDL,ARSP,ADIL)
      DIMENSION C(100),ROB(11),AEL(40),AEDL(40)
      DIMENSION ARSP(5),DILN(5),ADIL(16)
C
C     ZERO C ARRAY
C
      DO 10 I=1,100
   10 C(I)=0.0
C
C     READ REQUIRED CONSTANTS
CC
      READ (5,100) C(2),C(7),C(8),C(9),C(10)
      READ (5,200) C(11)
  200 FORMAT (E14.7)
      READ (5,100) (C(I),I=12,18)
      READ (5,100) C(1),C(3),C(4),C(5),C(6)
      READ (5,100) (C(I),I=19,30)
      READ (5,100) (C(I),I=31,40)
      READ (5,100) (C(I),I=41,44)
      READ (5,100) (C(I),I=45,56),C(61)
      READ (5,100) (C(I),I=57,60)
      READ (5,100) (C(I),I=62,71)
C
C     DEFAULT SYNTHESIS MODEL
C
      CALL SYNTH (C,ROB,AEL,AEDL,ARSP,ADIL)
      STOT=C(72)
C
C     WRITE SECTION
C
      WRITE (6,150) C(2),C(7),C(8),C(9),C(10)
  150 FORMAT ('1',9X,'LWL=  ',F10.5//10X,'DISPLACEMENT TO LENGTH=  ',
     1F10.5//10X,'PRISMATIC=  ',F10.5//10X,'L/H=  ',F10.5//
     210X,'LCB=  ',F10.5)
      WRITE (6,220) (C(I),I=11,18),STOT
  220 FORMAT ('0',9X,'KINEMATIC VISCOSITY=  ',E14.7//10X,
```

```
     1'DENSITY OF WATER=  ',F10.5//10X,'MEAN KEEL CHORD=  ',F10.5//
     210X,'MEAN RUDDER CHORD=  ',F10.5//10X,
     3'ROUGHNESS AND CORRELATION FACTOR=  ',F10.5//10X,
     4'FAIRBODY WETTED SURFACE=  ',F10.5//10X,'KEEL WETTED SURFACE=  ',
     5F10.5//10X,'RUDDER WETTED SURFACE=  ',F10.5//10X,
     6'TOTAL WETTED SURFACE=  ',F10.5)
      WRITE (6,110) C(1),C(3),C(4),C(5),C(6)
  110 FORMAT ('0',9X,'BWL /LWL=  ',F10.5//10X,'SAIL AREA=  ',F10.5//
     110X,'HEELING MOMENT ARM=  ',F10.5//10X,'PITCHING MOMENT ARM=  ',
     2F10.5//10X,'DISTANCE FROM FP TO RUDDER STOCK=  ',F10.5)
  100 FORMAT (8F10.0)
      WRITE (6,230) (C(I),I=19,30)
  230 FORMAT ('0',9X,'CLOSE HAULED LIFT COEF=  ',F10.5//
     110X,'RIG FORM DRAG COEF=  ',F10.5//
     210X,'CROSS SECTIONAL AREA OF RIG=  ',F10.5//
     310X,'SAIL FRICTIONAL COEF=  ',F10.5//
     410X,'INDUCED DRAG COEF / LIFT COEF**2=  ',F10.5//
     510X,'LATERAL AREA OF HULL=  ',F10.5//
     610X,'TRANSVERSE AREA OF HULL=  ',F10.5//
     710X,'DISTANCE BETWEEN CE SAIL AND FP=  ',F10.5//
     810X,'OFF WIND DRAG COEF=  ',F10.5//
     910X,'OFF WIND LIFT COEF=  ',F10.5//
     110X,'DISTANCE BETWEEN CE HULL AND FP=  ',F10.5//
     210X,'DENSITY OF AIR=  ',F10.5)
      WRITE (6,240)(C(I),I=31,40)
  240 FORMAT ('0',9X,'HORIZONTAL DISTANCE FROM MAXIMUM DRAFT OF',
     1' PROFILE MEASUREMENTS'//5F10.5//10X,
     2'PROFILE MEASUREMENTS'//(5F10.5))
      WRITE (6,245)(C(I),I=41,43)
  245 FORMAT ('0',9X,'DRAFT OF CANOE BODY / TOTAL DRAFT=  ',F10.5//
     110X,'HYDRODYNAMIC LIFT COEF=  ',F10.5//
     210X,'LAMDA X LIFT / DRAG=  ',F10.5)
      WRITE (6,250) C(61),(C(I),I=45,56)
  250 FORMAT ('0',9X,'DISTANCE FROM LWL TO VERTICAL HYDRO CE=  ',F10.5//
     110X,'*** RUDDER SECTION ***'//
     210X,'DISTANCE FROM LWL TO ROOT CHORD=  ',F10.5//
```

```
     310X,'ROOT CHORD=  ',F10.5//10X,'TIP CHORD=  ',F10.5//
     410X,'RUDDER SPAN=  ',F10.5//10X,'SWEEP ANGLE=  ',F10.5//
     510X,'ASPECT RATIO=  ',F10.5//10X,'MEAN CHORD=  ',F10.5//
     610X,'DCL / DALPHA=  ',F10.5//10X,'CROSS FLOW DRAG COEF=  ',F10.5//
     710X,'DCM / DCL=  ',F10.5//10X,'FORM DRAG COEF=  ',F10.5//
     810X,'RUDDER AREA=  ',F10.5)
      WRITE (6,254)
  254 FORMAT ('0',9X,'*** RIGHTING MOMENT SECTION ***')
      WRITE (6,255) (C(I),I=57,60)
  255 FORMAT ('0',9X,'METACENTRIC HEIGHT / LWL=  ',F10.5//
     110X,'FROUDE NUMBER RIGHTING MOMENT COEF=  ',E14.7//
     210X,'NON LINEAR HYDROSTATIC COEF=  ',E14.7//
     310X,'DISTANCE BELOW LWL TO CG=  ',F10.5)
      WRITE (6,260) (C(I),I=62,71)
  260 FORMAT ('0',9X,'*** SAIL SECTION ***'//
     110X,'I=  ',F10.5,10X,'J=  ',F10.5//
     210X,'P=  ',F10.5,10X,'E=  ',F10.5//
     310X,'AR FOR TRI=  ',F10.5,10X,'AR MAIN=  ',F10.5//
     410X,'AR SAIL PLAN=  ',F10.5//
     510X,'CE SAIL PLAN AFT MAST=  ',F10.5//
     610X,'FORWARD OVERHANG=  ',F10.5//
     710X,'FREEBOARD=  ',F10.5)
      WRITE (6,300)
  300 FORMAT ('1')
      RETURN
C
      END
```

```
      SUBROUTINE SYNTH (C,ROB,AEL,AEDL,ARSP,ADIL)
      DIMENSION C(100),ROB(11),AEL(40),AEDL(40)
      DIMENSION ARSP(5),DILN(5),ADIL(16)
      DIMENSION ARSPO(1),DILO(1)
      IF (C(2).EQ.-1.0) C(2)=30.0
      IF (C(7).EQ.-1.0) C(7)=225.0
      IF (C(8).EQ.-1.0) C(8)=0.53
      IF (C(1).EQ.-1.0) C(1)=0.3633-0.002018*C(2)
      IF (C(9).EQ.-1.0) C(9)=10975.0*C(1)/C(7)
      IF (C(6).EQ.-1.0) C(6)=0.95*C(2)
      IF (C(10).EQ.-1.0) C(10)=53.0
      IF (C(11).EQ.-1.0) C(11)=0.12791E-04
      IF (C(12).EQ.-1.0) C(12)=1.99
      IF (C(13).EQ.-1.0) C(13)=0.23*C(2)
      IF (C(15).EQ.-1.0) C(15)=0.0
      IF (C(16).EQ.-1.0) C(16)=C(2)*C(2)*(1.7/C(9)+3.5E-05*C(7)*C(9))
     1*(0.0712*(C(1)*C(9)-4.0)+1.0)
      IF (C(19).EQ.-1.0) C(19)=1.25
      IF (C(20).EQ.-1.0) C(20)=0.4
      IF (C(22).EQ.-1.0) C(22)=0.04
      IF (C(3).NE.-1.0) GO TO 30
      C(3)=C(2)*C(2)
   30 CONTINUE
      IF (C(62).NE.-1.0) GO TO 32
      C(62)=SQRT(C(3)/0.4044)
      C(63)=C(62)/3.0
      C(64)=C(62)/1.1
      C(65)=C(64)/3.0
      C(66)=3.0
      C(67)=3.0
      C(68)=C(62)*C(62)/C(3)
   32 CONTINUE
      ARSPO(1)=C(68)
      IF (C(23).EQ.-1.0) CALL EVALDK (5,1,ARSP,ARSPO,DILO,ADIL)
      IF (C(67).LE.C(66)) GO TO 35
      IF (C(23).EQ.-1.0) C(23)=DILO(1)+0.00892*(18.2-C(68))*(C(67)-C(66)
```

```
     1)
       GO TO 40
    35 CONTINUE
       IF (C(23).EQ.-1.0) C(23)=DILO(1)
    40 CONTINUE
       IF (C(27).EQ.-1.0) C(27)=0.0
       IF (C(28).EQ.-1.0) C(28)=0.0
       IF (C(30).EQ.-1.0) C(30)=0.00238
       C(31)=0.0
       IF (C(32).EQ.-1.0) C(32)=0.1*C(2)
       IF (C(33).EQ.-1.0) C(33)=0.2*C(2)
       IF (C(34).EQ.-1.0) C(34)=0.3*C(2)
       IF (C(35).EQ.-1.0) C(35)=0.55*C(2)
       IF (C(36).EQ.-1.0) C(36)=0.146*C(2)+2.0
       IF (C(37).EQ.-1.0) C(37)=0.98*C(36)
       IF (C(38).EQ.-1.0) C(38)=0.95/C(9)*C(2)
       IF (C(39).EQ.-1.0) C(39)=0.7/C(9)*C(2)
       C(40)=0.0
  125  IF (C(41).EQ.-1.0) C(41)=C(2)/C(9)/C(36)
    42 CALL LAMC (C,ROB,AEL,AEDL)
       IF (C(26).EQ.-1.0) C(26)=C(29)
       IF (C(69).EQ.-1.0) C(69)=0.02*(C(63)+C(65))
       IF (C(70).EQ.-1.0) C(70)=C(63)+C(69)-C(26)
       IF (C(71).EQ.-1.0) C(71)=0.057*C(2)+2.0
       IF (C(24).EQ.-1.0) C(24)=(2.1*C(2)+C(70))/2.0*C(71)
       IF (C(25).EQ.-1.0) C(25)=1.1*C(1)*C(2)*C(71)
       IF (C(4).EQ.-1.0) C(4)=0.43*C(62)+C(71)
       IF (C(17).EQ.-1.0) C(17)=2.1*(C(36)-C(2)/C(9))*C(13)
       IF (C(21).EQ.-1.0) C(21)=C(62)*0.01*(C(64)+C(65))
       IF (C(5).EQ.-1.0) C(5)=0.48*C(62)+C(71)
C
CC     RUDDER MODEL
C
       IF (C(6).EQ.-1.0) C(6)=0.95*C(2)
       IF (C(45).EQ.-1.0) C(45)=0.2*C(2)/C(9)
       IF (C(46).EQ.-1.0) C(46)=0.075*C(2)
```

```
      IF (C(47).EQ.-1.0)  C(47)=0.667*C(46)
      IF (C(48).EQ.-1.0)  C(48)=0.85*(C(36)-C(45))
      IF (C(49).EQ.-1.0)   C(49)=0.0
      C(51)=(C(46)+C(47))/2.0
      IF (C(50).EQ.-1.0)  C(50)=(C(48)+C(48))/C(51)
      IF (C(52).EQ.-1.0)  C(52)=0.09869*C(50)/(COS(C(49)/57.3)*SQRT(
     1C(50)**2/COS(C(49)/57.3)**4.0+4.0)+1.8)
      IF (C(53).EQ.-1.0)  C(53)=0.08+0.72*C(47)/C(46)
      IF (C(54).EQ.-1.0)  C(54)=0.5-(1.11*SQRT(C(50)*C(50)+4.0)+2.0)/
     1(4.0*(C(50)+2.0))
      IF (C(55).EQ.-1.0)  C(55)=0.0065
      IF (C(56).EQ.-1.0)  C(56)=C(51)*C(48)
      IF (C(57).EQ.-1.0)  C(57)=1119.0*C(1)**3.0/C(7)-0.335/C(9)
      IF (C(58).NE.-1.0)  GO TO 50
      IF (C(1).GT.0.28)  C(58)=(7.8-56350.0*(C(1)-0.28)**2.75)*1.0E-05
      IF (C(1).LE.0.28)  C(58)=7.8E-05
   50 CONTINUE
      IF (C(59).EQ.-1.0)  C(59)= C(57)*(0.0822*C(1)-0.02162)
      IF (C(60).EQ.-1.0)  C(60)=C(2)*0.025
      IF (C(61).EQ.-1.0)  C(61)=0.333*C(36)
      IF (C(14).EQ.-1.0)  C(14)=C(51)
      IF (C(18).EQ.-1.0)  C(18)=2.1*C(56)
      C(72)=C(16)+C(17)+C(18)
      RETURN
C
      END
```

```
      SUBROUTINE LAMC (C,ROB,AEL,AEDL)
      DIMENSION B3(7),BB3(7),XB3(7),C(50),ROB(11)
      DIMENSION ROBO(1),AEL(40),ATEN(1),ALD(1),AEDL(40)
      COMMON U,Z3,QL,RO
      COMMON XB3,B3
      Z3=C(35)
      RO=C(12)
      U=1.0
      QL=C(2)
      B3(6)=0.0
      DO 10 I=1,5
      XB3(I)=C(30+I)
      B3(I)=C(35+I)
   10 BB3(I)=B3(I)**2
      CALL YN (1.0,DYV,DNV)
      A2=RO*QL*QL/2.0
      A3=A2*QL
      DYV=DYV/A2
      DNV=DNV/A3
      ROBO(1)=C(41)
      CALL EVALDK (11,1,ROB,ROBO,ATEN,AEL)
      CALL EVALDK (11,1,ROB,ROBO,ALD,AEDL)
      IF (C(42).EQ.-1.0) C(42)=ATEN(1)*DYV*(-1.0)
      IF (C(43).EQ.-1.0) C(43)=ALD(1)
      IF (C(29).EQ.-1.0) C(29)=(1.0-DNV/DYV)*C(35)
      RETURN
C
      END
      FUNCTION BD(X)
      DIMENSION XB3(7),B3(7)
      COMMON U,Z3,QL,RO
      COMMON XB3,B3
      DO 80 I=1,4
      J=5-I
      IF (X .GT. XB3(J)) GO TO 90
   80 CONTINUE
```

```
90      BD=B3(J)+(B3(J+1)-B3(J))*(X-XB3(J))/(XB3(J+1)-XB3(J))
        IF (ABS(X).LT.0.0001) DB=B3(1)
        RETURN
        END
        FUNCTION BB(X)
        BB=BD(X)**2
        RETURN
        END
        SUBROUTINE SIMP(QQ,S,N,TGR)
        DIMENSION QQ(31)
        DELTA=S/(N-1)
        TGR=QQ(1)+4.*QQ(N-1)+QQ(N)
         NT=(N-3)/2
        DO 10 I=1,NT
        II=2*I
 10     TGR=TGR+4.*QQ(II)+2.*QQ(II+1)
        TGR=TGR*DELTA/3.0
        RETURN
        END
        FUNCTION DBB(X)
        SN=SIGN(1.0,X)
10      DBB=(BB(X+.01*SN)-BB(X))/(.01*SN)
        RETURN
        END
        SUBROUTINE YN (V,QY,QN)
        DIMENSION QQ(31),QQQ(31)
        COMMON U,Z3,QL,RO
        DO 30 I=1,31
        QX=(Z3/30.0)*(I-1)
        IF (QX.LT.0.00001) QX=0.00001
        QQ(I)=-U*DBB(QX)*V
   30   QQQ(I)=QX*QQ(I)
        CALL SIMP(QQ,Z3,31,TY3)
        CALL SIMP(QQQ,Z3,31,TN3)
        QY=-3.1416*RO*TY3/2.0
        QN=-3.1416*RO*TN3/2.0
```

```
      RETURN
C
      END
```

```
      SUBROUTINE CALCN (A,Y,D)
      REAL*8 A
      DIMENSION A(5,5),Y(15),D(15,4)
C
C     CLEAR A ARRAY
C
      DO 1 I=1,4
      DO 1 J=1,5
    1 A(I,J)=0.0
C
C     COMPUTE NON-ZERO ELEMENTS OF A
C
      DO 10 I=1,4
      A(1,I)=D(1,I)+D(2,I)+D(3,I)+D(4,I)
      A(2,I)= D(5,I)+D(6,I)+D(7,I)
      A(3,I)=D(10,I)+D(11,I)+D(12,I)+D(13,I)
   10 A(4,I)=D(8,I)+D(9,I)+D(14,I)+D(15,I)
      A(1,5)=-Y(1)-Y(2)-Y(3)-Y(4)
      A(2,5)=-Y(5)-Y(6)-Y(7)
      A(3,5)=-Y(10)-Y(11)-Y(12)-Y(13)
      A(4,5)=-Y(8)-Y(9)-Y(14)-Y(15)
      RETURN
C
      END
```

```
      FUNCTION SIMUL( N,A,X,EPS,INDIC,NRC)
      IMPLICIT REAL*8(A-H,O-Z)
      REAL*8 A,X,EPS,SIMUL
      DIMENSION IROW(50),JCOL(50),JORD(50),Y(50),A(NRC,NRC),X(N)
C
      MAX=N
      IF (INDIC.GE.0) MAX=N+1
C
C     IS N LARGER THAN 50
C
      IF (N.LE.50) GO TO 5
      WRITE (6,200)
      SIMUL=0.0
      RETURN
C
C     BEGIN ELIMINATION PROCEDURE
C
    5 DETER=1.0
      DO 18 K=1,N
      KM1=K-1
C
C     SEARCH FOR THE PIVOT ELEMENT
C
      PIVOT=0.0
      DO 11 I=1,N
      DO 11 J=1,N
C
C     SCAN IROW AND JCOL ARRAYS FOR INVALID PIVOT SUBSCRIPTS
C
      IF (K.EQ.1) GO TO 9
      DO 8 ISCAN=1,KM1
      DO 8 JSCAN=1,KM1
      IF (I.EQ.IROW(ISCAN)) GO TO 11
      IF (J.EQ.JCOL(JSCAN)) GO TO 11
    8 CONTINUE
    9 IF (DABS(A(I,J)).LE.DABS(PIVOT)) GO TO 11
```

```
      PIVOT=A(I,J)
      IROW(K)=I
      JCOL(K)=J
   11 CONTINUE
C
C     INSURE THAT SELECTED PIVOT IS LARGER THAN EPS
C
      IF (DABS(PIVOT).GT.EPS) GO TO 13
      SIMUL=0.0
      RETURN
C
C     UPDATE THE DETERMINANT VALUE
C
   13 IROWK=IROW(K)
      JCOLK=JCOL(K)
      DETER=DETER*PIVOT
C
C     NORMALIZE PIVOT ROW ELEMENTS
C
      DO 14 J=1,MAX
   14 A(IROWK,J)=A(IROWK,J)/PIVCT
C
C     CARRY OUT ELIMINATION AND DEVELOPE INVERSE
C
      A(IROWK,JCOLK)=1.0/PIVOT
      DO 18 I=1,N
      AIJCK=A(I,JCOLK)
      IF (I.EQ.IROWK) GO TO 18
      A(I,JCOLK)=-AIJCK/PIVOT
      DO 17 J=1,MAX
   17 IF (J.NE.JCOLK) A(I,J)=A(I,J)-AIJCK*A(IROWK,J)
   18 CONTINUE
C
C     ORDER SOLUTION VALUES (IF ANY) AND CREATE JORD ARRAY
C
      DO 20 I=1,N
```

```
      IROWI=IROW(I)
      JCOLI=JCOL(I)
      JORD(IROWI)=JCOLI
   20 IF (INDIC.GE.0) X(JCOLI)=A(IROWI,MAX)
C
C     ADJUST SIGN OF DETERMINANT
C
      INTCH=0
      NM1=N-1
      DO 22 I=1,NM1
      IP1=I+1
      DO 22 J=IP1,N
      IF (JORD(J).GE.JORD(I)) GO TO 22
      JTEMP=JORD(J)
      JORD(J)=JORD(I)
      JORD(I)=JTEMP
      INTCH=INTCH+1
   22 CONTINUE
      IF (INTCH/2*2.NE.INTCH) DETER=-DETER
C
C     IF INDIC IS POSITIVE RETURN WITH RESULTS
C
      IF (INDIC.LE.0) GO TO 26
      SIMUL=DETER
      RETURN
C
C     IF INDIC IS NEGATIVE OR ZERO, UNSCRAMBLE THE INVERSE
C     FIRST BY ROWS
C
   26 DO 28 J=1,N
      DO 27 I=1,N
      IROWI=IROW(I)
      JCOLI=JCOL(I)
   27 Y(JCOLI)=A(IROWI,J)
      DO 28 I=1,N
   28 A(I,J)=Y(I)
```

```
C
C      THEN BY COLUMNS
C
       DO 30 I=1,N
       DO 29 J=1,N
       IROWJ=IROW(J)
       JCOLJ=JCOL(J)
   29  Y(IROWJ)=A(I,JCOLJ)
       DO 30 J=1,N
   30  A(I,J)=Y(J)
C
C      RETURN FOR INDIC NEGATIVE OR ZERO
C
       SIMUL=DETER
       RETURN
C
C      FORMAT FOR OUTPUT STATEMENT
C
  200  FORMAT ( 10HON TOO BIG )
C
       END
```

```
      SUBROUTINE UGLYDK(NIN,NCL,NCR,XIN,YIN,ESL,ESR,AE)
C     APRIL 1975 DUCK SRIES    J.E.KERWIN
      DIMENSION XIN(1),YIN(1),AE(1),H(30),D(30),A(900),S(30)
      DATA HALF/0.5E00/,TWO/2.0E00/,SIX/6.0E00/,RAD/1.745329E-02/        PBS10355
      NM1=NIN-1                                                          PBS10356
      NM2=NM1-1                                                          PBS10357
      NM3=NM2-1
      NEQ=NM2                                                            PBS10358
      DO 1 N=1,NM1                                                       PBS10359
      H(N)=XIN(N+1)-XIN(N)                                               PBS10360
    1 D(N)=(YIN(N+1)-YIN(N))/H(N)                                        PBS10361
      IF(NCL.EQ.2) NEQ=NEQ+1
      IF(NCR.EQ.2) NEQ=NEQ+1
      NSQ=NEQ**2
      DO 4 N=1,NSQ                                                       PBS10367
    4 A(N)=0.0                                                           PBS10368
      J=1                                                                PBS10369
      L=1                                                                PBS10370
      IF(NCL.LT.2) GO TO 6
      A(1)=TWO*H(1)                                                      PBS10372
      A(2)=H(1)                                                          PBS10373
      SLP=ESL*RAD                                                        PBS10374
      S(1)=(D(1)-TAN(SLP))*SIX
      J=J+1                                                              PBS10376
      L=L+NEQ+1
      A(L-1)=H(1)
    6 DO 5 N=1,NM2                                                       PBS10380
      IF(N.GT.1) A(L-1)=H(N)                                             PBS10381
      A(L)=TWO*(H(N)+H(N+1))                                             PBS10382
      IF(N.LT.NM2) A(L+1)=H(N+1)                                         PBS10383
      IF(N.EQ.2.AND.NCL.EQ.1) A(L-1)=A(L-1)-H(N)**2/H(N+1)
      IF(N.EQ.1.AND.NCL.EQ.1) A(L)=A(L)+(1.0+H(N)/H(N+1))*H(N)
      IF(N.EQ.NM2.AND.NCR.EQ.1) A(L)=A(L)+(1.0+H(N+1)/H(N))*H(N+1)
      IF(N.EQ.NM3.AND.NCR.EQ.1) A(L+1)=A(L+1)-H(N+2)**2/H(N+1)
      S(J)=(D(N+1)-D(N))*SIX                                             PBS10384
      J=J+1                                                              PBS10385
```

```
5     L=L+NEQ+1                                                    PBS10386
      IF(NCR.LT.2) GO TO 7
      A(L-1)=H(NM1)                                                PBS10388
      A(L)=-TWO*H(NM1)                                             PBS10389
      L=L-NEQ                                                      PBS10390
      A(L)=-H(NM1)                                                 PBS10391
      SLP=ESR*RAD                                                  PBS10392
      S(J)=(D(NM1)+TAN(SLP))*SIX
7     CALL SIMQ(A,S,NEQ,KERROR)
      HOLD=S(NEQ)
      IF(NCL.EQ.2) GO TO 8
      DO 9 N=1,NM2                                                 PBS10396
      M=NM2-N+2                                                    PBS10397
9     S(M)=S(M-1)                                                  PBS10398
      IF(NCL.EQ.0) S(1)=0.0
      BUG=H(1)/H(2)
      IF(NCL.EQ.1) S(1)=(1.0+BUG)*S(2)-BUG*S(3)
8     IF(NCR.EQ.0) S(NIN)=0.0
      BUG=H(NM1)/H(NM2)
      IF(NCR.EQ.1) S(NIN)=(1.0+BUG)*S(NM1)-BUG*S(NM2)
      IF(NCR.EQ.2) S(NIN)=HOLD
      DO 10 N=1,NM1                                                PBS10401
      AE(N)=(S(N+1)-S(N))/(SIX*H(N))                               PBS10402
      M=N+NM1
      AE(M)=HALF*S(N)
      M=M+NM1
      AE(M)=D(N)-H(N)*(TWO*S(N)+S(N+1))/SIX
      M=M+NM1
10    AE(M)=YIN(N)
      RETURN
      END
```

```
      SUBROUTINE SIMQ(A,B,N,KS)                                        SIMQ 490
      DIMENSION A(1),B(1)
      TOL=0.0                                                          SIMQ 540
      KS=0                                                             SIMQ 550
      JJ=-N                                                            SIMQ 560
      DO 65 J=1,N                                                      SIMQ 570
      JY=J+1                                                           SIMQ 580
      JJ=JJ+N+1                                                        SIMQ 590
      BIGA=0                                                           SIMQ 600
      IT=JJ-J                                                          SIMQ 610
      DO 30 I=J,N                                                      SIMQ 620
      IJ=IT+I                                                          SIMQ 660
      IF(ABS(BIGA)-ABS(A(IJ))) 20,30,30
   20 BIGA=A(IJ)                                                       SIMQ 680
      IMAX=I                                                           SIMQ 690
   30 CONTINUE                                                         SIMQ 700
      IF(ABS(BIGA)-TOL) 35,35, 40
   35 KS=1                                                             SIMQ 750
      RETURN                                                           SIMQ 760
   40 I1=J+N*(J-2)                                                     SIMQ 800
      IT=IMAX-J                                                        SIMQ 810
      DO 50 K=J,N                                                      SIMQ 820
      I1=I1+N                                                          SIMQ 830
      I2=I1+IT                                                         SIMQ 840
      SAVE=A(I1)                                                       SIMQ 850
      A(I1)=A(I2)                                                      SIMQ 860
      A(I2)=SAVE                                                       SIMQ 870
   50 A(I1)=A(I1)/BIGA                                                 SIMQ 910
      SAVE=B(IMAX)                                                     SIMQ 920
      B(IMAX)=B(J)                                                     SIMQ 930
      B(J)=SAVE/BIGA                                                   SIMQ 940
      IF(J-N) 55,70,55                                                 SIMQ 980
   55 IQS=N*(J-1)                                                      SIMQ 990
      DO 65 IX=JY,N                                                    SIMQ1000
      IXJ=IQS+IX                                                       SIMQ1010
      IT=J-IX                                                          SIMQ1020
```

```
      DO 60 JX=JY,N                                                  SIMQ1030
      IXJX=N*(JX-1)+IX                                               SIMQ1040
      JJX=IXJX+IT                                                    SIMQ1050
   60 A(IXJX)=A(IXJX)-(A(IXJ)*A(JJX))                                SIMQ1060
   65 B(IX)=B(IX)-(B(J)*A(IXJ))                                      SIMQ1070
   70 NY=N-1                                                         SIMQ1110
      IT=N*N                                                         SIMQ1120
      DO 80 J=1,NY                                                   SIMQ1130
      IA=IT-J                                                        SIMQ1140
      IB=N-J                                                         SIMQ1150
      IC=N                                                           SIMQ1160
      DO 80 K=1,J                                                    SIMQ1170
      B(IB)=B(IB)-A(IA)*B(IC)                                        SIMQ1180
      IA=IA-N                                                        SIMQ1190
   80 IC=IC-1                                                        SIMQ1200
      RETURN                                                         SIMQ1210
      END
```

```
      SUBROUTINE EVALDK(NIN,NOUT,XIN,XOUT,YOUT,A)
C     APRIL 1975 SPLINE PROGRAM SERIES   J.E.KERWIN
      DIMENSION XIN(1),XOUT(1),YOUT(1),A(1)
      NM1=NIN-1
      MOUT=IABS(NOUT)
      IF(NOUT.GT.0) GO TO 1
      DEL=(XIN(NIN)-XIN(1))/(MOUT-1)
      DO 2 N=1,MOUT
    2 XOUT(N)=XIN(1)+(N-1)*DEL
    1 J=1
      DO 3 N=1,MOUT
      IF(XOUT(N).GE.XIN(2)) GO TO 4
      J=1
      GO TO 5
    4 IF(XOUT(N).LT.XIN(NM1)) GO TO 6
      J=NM1
      GO TO 5
    6 IF(XOUT(N).GE.XIN(J+1)) GO TO 7
    9 IF (XOUT(N).LT.XIN(J)) GO TO 8
    5 H1=XOUT(N)-XIN(J)
      H2=H1**2
      H3=H1*H2
      J2=J+NM1
      J3=J2+NM1
      J4=J3+NM1
      YOUT(N)=A(J)*H3+A(J2)*H2+A(J3)*H1+A(J4)
      GO TO 3
    7 J=J+1
      GO TO 6
    8 J=J-1
      GO TO 9
    3 CONTINUE
      RETURN
      END
```

```
      SUBROUTINE SAIL (XOLD,AXOLD,VT,GAMMA,C,Y,AY,KVA,DBETTA,BIN,AEA)
      REAL KVA,LIFT,LIFT2
      DIMENSION XOLD(4),AXOLD(4),C(100),Y(15),AY(15,4),BIN(21),AEA(80)
      DIMENSION ALPHA(2),BOUT(2)
C
C     COMPUTE APPARENT WIND, VA, AND APPARENT WIND ANGLE, BETTA
C
      PI=3.141593
      ICT=0
      VT1=0.55*VT
    1 CONTINUE
      VTCG=VT1*COS(GAMMA)
      VTSG=VT1*SIN(GAMMA)
      VASQ=(XOLD(1)+VTCG)**2+VTSG**2
      AVASQ=(AXOLD(1)+VTCG)**2+VTSG**2
      BETTA=ABS(ATAN2(VTSG,(XOLD(1)+VTCG)))
      ABETTA=ABS(ATAN2(VTSG,(AXOLD(1)+VTCG)))
      IF (ICT.EQ.1) GO TO 10
C
C     HULL AERO FORCES
C
      BOUT(1)= BETTA
      BOUT(2)=ABETTA
      CALL EVALDK (21,2,BIN,BOUT,ALPHA,AEA)
      FH=0.001428*VASQ*(C(24)*SIN(BETTA)**2+0.3*C(25)*COS(BETTA)**2)
     1/COS(ALPHA(1)-BETTA)
      AFH=0.001428*AVASQ*(C(24)*SIN(ABETTA)**2+0.3*C(25)*COS(ABETTA)**2)
     1/COS(ALPHA(2)-ABETTA)
      YMH=FH*C(2)*(0.2+0.17819*BETTA)*SIN(ALPHA(1))
      AYMH=AFH*C(2)*(0.2+0.17819*ABETTA)*SIN(ALPHA(2))
      ICT=1
      VT1=VT
      GO TO 1
C
C     SAIL FORCES
C
```

```
10 CONTINUE
   KVA=SQRT(VASQ)/1.689
   DBETTA=BETTA*57.2958
   BETTAO=BETTA
   ABETAO=ABETTA
   VASQO=VASQ
   AVASQO=AVASQ
   VASQ=VASQO*((COS(XOLD(2))*SIN(BETTAO))**2+COS(BETTAO)**2)
   AVASQ=AVASQO*((COS(XOLD(2))*SIN(ABETAO))**2+COS(ABETAO)**2)
   VASQ2=VASQO*((COS(AXOLD(2))*SIN(BETTAO))**2+COS(BETTAO)**2)
   BETTA=ATAN2(COS(XOLD(2))*SIN(BETTAO),COS(BETTAO))
   ABETTA=ATAN2(COS(XOLD(2))*SIN(ABETAO),CCS(ABETAO))
   BETTA2=ATAN2(COS(AXOLD(2))*SIN(BETTAO),COS(BETTAO))
   Q=C(30)/2.0*VASQ
   AQ=C(30)/2.0*AVASQ
   Q2=C(30)/2.0*VASQ2
   LIFT=C(19)*Q*C(3)
   ALIFT=C(19)*AQ*C(3)
   LIFT2=C(19)*Q2*C(3)
   DRAG=(C(20)*C(21)+C(22)*C(3))*Q+C(23)*LIFT**2
  1/Q/C(3)
   ADRAG=(C(20)*C(21)+C(22)*C(3))*AQ+C(23)*ALIFT**2/AQ/C(3)
   DRAG2=(C(20)*C(21)+C(22)*C(3))*Q2+C(23)*LIFT2**2
  1/Q2/C(3)
   IF (BETTA.LE.1.57) GO TO 20
   IF(C(28).NE.0.0) GO TO 11
   LIFT=LIFT*COS(BETTA-1.57)
   ALIFT=ALIFT*COS(ABETTA-1.57)
   LIFT2=LIFT2*COS(BETTA2-1.57)
   GO TO 15
11 LIFT=LIFT/C(19)*C(28)
   ALIFT=ALIFT/C(19)*C(28)
   LIFT2=LIFT2/C(19)*C(28)
15 CONTINUE
   IF (C(28).NE.0.0) GO TO 17
   DRAG=DRAG+(1.2*Q*C(3)-DRAG)*SIN(BETTA-1.57)
```

```
      ADRAG=ADRAG+(1.2*AQ*C(3)-ADRAG)*SIN(ABETTA-1.57)
      DRAG2=DRAG2+(1.2*Q2*C(3)-DRAG2)*SIN(BETTA2-1.57)
      GO TO 20
   17 DRAG=C(27)*Q*C(3)
      ADRAG=C(27)*AQ*C(3)
      DRAG2=C(27)*Q2*C(3)
   20 CONTINUE
C
C     COMPUTE AERO DRIVING FORCES
C
      Y(1)=(LIFT*SIN(BETTA)-DRAG*COS(BETTA))
     1-FH*COS(ALPHA(1))
      AY(1,1)=(ALIFT*SIN(ABETTA)-ADRAG*COS(ABETTA))
     1-AFH*COS(ALPHA(2))
      AY(1,2)=LIFT2*SIN(BETTA2)-DRAG2*COS(BETTA2)
     1-FH*COS(ALPHA(1))
      AY(1,3)=Y(1)
      AY(1,4)=Y(1)
C
C     COMPUTE AERO SIDE FORCE, Y(5)
C
      Y(5)=(LIFT*COS(BETTA)+DRAG*SIN(BETTA))
     1*COS(XOLD(2))+FH*SIN(ALPHA(1))
      AY(5,1)=(ALIFT*COS(ABETTA)+ADRAG*SIN(ABETTA))
     1*COS(XOLD(2))+AFH*SIN(ALPHA(2))
      AY(5,2)=(LIFT2*COS(BETTA2)+DRAG2*SIN(BETTA2))
     1*COS(AXOLD(2))+FH*SIN(ALPHA(1))
      AY(5,3)=Y(5)
      AY(5,4)=Y(5)
C
C     COMPUTE AERO HEELING MOMENT, Y(8)
C     C(4)=DISTANCE BETWEEN CE SAIL AND CE HULL
C
      Y(8)=(LIFT*COS(BETTA)+DRAG*SIN(BETTA))
     1*C(4)
      AY(8,1)=(ALIFT*COS(ABETTA)+ADRAG*SIN(ABETTA))
```

```
     1*C(4)
      AY(8,2)=(LIFT2*COS(BETTA2)+DRAG2*SIN(BETTA2))
     1*C(4)
      AY(8,3)=Y(8)
      AY(8,4)=Y(8)
C
C     COMPUTE YAWING MOMENT DUE TO EARO SIDE FORCES
C
      Y(10)=(Y(5)-FH*SIN(ALPHA(1)))*C(26)+YMH
      AY(10,1)=(AY(5,1)-AFH*SIN(ALPHA(2)))*C(26)+AYMH
      AY(10,2)=(AY(5,2)-FH*SIN(ALPHA(1)))*C(26)+YMH
      AY(10,3)=Y(10)
      AY(10,4)=Y(10)
C
C     COMPUTE SAIL YAWING MOMENT, Y(11)
C     C(5)= DISTANCE FROMCE SAIL TO CENTER OF RESISTANCE
C
      Y(11)=C(5)*Y(1)*SIN(XOLD(2))
      AY(11,1)=C(5)*AY(1,1)*SIN(XOLD(2))
      AY(11,2)=C(5)*AY(1,2)*SIN(AXOLD(2))
      AY(11,3)=Y(11)
      AY(11,4)=Y(11)
      RETURN
C
      END
```

```
      SUBROUTINE HULL (XOLD,AXOLD,C,Y,AY,AE1,AE2,AE3,AEP,XIN)
      DIMENSION XOLD(4),AXOLD(4),C(100),Y(15),AY(15,4)
      DIMENSION AE1(44),AE2(44),AE3(44),AEP(44),XIN(11)
      DIMENSION SLR(2),F1(2),F2(2),F3(2),CPOP(2)
      DIMENSION CFCP(2),CFLH(2),CFLCB(2),DWAVE(2),REFB(2),REKL(2)
      DIMENSION RERD(2),VS(2)
      DIMENSION CFFB(2),CFKL(2),CFRD(2),DFRIC(2)
      SLR(1)=XOLD(1)/1.689/C(2)**0.5
      SLR(2)=AXOLD(1)/1.689/C(2)**0.5
      CALL EVALDK (11,2,XIN,SLR,F1,AE1)
      CALL EVALDK (11,2,XIN,SLR,F2,AE2)
      CALL EVALDK (11,2,XIN,SLR,F3,AE3)
      CALL EVALDK (11,2,XIN,SLR,CPOP,AEP)
      VS(1)=XOLD(1)
      VS(2)=AXOLD(1)
C
C     COMPUTE WAVE RESISTANCE
C
      DO 2 I=1,2
      CFCP(I)=F2(I)*(ABS((C(8)-CPOP(I))*100.0))**1.7
      CFLH(I)=-F3(I)*(16.0-C(9))
      CFLCB(I)=SIN(1.57*SLR(I))*(ABS(62.5-17.5*C(8)-C(10)))**3/100.0
      DWAVE(I)=F1(I)*(C(2)/100.0)**3*C(7)*C(7)*(1.0+CFCP(I)+CFLH(I)
     1+CFLCB(I))
C
C     COMPUTE FRICTIONAL RESISTANCE
C
      REFB(I)=C(2)*VS(I)/C(11)
      REKL(I)=C(13)*VS(I)/C(11)
      RERD(I)=C(14)*VS(I)/C(11)
      IF (REFB(I).LE.0.0) REFB(I)=1.0
      IF (REKL(I).LE.0.0) REKL(I)=1.0
      IF (RERD(I).LE.0.0) RERD(I)=1.0
      CFFB(I)=0.075/(ALOG10(REFB(I))-2.0)**2+C(15)
      CFKL(I)=0.075/(ALOG10(REKL(I))-2.0)**2
      CFRD(I)=0.075/(ALOG10(RERD(I))-2.0)**2
```

```
      DFRIC(I)=C(12)/2.0*VS(I)**2*(CFFB(I)*C(16)+CFKL(I)*C(17)+CFRD(I)
     1*C(18))
    2 CONTINUE
      Y(2)=-ABS((DWAVE(1)+DFRIC(1))/COS(XOLD(2)))
C
C     COMPUTE AUGMENTED FORCES
C
      AY(2,1)=-ABS((DWAVE(2)+DFRIC(2))/COS(XOLD(2)))
      AY(2,2)=-ABS((DWAVE(1)+DFRIC(1))/COS(AXOLD(2)))
      AY(2,3)=Y(2)
      AY(2,4)=Y(2)
      RETURN
C
      END
```

```
      SUBROUTINE RUDDR (XOLD,AXOLD,C,Y,AY)
      DIMENSION XOLD(4),AXOLD(4),C(100),Y(15),AY(15,4)
      A=XOLD(4)/57.3
      AA=AXOLD(4)/57.3
      X3=XOLD(3)/57.3
      XX3=AXOLD(3)/57.3
      CL=C(52)*XOLD(4)+C(53)/C(50)*A**2
      CL4=C(52)*AXOLD(4)+C(53)/C(50)*A**2
      CD=C(55)+CL**2/(2.827*C(50))+0.0166*CL**2
      CD4=C(55)+CL4**2/(2.827*C(50))+0.0166*CL4**2
      Q=0.5*C(12)*XOLD(1)**2*C(56)
      AQ=0.5*C(12)*AXOLD(1)**2*C(56)
C
C     COMPUTE RUDDER SIDE FORCE,Y(7)
C
      FAC=CL*COS(X3)-CD*SIN(X3)
      Y(7)=-FAC*Q*COS(XOLD(2))
      AY(7,1)=-FAC*AQ*COS(XOLD(2))
      AY(7,2)=-FAC*Q*COS(AXOLD(2))
      AY(7,3)=-(CL*COS(XX3)-CD*SIN(XX3))*Q*COS(XOLD(2))
      AY(7,4)=-(CL4*COS(X3)-CD4*SIN(X3))*Q*COS(XOLD(2))
C
C     COMPUTE RUDDER DRAG, Y(4)
C
      FAC=CL*SIN(X3)+CD*COS(X3)
      Y(4)=-FAC*Q
      AY(4,1)=-FAC*AQ
      AY(4,2)=Y(4)
      AY(4,3)=-(CL*SIN(XX3)+CD*COS(XX3))*Q
      AY(4,4)=-(CL4*SIN(X3)+CD4*COS(X3))*Q
C
C     COMPUTE YAWING MOMENT FROM RUDDER, Y(13)
C
      CN=CL*COS(A)+CD*SIN(A)
      CN4=CL4*COS(AA)+CD4*SIN(AA)
      CM=(0.25-C(54))*C(52)-0.5*C(53)/C(50)*A**2
```

```
      CM4=(0.25-C(54))*C(52)-0.5*C(53)/C(50)*AA**2
      IF (CN.LT.0.0001) CN=0.0001
      CP=-CM/CN*C(51)
      IF (CN4.LT.0.0001) CN4=0.0001
      CP4=-CM4/CN4*C(51)
      Y(13)=Y(7)*(C(6)+CP)
      AY(13,1)=AY(7,1)*(C(6)+CP)
      AY(13,2)=AY(7,2)*(C(6)+CP)
      AY(13,3)=AY(7,3)*(C(6)+CP)
      AY(13,4)=AY(7,4)*(C(6)+CP4)
C
C     COMPUTE HEELING MOMENT FROM RUDDER
C
      CPS=(0.4244*CL*COS(A)+CD*SIN(A))/CN*C(48)
      CPS4=(0.4244*CL4*COS(AA)+CD4*SIN(AA))/CN4*C(48)
      Y(15)=CL*Q*(C(45)+CPS)
      AY(15,1)=CL*AQ*(C(45)+CPS)
      AY(15,2)=Y(15)
      AY(15,3)=Y(15)
      AY(15,4)=CL4*Q*(C(45)+CPS)
      RETURN
C
      END
```

```
      SUBROUTINE KEEL (XOLD,AXOLD,C,Y,AY)
      DIMENSION XOLD(4),AXOLD(4),C(100),Y(15),AY(15,4)
      Q=C(12)*(XOLD(1)*COS(XOLD(2)))**2/2.0
      Q1=C(12)*(AXOLD(1)*COS(XOLD(2)))**2/2.0
      Q2=C(12)*(XOLD(1)*COS(AXOLD(2)))**2/2.0
      XL=C(42)*Q*XOLD(3)/57.3*C(2)**2
      XL1=C(42)*Q1*XOLD(3)/57.3*C(2)**2
      XL2=C(42)*Q2*XOLD(3)/57.3*C(2)**2
      XL3=C(42)*Q*AXOLD(3)/57.3*C(2)**2
C
C     COMPUTE KEEL SIDE FORCE, Y(6)
C
      Y(6)=-XL
      AY(6,1)=-XL1
      AY(6,2)=-XL2
      AY(6,3)=-XL3
      AY(6,4)=Y(6)
C
C     COMPUTE INDUCED KEEL DRAG , Y(3)
C
      Y(3)=-XL*XOLD(3)/57.3/C(43)/COS(XOLD(2))**2
      AY(3,1)=-XL1*XOLD(3)/57.3/C(43)/COS(XOLD(2))**2
      AY(3,2)=-XL2*XOLD(3)/57.3/C(43)/COS(AXOLD(2))**2
      AY(3,3)=-XL3*AXOLD(3)/57.3/C(43)/COS(XOLD(2))**2
      AY(3,4)=Y(3)
C
C     COMPUTE MOMENT DUE TO KEEL SIDE FORCE, Y(12)
C
      Y(12)=C(29)*Y(6)
      AY(12,1)=C(29)*AY(6,1)
      AY(12,2)=C(29)*AY(6,2)
      AY(12,3)=C(29)*AY(6,3)
      AY(12,4)=Y(12)
C
C     COMPUTE HEELING MOMENT
C
```

```
      Y(14)=C(61)*Y(6)/COS(XOLD(2))*(-1.0)
      AY(14,1)=C(61)*AY(6,1)/COS(XOLD(2))*(-1.0)
      AY(14,2)=C(61)*AY(6,2)/COS(AXOLD(2))*(-1.0)
      AY(14,3)=C(61)*AY(6,3)/COS(XOLD(2))*(-1.0)
      AY(14,4)=Y(14)
      RETURN
C
      END
```

```
      SUBROUTINE RTMOM (XOLD,AXOLD,C,Y,AY)
      DIMENSION XOLD(4),AXOLD(4),C(100),Y(15),AY(15,4)
C
C     COMPUTE HYDROSTATIC RIGHTING MOMENT
C
C     C(1) = BWL / LWL
C     C(2) = LWL
      FAC=-0.00224*C(7)*C(2)**4.0
      FN=XOLD(1)/SQRT(32.2*C(2))
      FN1=AXOLD(1)/SQRT(32.2*C(2))
      Y(9)=FAC*XOLD(2)*(C(57)+C(58)*FN+C(59)*XOLD(2))
     1+C(60)*SIN(XOLD(2))
C
C     COMPUTE AUGMENTED FORCES
C
      AY(9,1)=FAC*XOLD(2)*(C(57)+C(58)*FN1+C(59)*XOLD(2))
     1+C(60)*SIN(XOLD(2))
      AY(9,2)=FAC*AXOLD(2)*(C(57)+C(58)*FN+C(59)*AXOLD(2))
     1+C(60)*SIN(AXOLD(2))
      AY(9,3)=Y(9)
      AY(9,4)=Y(9)
      RETURN
C
      END
```

## 8.3 Example Output

Two example computer outputs are listed in this section. The first is the yacht Antiope and the second is the model generated sailing boat which is produced if all geometric parameters are defaulted.

```
ITMAX  =        10
IPRINT =         0
N      =         4
EPS1   =         1.0D-10
EPS2   =         1.0E-02
```

XOLD(1)...XOLD( 4)

1.000000E 01  0.000000E-01  0.000000E-01  0.000000E-01

SOLUTIONS ARE COMPUTED FOR THE FOLLOWING TRUE WIND SPEEDS (KNOTS)

5.00000  7.50000  10.00000

SOLUTIONS ARE COMPUTED FOR THE FOLLOWING TRUE WIND ANGLES FOR EACH WIND SPEED

180.00000 160.00000 140.00000 120.00000 100.00000 80.00000 60.00000 45.00000 35.00000

```
LWL=     24.30000
DISPLACEMENT TO LENGTH=    180.39990
PRISMATIC=      0.53000
L/H=     12.15000
LCB=     53.50000
KINEMATIC VISCOSITY=    0.1279100E-04
DENSITY OF WATER=       1.99000
MEAN KEEL CHORD=       7.12500
MEAN RUDDER CHORD=      0.00000
ROUGHNESS AND CORRELATION FACTOR=       0.00000
FAIRBODY WETTED SURFACE=    118.61000
KEEL WETTED SURFACE=     41.38200
RUDDER WETTED SURFACE=      0.00000
TOTAL WETTED SURFACE=    159.99200
BWL /LWL=       0.23900
SAIL AREA=    400.00000
HEELING MOMENT ARM=     16.27361
PITCHING MOMENT ARM=     17.84613
DISTANCE FROM FP TO RUDDER STOCK=     16.00000
CLOSE HAULED LIFT COEF=      1.25000
RIG FORM DRAG COEF=      0.40000
CROSS SECTIONAL AREA OF RIG=     19.60001
SAIL FRICTIONAL COEF=      0.04000
INDUCED DRAG COEF / LIFT COEF**2=       0.13030
LATERAL AREA OF HULL=    100.00000
TRANSVERSE AREA OF HULL=     27.00000
DISTANCE BETWEEN CE SAIL AND FP=     11.50000
OFF WIND DRAG COEF=      0.00000
```

```
       OFF WIND LIFT COEF=      0.00000
       DISTANCE BETWEEN CE HULL AND FP=     11.35764
       DENSITY OF AIR=      0.00238
       HORIZONTAL DISTANCE FROM MAXIMUM DRAFT OF PROFILE MEASUREMENTS
0.00000   5.75000   8.51000  14.67000  16.91000
       PROFILE MEASUREMENTS
4.65000   4.62000   2.12000   0.78000   0.00000
       DRAFT OF CANOE BODY / TOTAL DRAFT=      0.35000
       HYDRODYNAMIC LIFT COEF=      0.09805
       LAMDA X LIFT / DRAG=      2.06498
       DISTANCE FROM LWL TO VERTICAL HYDRO CE=      1.54845
       *** RUDDER SECTION ***
       DISTANCE FROM LWL TO ROOT CHORD=      0.40000
       ROOT CHORD=      1.82250
       TIP CHORD=      1.21561
       RUDDER SPAN=      3.61250
       SWEEP ANGLE=      0.00000
       ASPECT RATIO=      4.75625
       MEAN CHORD=      1.51905
       DCL / DALPHA=      0.06745
       CROSS FLOW DRAG COEF=      0.56024
       DCM / DCL=      0.21407
       FORM DRAG COEF=      0.00650
       RUDDER AREA=      5.48758
       *** RIGHTING MOMENT SECTION ***
       METACENTRIC HEIGHT / LWL=      0.05711
       FROUDE NUMBER RIGHTING MOMENT COEF=   0.7800000E-04
```

```
NON LINEAR HYDROSTATIC COEF=  -0.1127451E-03
DISTANCE BELOW LWL TO CG=      0.60750
*** SAIL SECTION ***
I=    31.45027          J=     10.48342
P=    28.59114          E=      9.53038
AR FOR TRI=      3.00000          AR MAIN=      3.00000
AR SAIL PLAN=      2.47280
CE SAIL PLAN AFT MAST=      0.40028
FORWARD OVERHANG=     -0.61630
FREEBOARD=      2.75000
```

```
        ---------------------------------------------

        KVT=      5.00000  KNOTS          DGAMMA=    180.00000  DEGREES

        KVA=      2.48617  KNOTS          DBETTA=    179.99980  DEGREES

SUCCESSFUL CONVERGENCE

ITER   =   5

        BOAT SPEED=      2.51383  KNOTS          HEEL ANGLE=      0.00128  DEGREES

        LEEWAY ANGLE=     -0.00390  DEGREES          RUDDER ANGLE=      0.01191DEGREES

        ---------------------------------------------

        ---------------------------------------------

        KVT=      5.00000  KNOTS          DGAMMA=    160.00000  DEGREES

        KVA=      2.60820  KNOTS          DBETTA=    139.03030  DEGREES

SUCCESSFUL CONVERGENCE

ITER   =   2

        BOAT SPEED=      2.72703  KNOTS          HEEL ANGLE=      0.02578  DEGREES

        LEEWAY ANGLE=      0.02088  DEGREES          RUDDER ANGLE=      0.01149DEGREES

        ---------------------------------------------

NO CONVERGENCE

        KVT=      5.00000  KNOTS          DGAMMA=    140.00000  DEGREES

        KVA=      3.24689  KNOTS          DBETTA=     98.17024  DEGREES

SUCCESSFUL CONVERGENCE

ITER   =  11

        BOAT SPEED=      3.36880  KNOTS          HEEL ANGLE=      0.40965  DEGREES

        LEEWAY ANGLE=      0.14458  DEGREES          RUDDER ANGLE=      0.00311DEGREES

        ---------------------------------------------

        KVT=      5.00000  KNOTS          DGAMMA=    120.00000  DEGREES

        KVA=      4.67690  KNOTS          DBETTA=     67.79747  DEGREES

SUCCESSFUL CONVERGENCE
```

```
ITER   =   4
         BOAT SPEED=     4.26724  KNOTS          HEEL ANGLE=     2.74890  DEGREES
         LEEWAY ANGLE=     0.41392  DEGREES          RUDDER ANGLE=     0.19046DEGREES
         ------------------------------------------------
         ------------------------------------------------
         KVT=     5.00000  KNOTS          DGAMMA=   100.00000  DEGREES
         KVA=     6.28702  KNOTS          DBETTA=    51.55513  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
         BOAT SPEED=     4.77718  KNOTS          HEEL ANGLE=     6.77472  DEGREES
         LEEWAY ANGLE=     0.66322  DEGREES          RUDDER ANGLE=     0.66225DEGREES
         ------------------------------------------------
         ------------------------------------------------
         KVT=     5.00000  KNOTS          DGAMMA=    80.00000  DEGREES
         KVA=     7.53630  KNOTS          DBETTA=    40.79662  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
         BOAT SPEED=     4.83670  KNOTS          HEEL ANGLE=    10.99982  DEGREES
         LEEWAY ANGLE=     0.97314  DEGREES          RUDDER ANGLE=     1.19417DEGREES
         ------------------------------------------------
         ------------------------------------------------
         KVT=     5.00000  KNOTS          DGAMMA=    60.00000  DEGREES
         KVA=     8.15836  KNOTS          DBETTA=    32.05679  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
         BOAT SPEED=     4.41289  KNOTS          HEEL ANGLE=    13.76510  DEGREES
         LEEWAY ANGLE=     1.54980  DEGREES          RUDDER ANGLE=     1.49892DEGREES
         ------------------------------------------------
```

```
        ------------------------------------------------
        KVT=      5.00000  KNOTS          DGAMMA=    45.00000  DEGREES
        KVA=      7.97554  KNOTS          DBETTA=    26.31445  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
        BOAT SPEED=      3.61350  KNOTS          HEEL ANGLE=    13.57446  DEGREES
        LEEWAY ANGLE=      2.49007  DEGREES          RUDDER ANGLE=     1.52272DEGREES
        ------------------------------------------------
        ------------------------------------------------
        KVT=      5.00000  KNOTS          DGAMMA=    35.00000  DEGREES
        KVA=      7.44743  KNOTS          DBETTA=    22.64893  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
        BOAT SPEED=      2.77712  KNOTS          HEEL ANGLE=    12.01359  DEGREES
        LEEWAY ANGLE=      3.95441  DEGREES          RUDDER ANGLE=     1.51425DEGREES
        ------------------------------------------------
        ------------------------------------------------
        KVT=      7.50000  KNOTS          DGAMMA=   180.00000  DEGREES
        KVA=      3.76861  KNOTS          DBETTA=   179.99980  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
        BOAT SPEED=      3.73182  KNOTS          HEEL ANGLE=     0.00292  DEGREES
        LEEWAY ANGLE=     -0.00395  DEGREES          RUDDER ANGLE=     0.01209DEGREES
        ------------------------------------------------
        ------------------------------------------------
        KVT=      7.50000  KNOTS          DGAMMA=   160.00000  DEGREES
        KVA=      3.97397  KNOTS          DBETTA=   139.79790  DEGREES
SUCCESSFUL CONVERGENCE
```

```
ITER   =   2
         BOAT SPEED=     4.01511  KNOTS          HEEL ANGLE=     0.05447  DEGREES
         LEEWAY ANGLE=     0.01904  DEGREES          RUDDER ANGLE=     0.01699DEGREES
         ---------------------------------------------
         ---------------------------------------------
         KVT=     7.50000  KNOTS          DGAMMA=   140.00000  DEGREES
         KVA=     4.91665  KNOTS          DBETTA=   101.32590  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
         BOAT SPEED=     4.77972  KNOTS          HEEL ANGLE=     0.86860  DEGREES
         LEEWAY ANGLE=     0.13080  DEGREES          RUDDER ANGLE=     0.05872DEGREES
         ---------------------------------------------
         ---------------------------------------------
         KVT=     7.50000  KNOTS          DGAMMA=   120.00000  DEGREES
         KVA=     6.75196  KNOTS          DBETTA=    74.14812  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
         BOAT SPEED=     5.59371  KNOTS          HEEL ANGLE=     4.78607  DEGREES
         LEEWAY ANGLE=     0.28889  DEGREES          RUDDER ANGLE=     0.56792DEGREES
         ---------------------------------------------
         ---------------------------------------------
         KVT=     7.50000  KNOTS          DGAMMA=   100.00000  DEGREES
         KVA=     8.77144  KNOTS          DBETTA=    57.35799  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
         BOAT SPEED=     6.03347  KNOTS          HEEL ANGLE=    11.95808  DEGREES
         LEEWAY ANGLE=     0.35957  DEGREES          RUDDER ANGLE=     1.76328DEGREES
         ---------------------------------------------
```

```
         ----------------------------------------
         KVT=      7.50000  KNOTS          DGAMMA=     80.00000  DEGREES
         KVA=     10.36289  KNOTS          DBETTA=     45.45833  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
         BOAT SPEED=      5.96515  KNOTS          HEEL ANGLE=     19.44243  DEGREES
         LEEWAY ANGLE=      0.50853  DEGREES          RUDDER ANGLE=      3.10435DEGREES
         ----------------------------------------
         ----------------------------------------
         KVT=      7.50000  KNOTS          DGAMMA=     60.00000  DEGREES
         KVA=     11.17890  KNOTS          DBETTA=     35.52245  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
         BOAT SPEED=      5.34839  KNOTS          HEEL ANGLE=     24.68011  DEGREES
         LEEWAY ANGLE=      1.17645  DEGREES          RUDDER ANGLE=      3.94630DEGREES
         ----------------------------------------
         ----------------------------------------
         KVT=      7.50000  KNOTS          DGAMMA=     45.00000  DEGREES
         KVA=     11.17072  KNOTS          DBETTA=     28.34309  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
         BOAT SPEED=      4.52826  KNOTS          HEEL ANGLE=     25.90138  DEGREES
         LEEWAY ANGLE=      2.44491  DEGREES          RUDDER ANGLE=      3.91684DEGREES
         ----------------------------------------
         ----------------------------------------
         KVT=      7.50000  KNOTS          DGAMMA=     35.00000  DEGREES
         KVA=     10.53564  KNOTS          DBETTA=     24.09880  DEGREES
SUCCESSFUL CONVERGENCE
```

```
        ----------------------------------------
        KVT=      7.50000  KNOTS          DGAMMA=     80.00000  DEGREES
        KVA=     10.36289  KNOTS          DBETTA=     45.45833  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
        BOAT SPEED=      5.96515  KNOTS          HEEL ANGLE=     19.44243  DEGREES
        LEEWAY ANGLE=      0.50853  DEGREES          RUDDER ANGLE=      3.10435DEGREES
        ----------------------------------------
        ----------------------------------------
        KVT=      7.50000  KNOTS          DGAMMA=     60.00000  DEGREES
        KVA=     11.17890  KNOTS          DBETTA=     35.52245  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
        BOAT SPEED=      5.34839  KNOTS          HEEL ANGLE=     24.68011  DEGREES
        LEEWAY ANGLE=      1.17645  DEGREES          RUDDER ANGLE=      3.94630DEGREES
        ----------------------------------------
        ----------------------------------------
        KVT=      7.50000  KNOTS          DGAMMA=     45.00000  DEGREES
        KVA=     11.17072  KNOTS          DBETTA=     28.34309  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
        BOAT SPEED=      4.52826  KNOTS          HEEL ANGLE=     25.90138  DEGREES
        LEEWAY ANGLE=      2.44491  DEGREES          RUDDER ANGLE=      3.91684DEGREES
        ----------------------------------------
        ----------------------------------------
        KVT=      7.50000  KNOTS          DGAMMA=     35.00000  DEGREES
        KVA=     10.53564  KNOTS          DBETTA=     24.09880  DEGREES
SUCCESSFUL CONVERGENCE
```

```
ITER   =   4

         BOAT SPEED=      3.47308  KNOTS          HEEL ANGLE=     23.64365  DEGREES
         LEEWAY ANGLE=      4.47674  DEGREES          RUDDER ANGLE=      4.04634DEGREES
         ------------------------------------------------

         ------------------------------------------------

         KVT=     10.00000  KNOTS          DGAMMA=    180.00000  DEGREES
         KVA=      5.16953  KNOTS          DBETTA=    179.99990  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4

         BOAT SPEED=      4.83037  KNOTS          HEEL ANGLE=      0.00542  DEGREES
         LEEWAY ANGLE=     -0.00401  DEGREES          RUDDER ANGLE=      0.01243DEGREES
         ------------------------------------------------

         ------------------------------------------------

         KVT=     10.00000  KNOTS          DGAMMA=    160.00000  DEGREES
         KVA=      5.48727  KNOTS          DBETTA=    141.44290  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3

         BOAT SPEED=      5.10574  KNOTS          HEEL ANGLE=      0.08175  DEGREES
         LEEWAY ANGLE=      0.01586  DEGREES          RUDDER ANGLE=      0.02775DEGREES
         ------------------------------------------------

         ------------------------------------------------

         KVT=     10.00000  KNOTS          DGAMMA=    140.00000  DEGREES
         KVA=      6.67725  KNOTS          DBETTA=    105.70840  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3

         BOAT SPEED=      5.85245  KNOTS          HEEL ANGLE=      1.40412  DEGREES
         LEEWAY ANGLE=      0.10124  DEGREES          RUDDER ANGLE=      0.17259DEGREES
         ------------------------------------------------
```

```
        ---------------------------------------------

        KVT=     10.00000  KNOTS          DGAMMA=    120.00000  DEGREES

        KVA=      8.79442  KNOTS          DBETTA=     79.97887  DEGREES

SUCCESSFUL CONVERGENCE

ITER  =   8

        BOAT SPEED=      6.52654  KNOTS          HEEL ANGLE=      6.55590  DEGREES

        LEEWAY ANGLE=      0.10446  DEGREES          RUDDER ANGLE=      1.10168DEGREES

        ---------------------------------------------

        ---------------------------------------------

        KVT=     10.00000  KNOTS          DGAMMA=    100.00000  DEGREES

        KVA=     10.96851  KNOTS          DBETTA=     63.87666  DEGREES

SUCCESSFUL CONVERGENCE

ITER  =   4

        BOAT SPEED=      6.56510  KNOTS          HEEL ANGLE=     16.25755  DEGREES

        LEEWAY ANGLE=     -0.16120  DEGREES          RUDDER ANGLE=      3.55508DEGREES

        ---------------------------------------------

        ---------------------------------------------

        KVT=     10.00000  KNOTS          DGAMMA=     80.00000  DEGREES

        KVA=     12.85525  KNOTS          DBETTA=     50.00259  DEGREES

SUCCESSFUL CONVERGENCE

ITER  =   3

        BOAT SPEED=      6.52192  KNOTS          HEEL ANGLE=     27.24298  DEGREES

        LEEWAY ANGLE=     -0.33663  DEGREES          RUDDER ANGLE=      5.98752DEGREES

        ---------------------------------------------

        ---------------------------------------------

        KVT=     10.00000  KNOTS          DGAMMA=     60.00000  DEGREES

        KVA=     13.80846  KNOTS          DBETTA=     38.84161  DEGREES

SUCCESSFUL CONVERGENCE
```

```
ITER   =  5
         BOAT SPEED=      5.75414  KNOTS          HEEL ANGLE=     35.06798  DEGREES
         LEEWAY ANGLE=      0.37846  DEGREES          RUDDER ANGLE=      7.60845DEGREES
         ---------------------------------------------

         ---------------------------------------------
         KVT=     10.00000  KNOTS          DGAMMA=     45.00000  DEGREES
         KVA=     13.68682  KNOTS          DBETTA=     31.10666  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =  4
         BOAT SPEED=      4.64757  KNOTS          HEEL ANGLE=     37.00015  DEGREES
         LEEWAY ANGLE=      2.45695  DEGREES          RUDDER ANGLE=      8.19907DEGREES
         ---------------------------------------------

         ---------------------------------------------
         KVT=     10.00000  KNOTS          DGAMMA=     35.00000  DEGREES
         KVA=     12.49910  KNOTS          DBETTA=     27.31577  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =  7
         BOAT SPEED=      2.91379  KNOTS          HEEL ANGLE=     32.23439  DEGREES
         LEEWAY ANGLE=      7.24246  DEGREES          RUDDER ANGLE=     13.07657DEGREES
         ---------------------------------------------
```

```
ITMAX  =        10
IPRINT =         0
N      =         4
EPS1   =         1.0D-10
EPS2   =         1.0E-02

          XOLD(1)...XOLD( 4)

    1.000000E 01     0.000000E-01     0.000000E-01     0.000000E-01

         SOLUTIONS ARE COMPUTED FOR THE FOLLOWING TRUE WIND SPEEDS (KNOTS)

  5.00000   7.50000  10.00000

         SOLUTIONS ARE COMPUTED FOR THE FOLLOWING TRUE WIND ANGLES FOR EACH WIND SPEED

180.00000 160.00000 140.00000 120.00000 100.00000  80.00000  60.00000  45.00000  35.00000
```

LWL= 30.00000

DISPLACEMENT TO LENGTH= 225.00000

PRISMATIC= 0.53000

L/H= 14.76796

LCB= 53.00000

KINEMATIC VISCOSITY= 0.1279100E-04

DENSITY OF WATER= 1.99000

MEAN KEEL CHORD= 6.90000

MEAN RUDDER CHORD= 1.87537

ROUGHNESS AND CORRELATION FACTOR= 0.00000

FAIRBODY WETTED SURFACE= 215.25700

KEEL WETTED SURFACE= 63.01086

RUDDER WETTED SURFACE= 19.99725

TOTAL WETTED SURFACE= 298.26480

BWL /LWL= 0.30276

SAIL AREA= 900.00000

HEELING MOMENT ARM= 23.99541

PITCHING MOMENT ARM= 26.35417

DISTANCE FROM FP TO RUDDER STOCK= 28.49998

CLOSE HAULED LIFT COEF= 1.25000

RIG FORM DRAG COEF= 0.40000

CROSS SECTIONAL AREA OF RIG= 26.97595

SAIL FRICTIONAL COEF= 0.04000

INDUCED DRAG COEF / LIFT COEF**2= 0.13030

LATERAL AREA OF HULL= 121.29310

TRANSVERSE AREA OF HULL= 37.06689

DISTANCE BETWEEN CE SAIL AND FP= 13.93835

OFF WIND DRAG COEF= 0.00000

```
       OFF WIND LIFT COEF=      0.00000
       DISTANCE BETWEEN CE HULL AND FP=     13.93835
       DENSITY OF AIR=      0.00238
       HORIZONTAL DISTANCE FROM MAXIMUM DRAFT OF PROFILE MEASUREMENTS
0.00000   3.00000   6.00000   9.00000  16.50000
       PROFILE MEASUREMENTS
6.38000   6.25240   1.92985   1.42200   0.00000
       DRAFT OF CANOE BODY / TOTAL DRAFT=      0.31841
       HYDRODYNAMIC LIFT COEF=      0.11209
       LAMDA X LIFT / DRAG=      2.04978
       DISTANCE FROM LWL TO VERTICAL HYDRO CE=      2.12454
       *** RUDDER SECTION ***
       DISTANCE FROM LWL TO ROOT CHORD=      0.40628
       ROOT CHORD=      2.25000
       TIP CHORD=      1.50075
       RUDDER SPAN=      5.07766
       SWEEP ANGLE=      0.00000
       ASPECT RATIO=      5.41509
       MEAN CHORD=      1.87537
       DCL / DALPHA=      0.07057
       CROSS FLOW DRAG COEF=      0.56024
       DCM / DCL=      0.21654
       FORM DRAG COEF=      0.00650
       RUDDER AREA=      9.52251
       *** RIGHTING MOMENT SECTION ***
       METACENTRIC HEIGHT / LWL=      0.11534
       FROUDE NUMBER RIGHTING MOMENT COEF=   0.6089515E-04
```

```
NON LINEAR HYDROSTATIC COEF=   0.3767873E-03
DISTANCE BELOW LWL TO CG=      0.75000
*** SAIL SECTION ***
I=    47.17540          J=     15.72513
P=    42.88670          E=     14.29557
AB FOR TRI=      3.00000          AB MAIN=      3.00000
AB SAIL PLAN=      2.47280
CE SAIL PLAN AFT MAST=      0.60041
FORWARD OVERHANG=      2.38720
FREEBOARD=      3.71000
```

```
        ------------------------------------------------
        KVT=      5.00000   KNOTS          DGAMMA=    180.00000  DEGREES
        KVA=      2.36443   KNOTS          DBETTA=    179.99980  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   5
        BOAT SPEED=      2.63557  KNOTS          HEEL ANGLE=      0.00057  DEGREES
        LEEWAY ANGLE=     -0.00116  DEGREES          RUDDER ANGLE=      0.00433DEGREES
        ------------------------------------------------
        ------------------------------------------------
        KVT=      5.00000   KNOTS          DGAMMA=    160.00000  DEGREES
        KVA=      2.49134   KNOTS          DBETTA=    136.65290  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   2
        BOAT SPEED=      2.88579  KNOTS          HEEL ANGLE=      0.01554  DEGREES
        LEEWAY ANGLE=      0.02097  DEGREES          RUDDER ANGLE=      0.00262DEGREES
        ------------------------------------------------
NO CONVERGENCE
        KVT=      5.00000   KNOTS          DGAMMA=    140.00000  DEGREES
        KVA=      3.21880   KNOTS          DBETTA=     93.15175  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =  11
        BOAT SPEED=      3.65326  KNOTS          HEEL ANGLE=      0.24055  DEGREES
        LEEWAY ANGLE=      0.13603  DEGREES          RUDDER ANGLE=      0.02736DEGREES
        ------------------------------------------------
        KVT=      5.00000   KNOTS          DGAMMA=    120.00000  DEGREES
        KVA=      4.83768   KNOTS          DBETTA=     63.51920  DEGREES
SUCCESSFUL CONVERGENCE
```

```
ITER   =   4
         BOAT SPEED=      4.65673  KNOTS          HEEL ANGLE=      1.80063  DEGREES
         LEEWAY ANGLE=      0.54518  DEGREES          RUDDER ANGLE=      0.06240DEGREES
         ------------------------------------------------
         ------------------------------------------------
         KVT=      5.00000  KNOTS          DGAMMA=    100.00000  DEGREES
         KVA=      6.53116  KNOTS          DBETTA=     48.93198  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
         BOAT SPEED=      5.15885  KNOTS          HEEL ANGLE=      4.21832  DEGREES
         LEEWAY ANGLE=      0.98065  DEGREES          RUDDER ANGLE=      0.20861DEGREES
         ------------------------------------------------
         ------------------------------------------------
         KVT=      5.00000  KNOTS          DGAMMA=     80.00000  DEGREES
         KVA=      7.84539  KNOTS          DBETTA=     38.87585  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
         BOAT SPEED=      5.23940  KNOTS          HEEL ANGLE=      6.78553  DEGREES
         LEEWAY ANGLE=      1.49549  DEGREES          RUDDER ANGLE=      0.37304DEGREES
         ------------------------------------------------
         ------------------------------------------------
         KVT=      5.00000  KNOTS          DGAMMA=     60.00000  DEGREES
         KVA=      8.57841  KNOTS          DBETTA=     30.31612  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
         BOAT SPEED=      4.90367  KNOTS          HEEL ANGLE=      8.62737  DEGREES
         LEEWAY ANGLE=      2.18603  DEGREES          RUDDER ANGLE=      0.45298DEGREES
         ------------------------------------------------
```

```
        ---------------------------------------------
        KVT=      5.00000  KNOTS          DGAMMA=    45.00000  DEGREES
        KVA=      8.39471  KNOTS          DBETTA=    24.90797  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
        BOAT SPEED=      4.07831  KNOTS          HEEL ANGLE=     8.49245  DEGREES
        LEEWAY ANGLE=      3.16383  DEGREES          RUDDER ANGLE=     0.43054DEGREES
        ---------------------------------------------
        ---------------------------------------------
        KVT=      5.00000  KNOTS          DGAMMA=    35.00000  DEGREES
        KVA=      7.81175  KNOTS          DBETTA=    21.53836  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
        BOAT SPEED=      3.17022  KNOTS          HEEL ANGLE=     7.44635  DEGREES
        LEEWAY ANGLE=      4.64773  DEGREES          RUDDER ANGLE=     0.38519DEGREES
        ---------------------------------------------
        ---------------------------------------------
        KVT=      7.50000  KNOTS          DGAMMA=   180.00000  DEGREES
        KVA=      3.59100  KNOTS          DBETTA=   179.99980  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
        BOAT SPEED=      3.91276  KNOTS          HEEL ANGLE=     0.00121  DEGREES
        LEEWAY ANGLE=      0.00031  DEGREES          RUDDER ANGLE=     0.00054DEGREES
        ---------------------------------------------
        ---------------------------------------------
        KVT=      7.50000  KNOTS          DGAMMA=   160.00000  DEGREES
        KVA=      3.81778  KNOTS          DBETTA=   137.78660  DEGREES
SUCCESSFUL CONVERGENCE
```

```
ITER   =   2
         BOAT SPEED=      4.21828  KNOTS          HEEL ANGLE=      0.03173  DEGREES
         LEEWAY ANGLE=      0.02009  DEGREES          RUDDER ANGLE=      0.00429DEGREES
         ------------------------------------------------
         ------------------------------------------------
         KVT=      7.50000  KNOTS          DGAMMA=    140.00000  DEGREES
         KVA=      4.86734  KNOTS          DBETTA=     97.92107  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
         BOAT SPEED=      5.07021  KNOTS          HEEL ANGLE=      0.49961  DEGREES
         LEEWAY ANGLE=      0.14829  DEGREES          RUDDER ANGLE=      0.01619DEGREES
         ------------------------------------------------
         ------------------------------------------------
         KVT=      7.50000  KNOTS          DGAMMA=    120.00000  DEGREES
         KVA=      6.84121  KNOTS          DBETTA=     71.69914  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
         BOAT SPEED=      5.90355  KNOTS          HEEL ANGLE=      2.91928  DEGREES
         LEEWAY ANGLE=      0.51083  DEGREES          RUDDER ANGLE=      0.18288DEGREES
         ------------------------------------------------
         ------------------------------------------------
         KVT=      7.50000  KNOTS          DGAMMA=    100.00000  DEGREES
         KVA=      9.05576  KNOTS          DBETTA=     54.64867  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
         BOAT SPEED=      6.53885  KNOTS          HEEL ANGLE=      7.42339  DEGREES
         LEEWAY ANGLE=      0.95508  DEGREES          RUDDER ANGLE=      0.56130DEGREES
         ------------------------------------------------
```

```
        ------------------------------------------------
        KVT=      7.50000  KNOTS          DGAMMA=     80.00000  DEGREES
        KVA=     10.80911  KNOTS          DBETTA=     43.10342  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
        BOAT SPEED=      6.58876  KNOTS          HEEL ANGLE=     12.24898  DEGREES
        LEEWAY ANGLE=      1.51378  DEGREES          RUDDER ANGLE=      0.99877DEGREES
        ------------------------------------------------
        ------------------------------------------------
        KVT=      7.50000  KNOTS          DGAMMA=     60.00000  DEGREES
        KVA=     11.74616  KNOTS          DBETTA=     33.57051  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
        BOAT SPEED=      6.03699  KNOTS          HEEL ANGLE=     15.68644  DEGREES
        LEEWAY ANGLE=      2.41843  DEGREES          RUDDER ANGLE=      1.26121DEGREES
        ------------------------------------------------
        ------------------------------------------------
        KVT=      7.50000  KNOTS          DGAMMA=     45.00000  DEGREES
        KVA=     11.81018  KNOTS          DBETTA=     26.68242  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
        BOAT SPEED=      5.24840  KNOTS          HEEL ANGLE=     16.53915  DEGREES
        LEEWAY ANGLE=      3.57327  DEGREES          RUDDER ANGLE=      1.20193DEGREES
        ------------------------------------------------
        ------------------------------------------------
        KVT=      7.50000  KNOTS          DGAMMA=     35.00000  DEGREES
        KVA=     11.24568  KNOTS          DBETTA=     22.49055  DEGREES
SUCCESSFUL CONVERGENCE
```

```
ITER   =   4
         BOAT SPEED=     4.24629  KNOTS          HEEL ANGLE=     15.29806  DEGREES
         LEEWAY ANGLE=      5.22368  DEGREES          RUDDER ANGLE=      1.09039DEGREES
         ---------------------------------------------
         ---------------------------------------------
         KVT=     10.00000  KNOTS          DGAMMA=    180.00000  DEGREES
         KVA=      4.96443  KNOTS          DBETTA=    179.99980  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
         BOAT SPEED=      5.03554  KNOTS          HEEL ANGLE=      0.00228  DEGREES
         LEEWAY ANGLE=     -0.00046  DEGREES          RUDDER ANGLE=      0.00276DEGREES
         ---------------------------------------------
         ---------------------------------------------
         KVT=     10.00000  KNOTS          DGAMMA=    160.00000  DEGREES
         KVA=      5.32662  KNOTS          DBETTA=    140.05190  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
         BOAT SPEED=      5.31337  KNOTS          HEEL ANGLE=      0.04492  DEGREES
         LEEWAY ANGLE=      0.01862  DEGREES          RUDDER ANGLE=      0.00731DEGREES
         ---------------------------------------------
         ---------------------------------------------
         KVT=     10.00000  KNOTS          DGAMMA=    140.00000  DEGREES
         KVA=      6.61337  KNOTS          DBETTA=    103.60230  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
         BOAT SPEED=      6.10511  KNOTS          HEEL ANGLE=      0.78191  DEGREES
         LEEWAY ANGLE=      0.14843  DEGREES          RUDDER ANGLE=      0.04948DEGREES
         ---------------------------------------------
```

```
        ---------------------------------------------
        KVT=     10.00000  KNOTS          DGAMMA=    120.00000  DEGREES
        KVA=      8.88492  KNOTS          DBETTA=     77.08757  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   9
        BOAT SPEED=      6.98967  KNOTS          HEEL ANGLE=      4.09941  DEGREES
        LEEWAY ANGLE=      0.45382  DEGREES          RUDDER ANGLE=      0.35205DEGREES
        ---------------------------------------------
        ---------------------------------------------
        KVT=     10.00000  KNOTS          DGAMMA=    100.00000  DEGREES
        KVA=     11.29239  KNOTS          DBETTA=     60.70335  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   8
        BOAT SPEED=      7.26006  KNOTS          HEEL ANGLE=     10.27948  DEGREES
        LEEWAY ANGLE=      0.89417  DEGREES          RUDDER ANGLE=      1.12386DEGREES
        ---------------------------------------------
        ---------------------------------------------
        KVT=     10.00000  KNOTS          DGAMMA=     80.00000  DEGREES
        KVA=     13.33439  KNOTS          DBETTA=     47.60773  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   3
        BOAT SPEED=      7.25288  KNOTS          HEEL ANGLE=     17.39751  DEGREES
        LEEWAY ANGLE=      1.48165  DEGREES          RUDDER ANGLE=      2.01724DEGREES
        ---------------------------------------------
        ---------------------------------------------
        KVT=     10.00000  KNOTS          DGAMMA=     60.00000  DEGREES
        KVA=     14.65839  KNOTS          DBETTA=     36.21414  DEGREES
SUCCESSFUL CONVERGENCE
```

```
ITER   =   5
         BOAT SPEED=     6.82657  KNOTS          HEEL ANGLE=    23.44096  DEGREES
         LEEWAY ANGLE=     2.54576  DEGREES          RUDDER ANGLE=     2.50608DEGREES
         ---------------------------------------------
         ---------------------------------------------
         KVT=     10.00000  KNOTS          DGAMMA=    45.00000  DEGREES
         KVA=     14.70452  KNOTS          DBETTA=    28.74271  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
         BOAT SPEED=     5.82167  KNOTS          HEEL ANGLE=    24.95070  DEGREES
         LEEWAY ANGLE=     4.21530  DEGREES          RUDDER ANGLE=     2.51346DEGREES
         ---------------------------------------------
         ---------------------------------------------
         KVT=     10.00000  KNOTS          DGAMMA=    35.00000  DEGREES
         KVA=     14.17157  KNOTS          DBETTA=    23.87466  DEGREES
SUCCESSFUL CONVERGENCE
ITER   =   4
         BOAT SPEED=     4.76666  KNOTS          HEEL ANGLE=    23.88383  DEGREES
         LEEWAY ANGLE=     6.43894  DEGREES          RUDDER ANGLE=     2.34001DEGREES
         ---------------------------------------------
```

Thesis
M925 Munger
Prediction of sailing
boat performance.

103480

thesM925
Prediction of sailing boat performance.
3 2768 001 92556 3
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